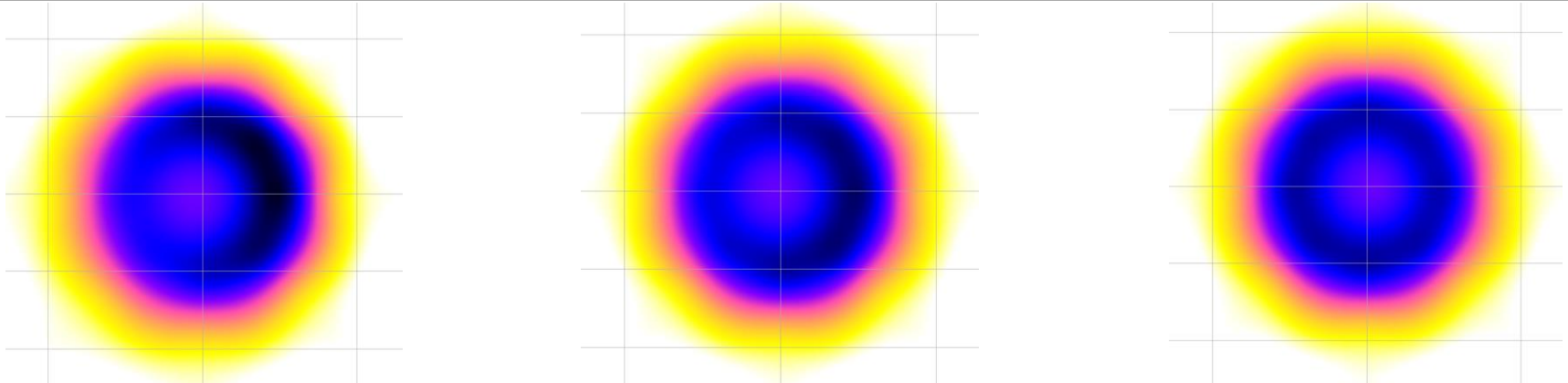
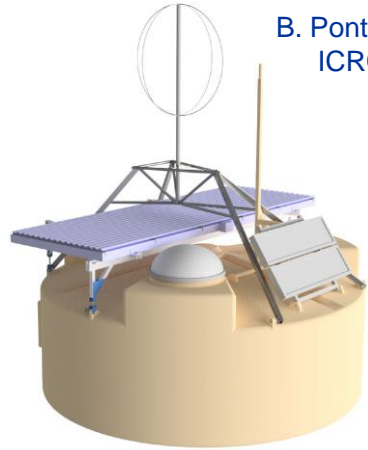


Reconstructing inclined extensive air showers from radio measurements

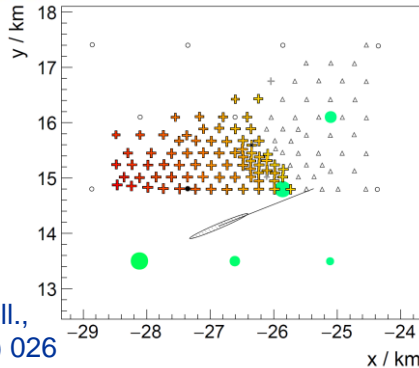
Tim Huege (KIT & VUB), Felix Schlüter (KIT & UNSAM)



Inclined showers are of high interest



B. Pont for Auger,
ICRC 2019



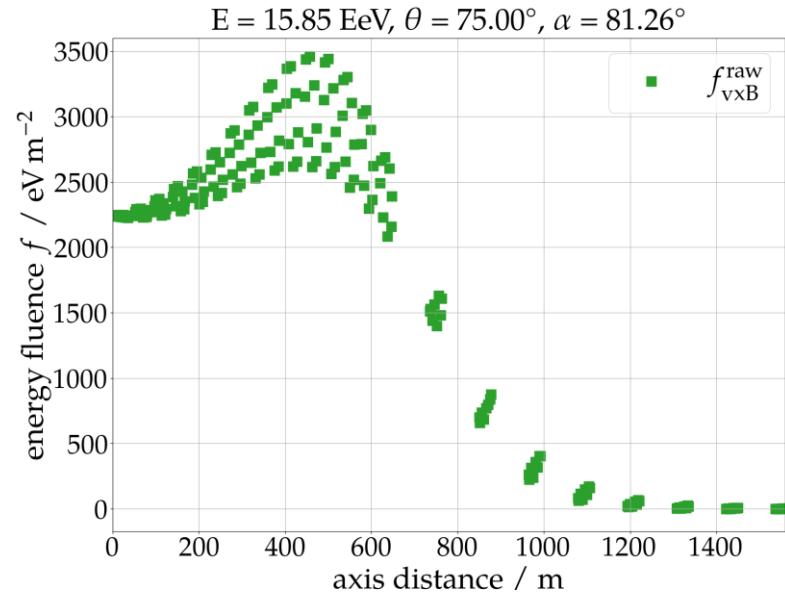
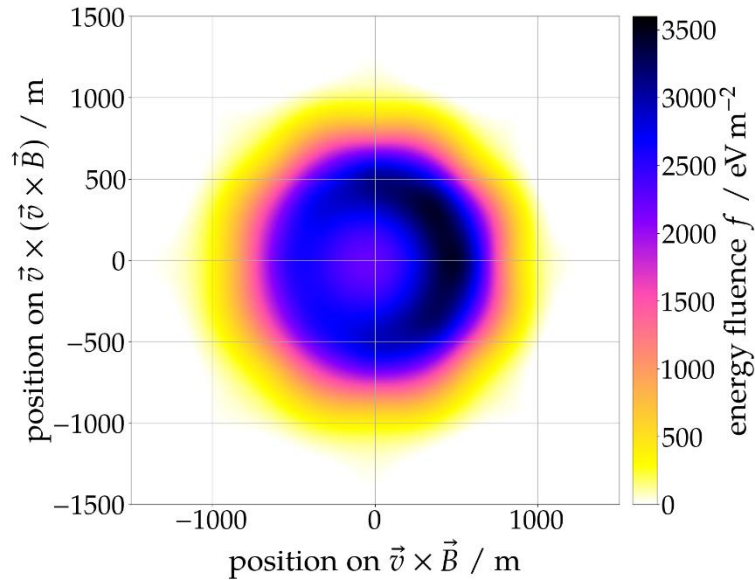
Pierre Auger Coll.,
JCAP 1810 (2018) 026

- inclined EAS have been long-predicted to possess large radio-emission footprints
- inclined EAS have been measured by AERA
- the Pierre Auger Collaboration is building the AugerPrime Radio Detector, 1660 antennas on 3,000 km², for showers with $\theta > 65^\circ$
- the GRAND collaboration plans up to 200,000 antennas on 200,000 km²
- we need reliable reconstruction algorithms

Basis of this study

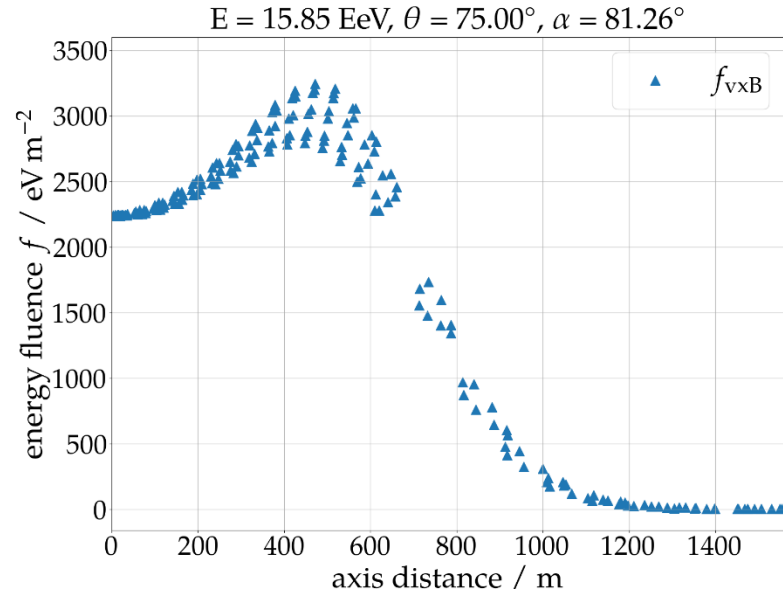
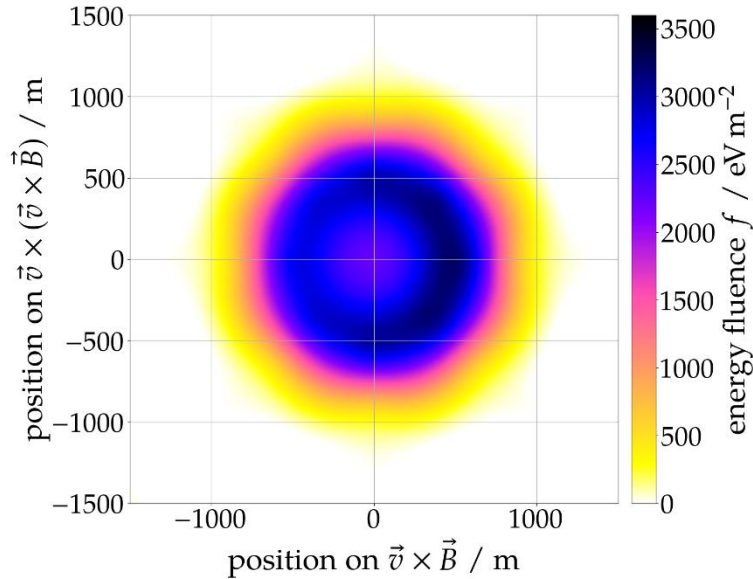
- CORSIKA/CoREAS v7.7 with QGSJETII-04 and UrQMD
- simulations filtered to the 30-80 MHz band
- energies from $10^{18.4}$ to $10^{20.2}$ eV
- zenith angles from 65° to 85° , excluding showers with $\alpha < 20^\circ$
- optimized thinning at $5e-6$ (derivation) and $1e-6$ (performance check)
- atmospheres and magnetic field as at Pierre Auger Observatory

1: Convert to shower axis & apply core fit



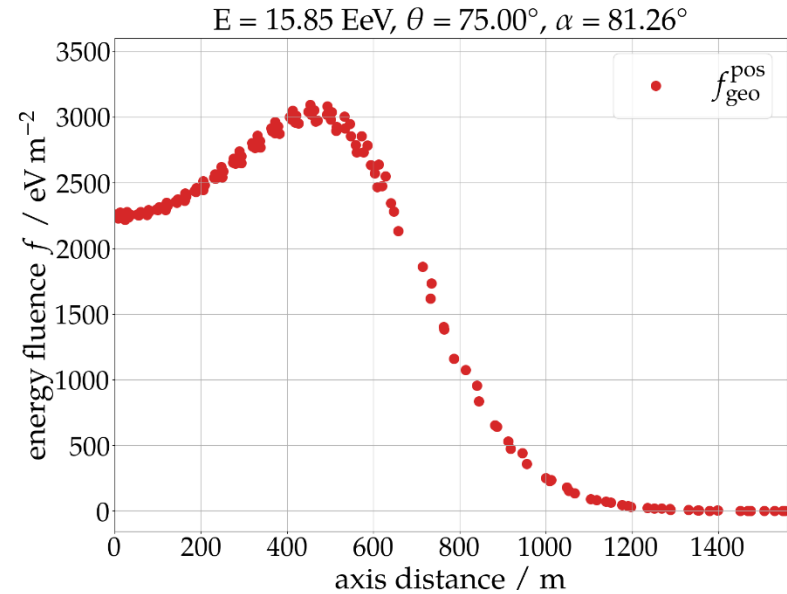
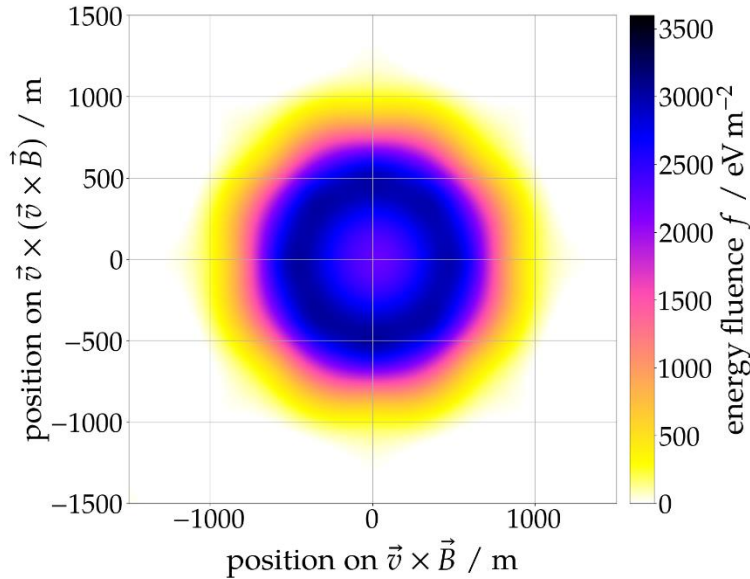
- allow for core shift due to atmospheric refraction (see [arXiv:2005.06775](https://arxiv.org/abs/2005.06775))
- significant asymmetries remain in shower plane

2: Apply geometrical early-late correction



- geometrical early-late correction improves symmetry ([arXiv:1908.07840](https://arxiv.org/abs/1908.07840))
- corrects axis distance and energy fluence for a given source distance

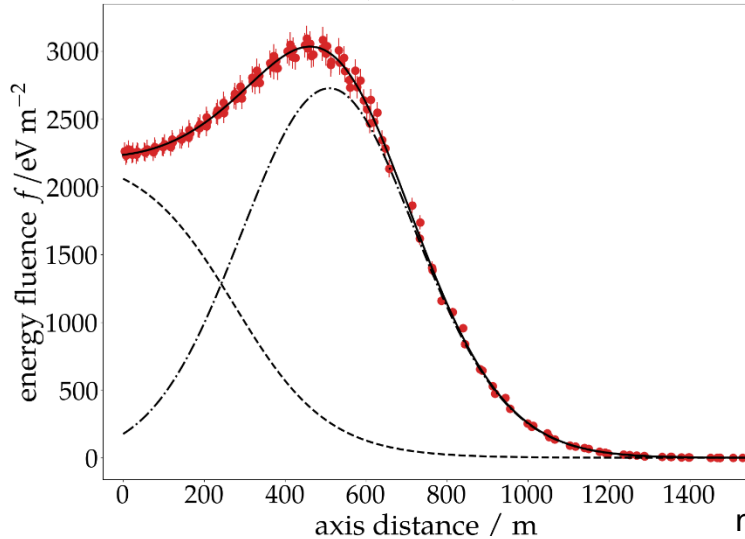
3: Calculate pure geomagnetic emission



- deduct charge-excess via known polarisation properties
- pure geomagnetic emission component is rotationally symmetric

4: Fit a radially symmetric LDF

$E = 15.85 \text{ EeV}, \theta = 75.00^\circ, \alpha = 81.26^\circ$



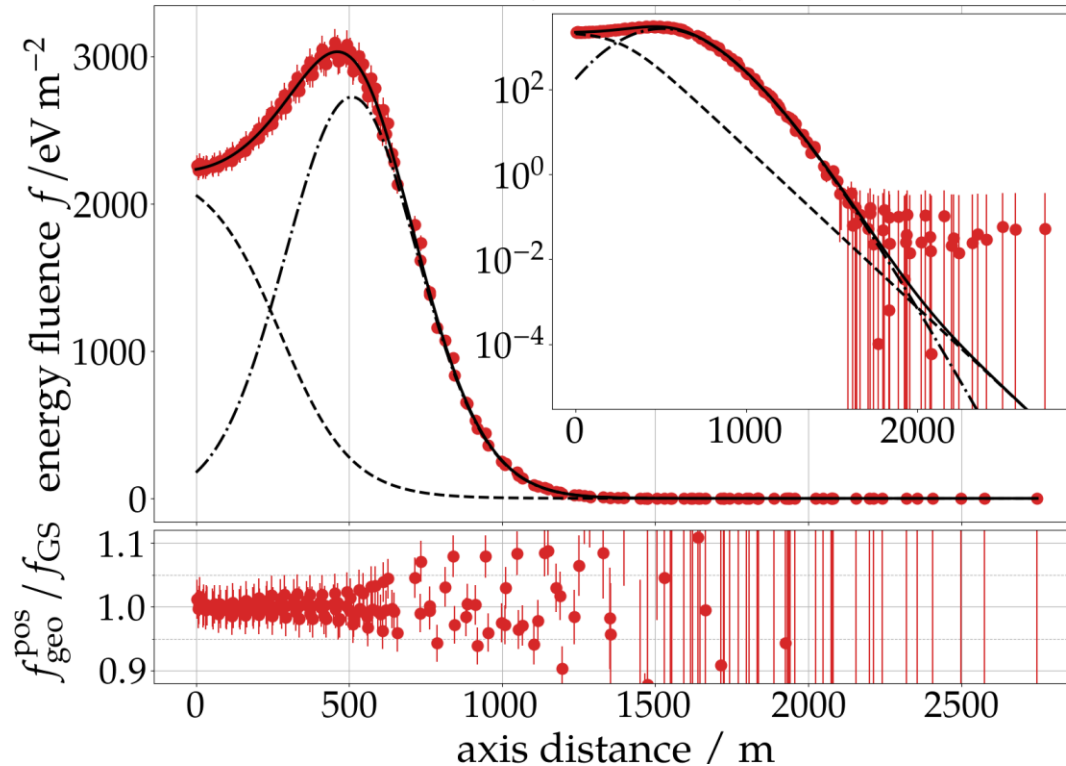
$$f_{GS}(r) = f_0 \left[\exp \left(- \left(\frac{r - r_0}{\sigma} \right)^p \right) + \frac{a_{rel}}{1 + \exp \left(s \cdot \left(\frac{r}{r_0} - r_{02} \right) \right)} \right]$$

f_0 : normalization
 σ : width of Gaussian
 p : ~2, cf. b
 a_{rel} : relative amplitude of Sigmoid vs. Gauss
 s : shape parameters
 r_0 : position of Gaussian
 r_{02} : shape parameters

- function changed from ICRC2019 for a better fit at large distances
- 7 parameters plus 2 core coordinates, too many for practical application

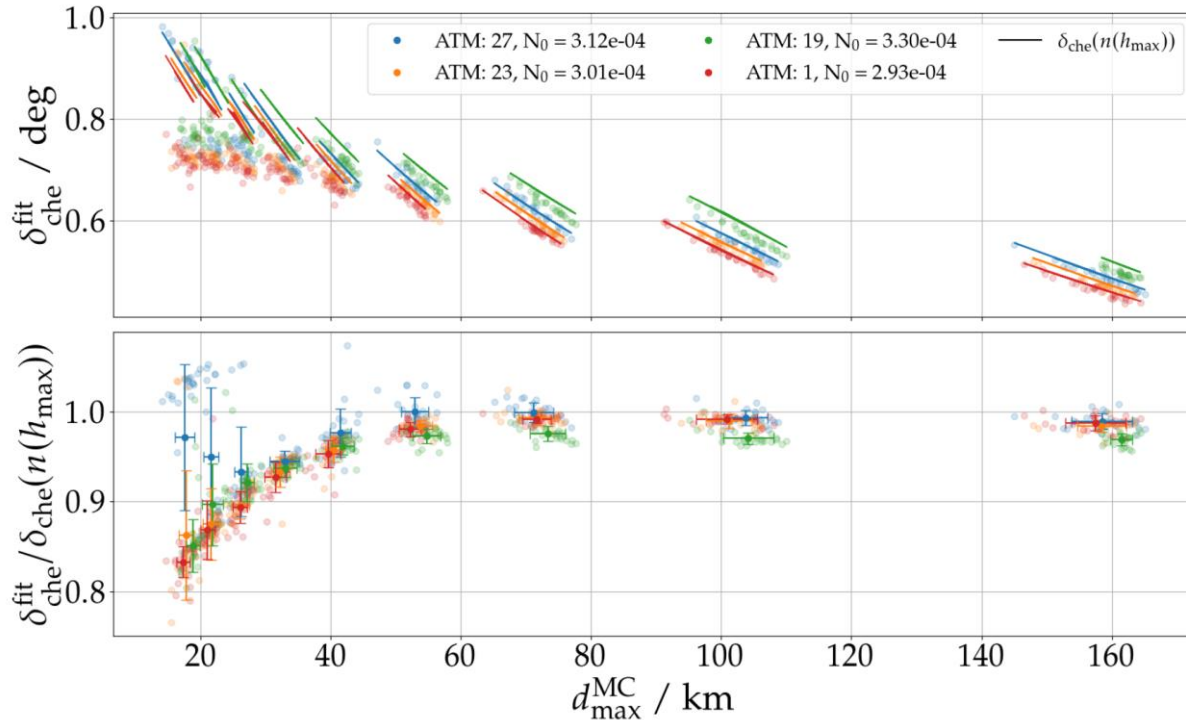
4: Performance of Gauss-Sigmoid fit function

$E = 15.85 \text{ EeV}, \theta = 75.00^\circ, \alpha = 81.26^\circ$



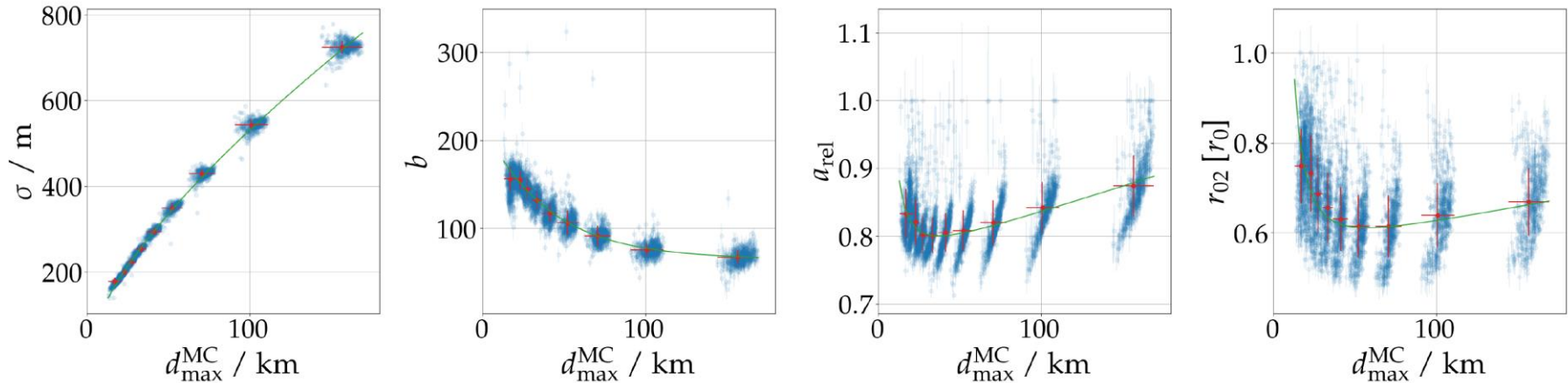
- very good fit over the complete distance range
- artifacts from particle thinning visible at largest distances, care taken that fit not biased by these

5: Reduce number of parameters



- position of Gauss corresponds to Cherenkov radius calculated from refractive index at X_{\max} !
- some deviations at lowest zenith angles

5: Recuce number of parameters



- shape parameter s is set to $s = 5$ (ensures Sigmoid dominant in center)
- other parameters can be parameterized as $f(\text{distance to } X_{\max})$
- second-order influence of X_{\max} value, but decided not to parameterize
- out of 7 fit parameters, 6 successfully fixed or correlated to d_{\max}

6: Parameterization of charge-excess fraction

- so far determined from polarisation, but impractical in presence of noise
- therefore parameterize charge-excess fraction

$$a_{ce} = \left[0.348 - \frac{d_{\max}}{850.9 \text{ km}} \right] \cdot \frac{r}{d_{\max}} \cdot \exp \left[\frac{r}{622.3 \text{ m}} \right] \cdot \left[\left(\frac{\rho_{\max}}{0.428 \text{ kg m}^{-3}} \right)^{3.32} - 0.0057 \right]$$

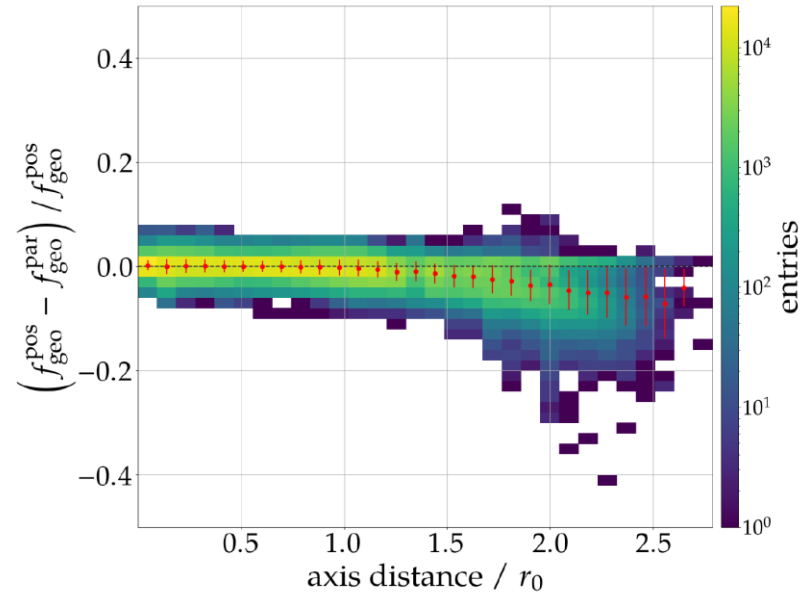
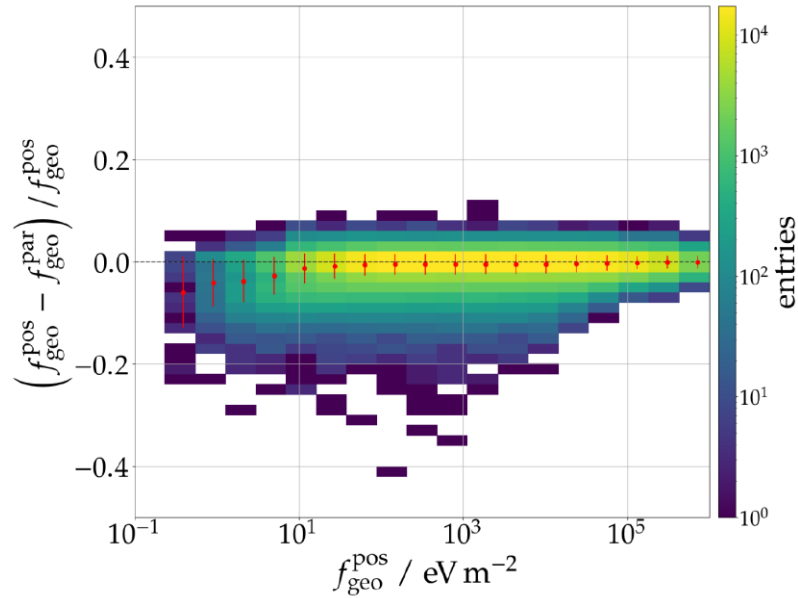
source dist.
off-axis angle
axis distance
atmospheric density correction

- with this, we can calculate geomagnetic energy fluence at any location by subtraction of charge-excess fluence from $\mathbf{v} \times \mathbf{B}$ measurement

$$f_{\text{geo}}^{\text{par}} = \frac{f_{\mathbf{v} \times \mathbf{B}}}{\left(1 + \frac{\cos(\phi)}{|\sin(\alpha)|} \cdot \sqrt{a(r, d_{\max}, \rho_{\max})} \right)^2}$$

cf. Glaser et al. JCAP 09 (2016) 024 and
 Astroparticle Physics 104 (2019) 64-77

6: Performance of charge-excess parametrization



- agreement of charge-excess parameterization with direct calculation agrees on average within 2%

7: Final fit function

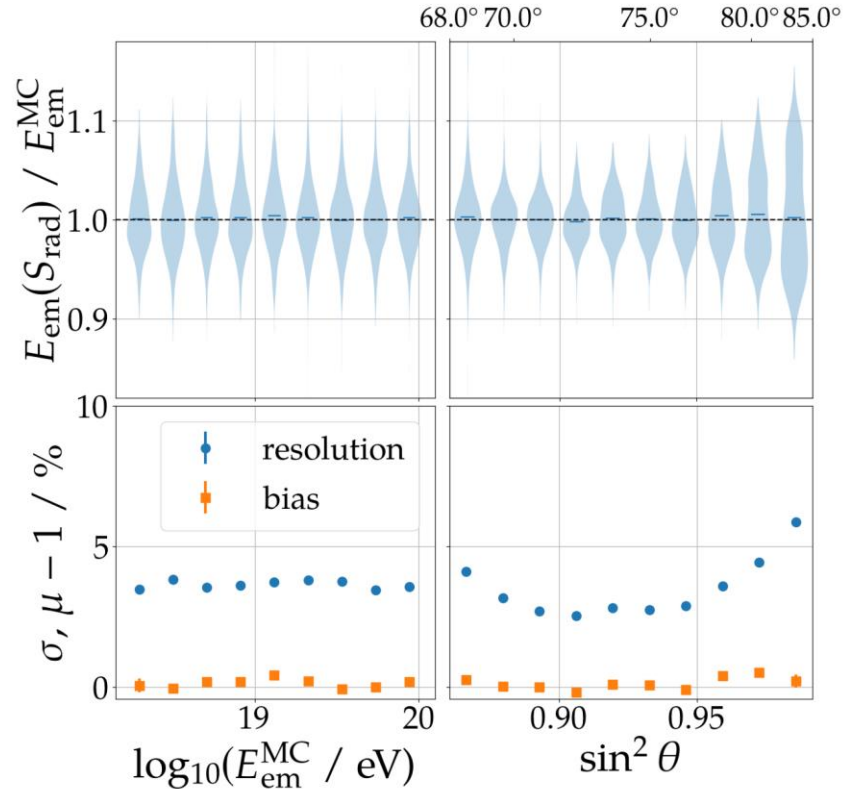
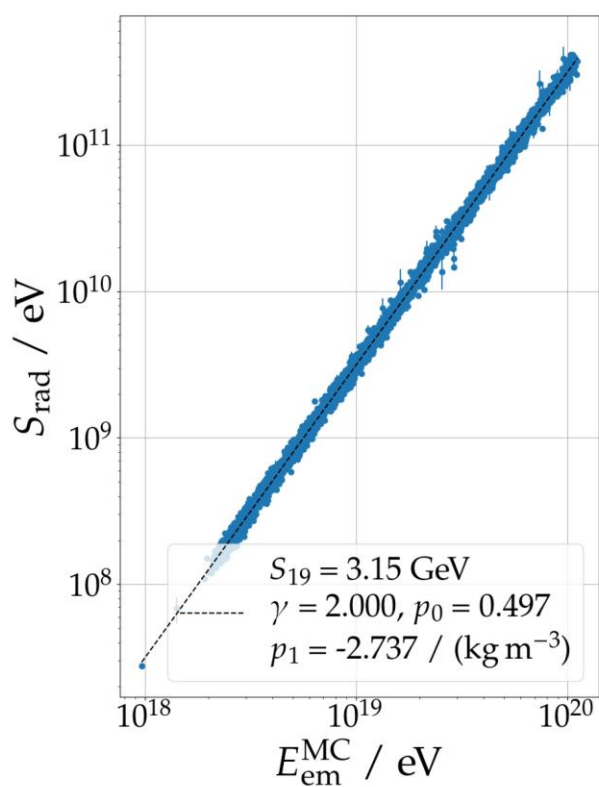
- fit with 4 free parameters: geomagnetic radiation energy, d_{\max} , core x/y

$$f_{\text{geo}}(r, E_{\text{geo}}, d_{\max}) = E_{\text{geo}} \frac{f_{\text{GS}}(r, d_{\max})}{2\pi \int_0^{5r_0} f_{\text{GS}}(r, d_{\max}) r \, dr}$$

- then apply geomagnetic angle and atmospheric density correction to get „corrected geomagnetic radiation energy“ S_{geo}
- finally correlate S_{geo} with shower electromagnetic energy

$$S_{\text{geo}} = S_{19} \cdot \left(\frac{E_{\text{em}}}{10 \text{ EeV}} \right)^\gamma$$

7: Test performance on 1.5 km grid simulations



- use MC start values - intrinsic resolution
- quadratic scaling
- negligible bias
- resolution <5%

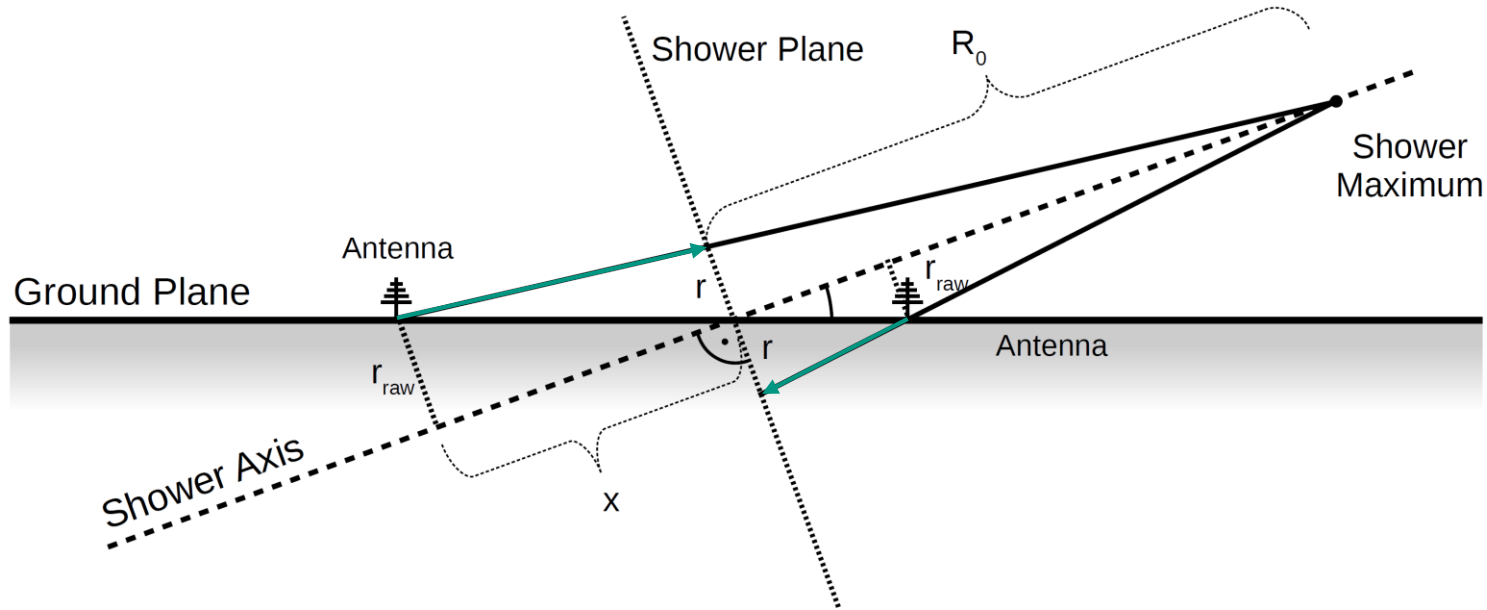
Conclusions

- we have developed a signal model and reconstruction for inclined EAS
- we fit the symmetric geomagnetic emission with a Gauss-sigmoid LDF
- the fit has two free parameters plus two core coordinates
- the intrinsic energy resolution is better than 5% on a 1.5 km grid
- can be used for AugerPrime Radio Detector, likely GRAND

- see it in action in talk by F. Schlüter, PoS(ICRC2021)262

Backup

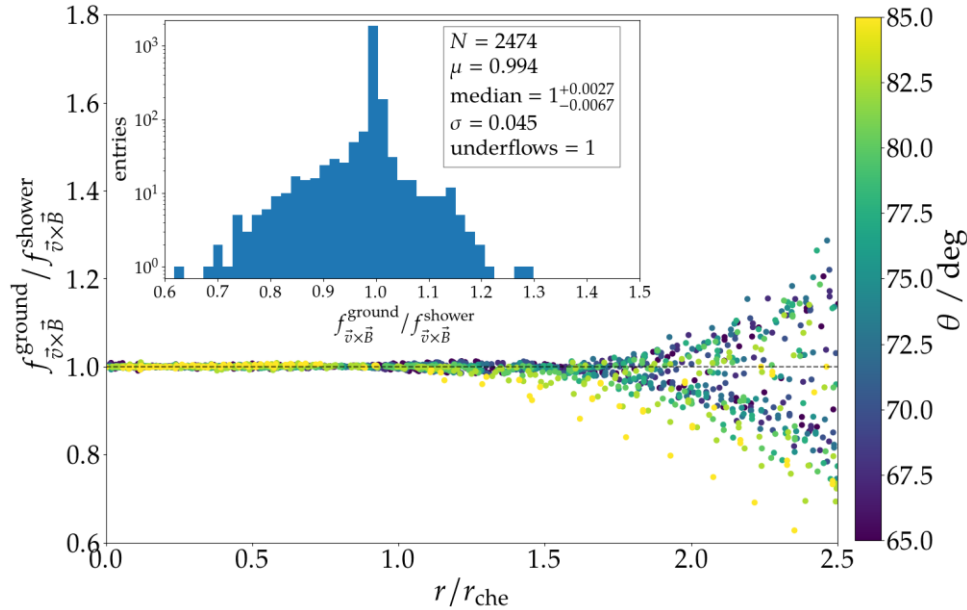
Correcting for early-late asymmetries



- correcting axis distances and energy fluences

$$f = f_{\text{raw}} \cdot \left(\frac{R}{R_0} \right)^2 \quad r = r_{\text{raw}} \cdot \frac{R_0}{R} \quad R \equiv R_0 + x$$

Performance of early-late correction



- most significant deviations are at large lateral distances and large zenith angles

Determining charge-excess fraction directly

$$f_{\text{geo}}^{\text{pos}} = \left(\sqrt{f_{\mathbf{v} \times \mathbf{B}}} - \frac{\cos(\phi)}{|\sin(\phi)|} \cdot \sqrt{f_{\mathbf{v} \times \mathbf{v} \times \mathbf{B}}} \right)^2$$
$$f_{\text{ce}}^{\text{pos}} = \frac{1}{\sin^2(\phi)} \cdot f_{\mathbf{v} \times \mathbf{v} \times \mathbf{B}}.$$

- for a given observation position, the charge-excess fraction can be determined directly via the known polarisation characteristics of the geomagnetic and charge-excess contributions, cf. Glaser et al., *Astroparticle Physics* 104 (2019) 64-77

Parameter correlations

$$r_0 = \tan(\delta_{\text{che}}) \cdot d_{\text{max}}, \quad \delta_{\text{che}} = \cos^{-1} \left(\frac{1}{n(h(d_{\text{max}}))} \right)$$

$$\sigma = \left(0.132 \cdot \left(\frac{d_{\text{max}} - 5 \text{ km}}{\text{m}} \right)^{0.714} + 56.3 \right) \text{ m}$$

$$p(r) = \begin{cases} 2 & r \leq r_0 \\ 2 \cdot (r_0/r)^{b/1000} & r > r_0 \end{cases}, \quad b = 154.9 \cdot \exp \left(-\frac{d_{\text{max}}}{40.0 \text{ km}} \right) + 64.9,$$

$$a_{\text{rel}} = 0.757 + \frac{d_{\text{max}}}{1301.4 \text{ km}} + \frac{19.8 \text{ km}^2}{d_{\text{max}}^2},$$

$$r_{02} = 0.552 + \frac{d_{\text{max}}}{1454.2 \text{ km}} + \frac{66.2 \text{ km}^2}{d_{\text{max}}^2}.$$