

A Numerical Approach to Angular Distributions in Hadronic Cascades

International Cosmic Ray Conference – 2021



CARLSBERG FOUNDATION

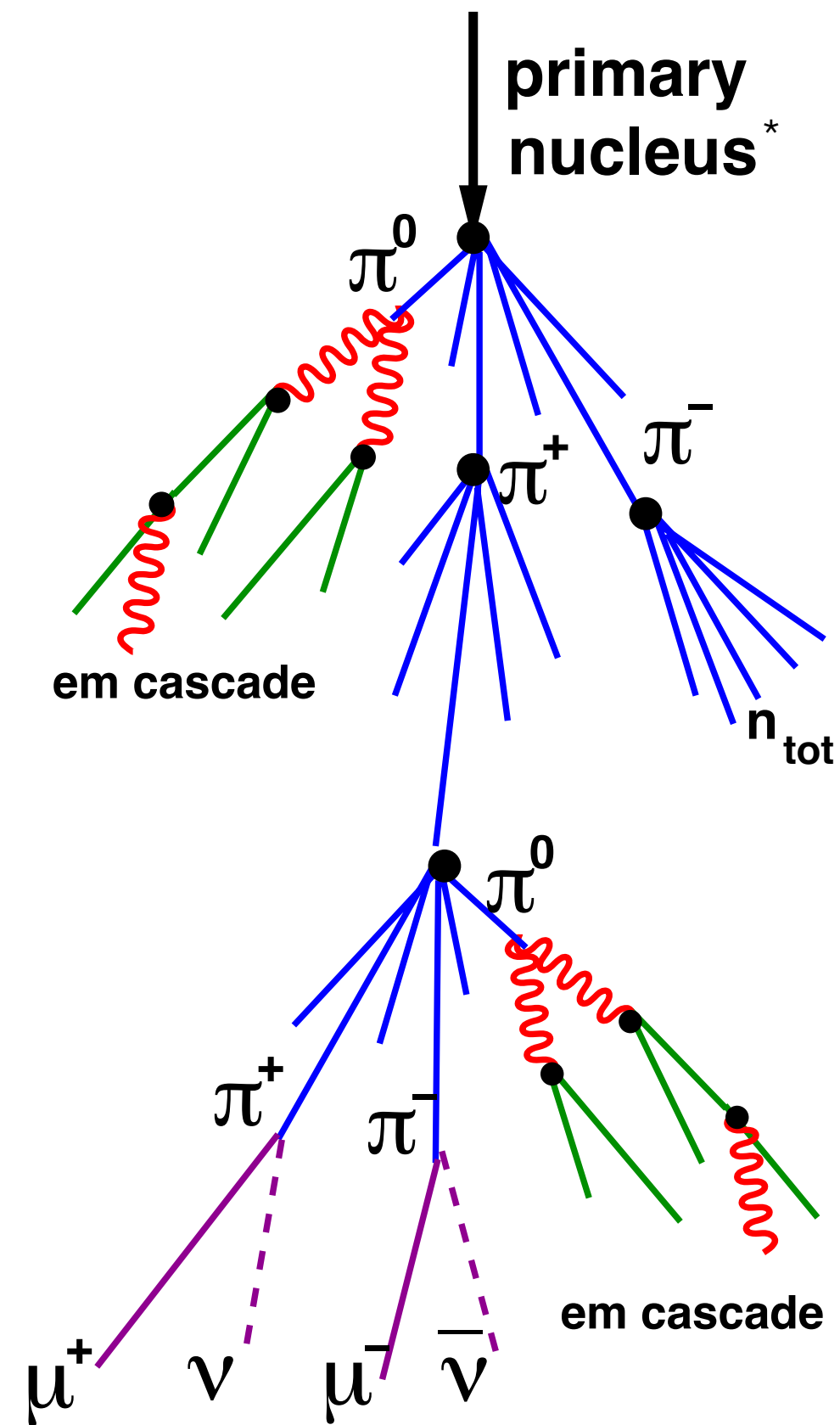
UNIVERSITY OF
COPENHAGEN

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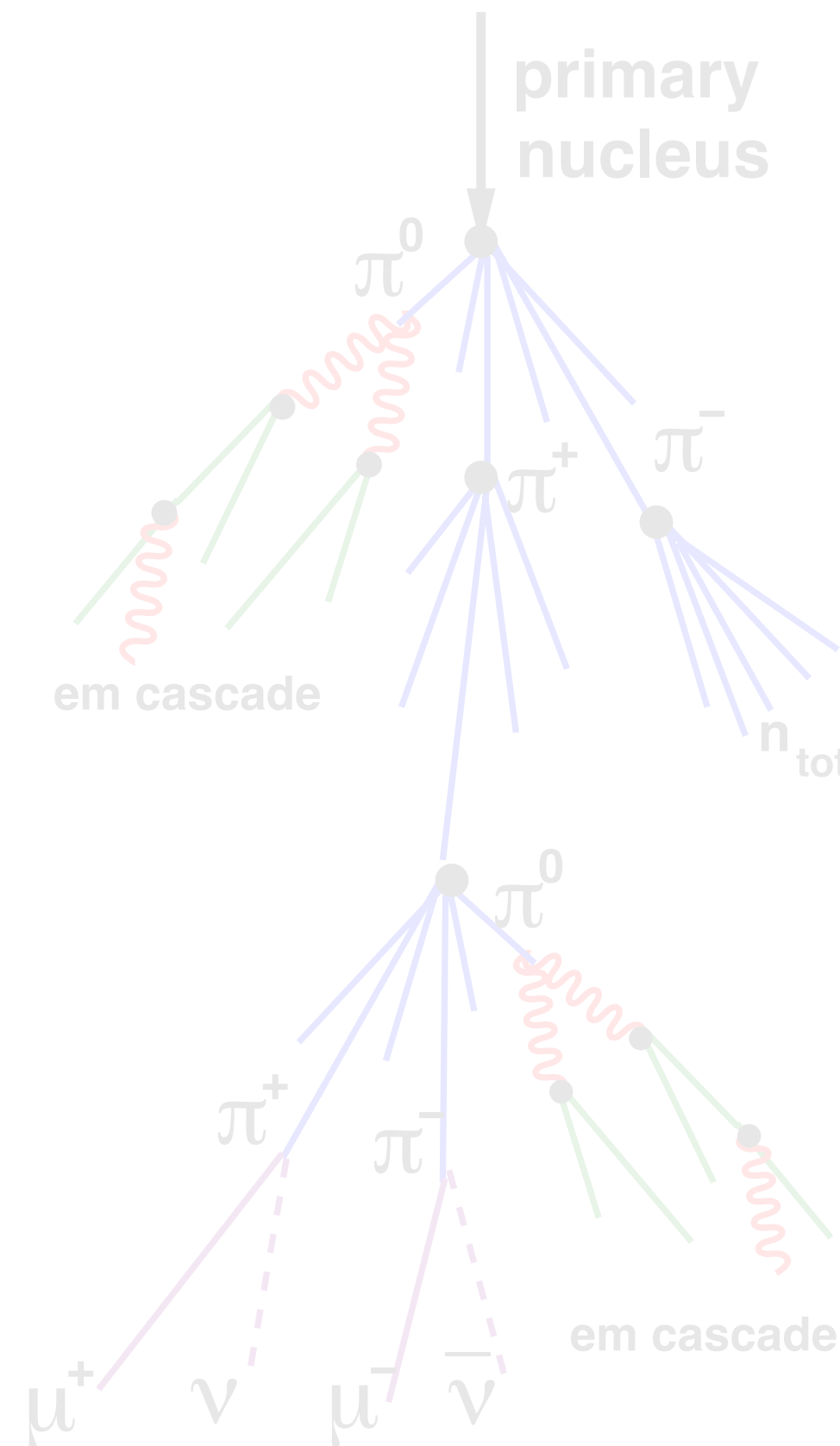
²Institute of Cosmic Ray Research, University of Tokyo

Hadronic cascades



- > Central to the evolution of air showers;
- > Rich in secondary particles, which are widely spread at low energies;
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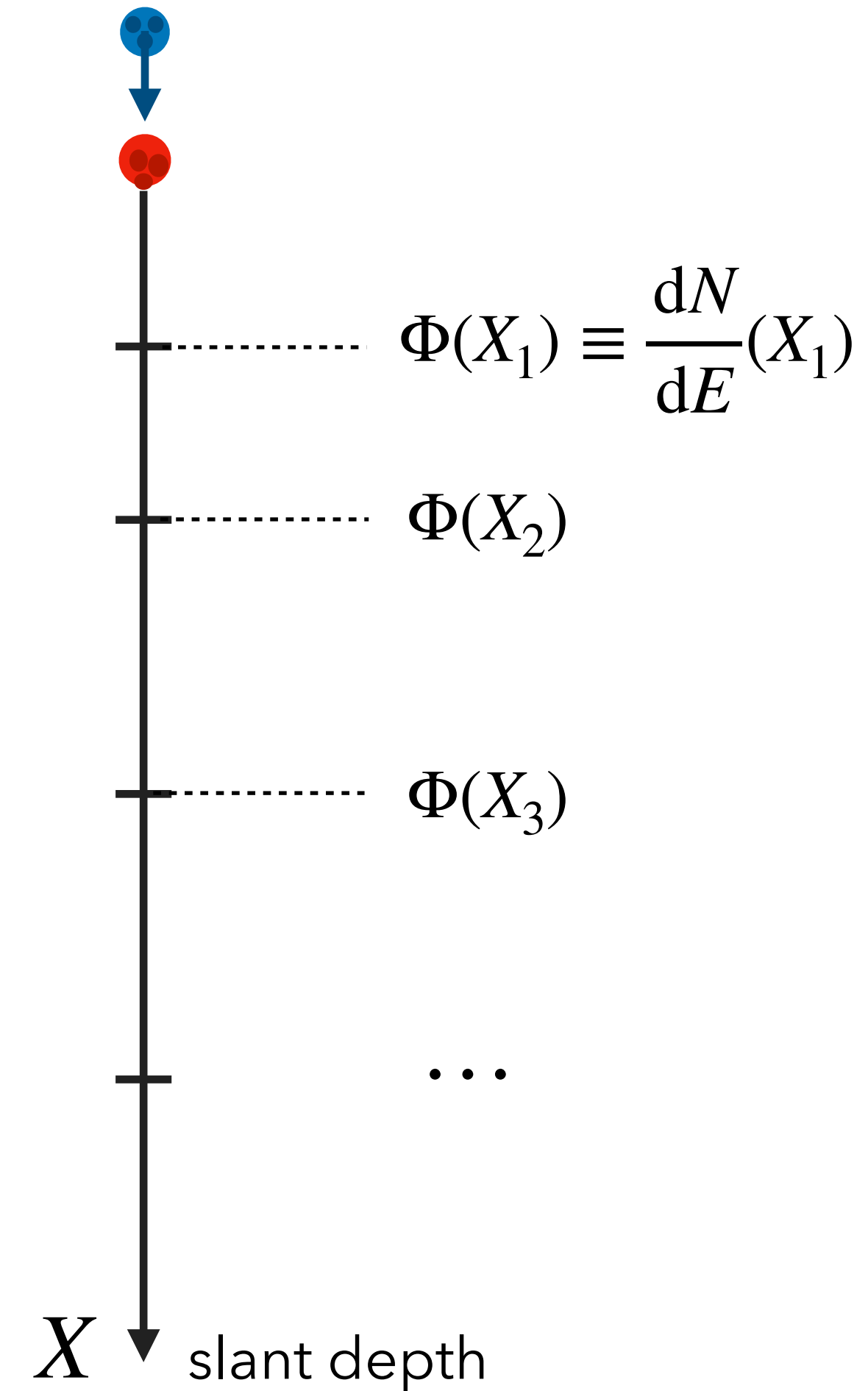
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- > Use MCEq*, a state-of-the-art numerical software for 1D cascade development;
- > Extend MCEq from **1D (X)** to 2D ($X+\theta$);



* – Matrix Cascade Equations;
<https://github.com/afedynitch/MCEq>

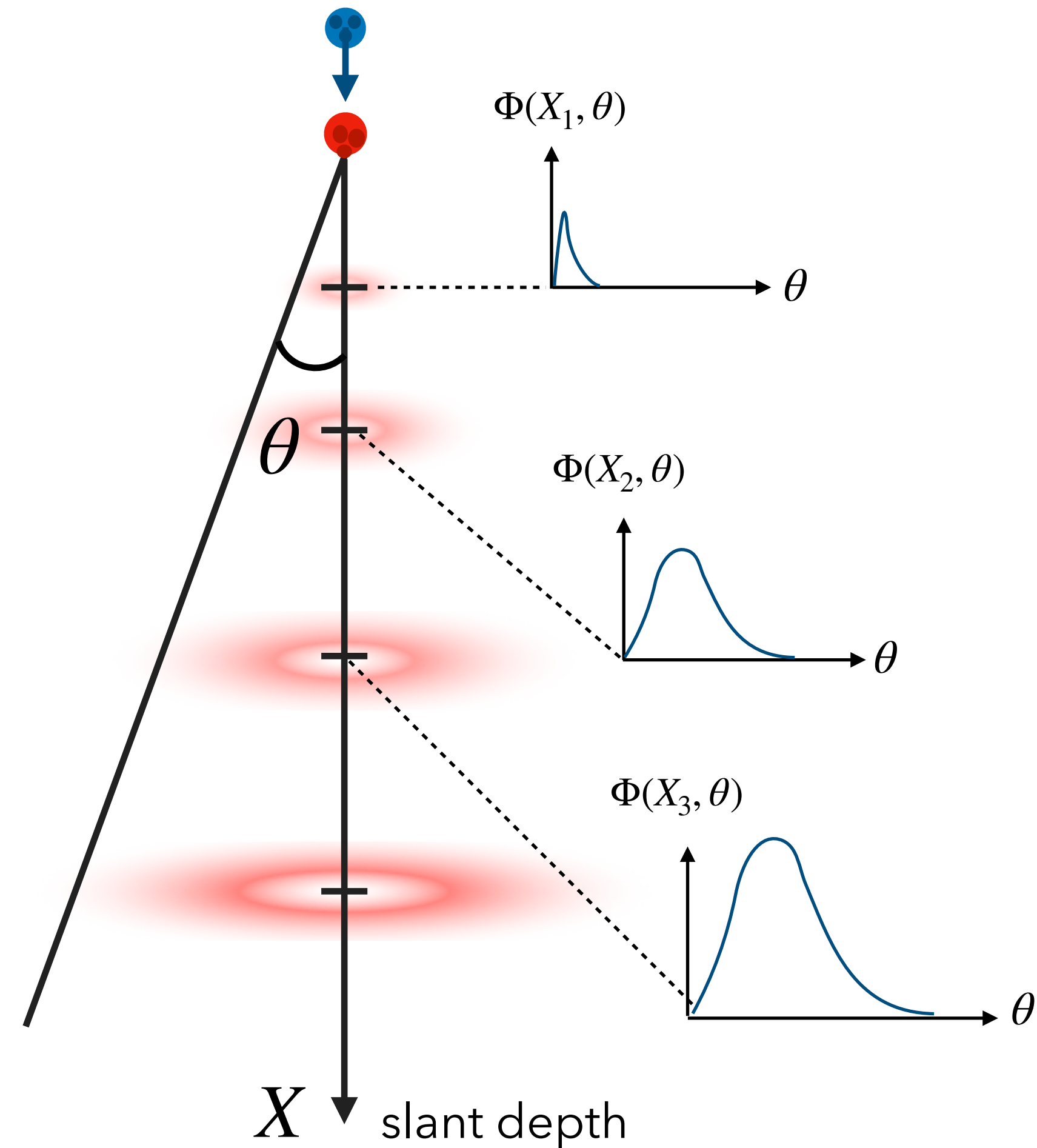
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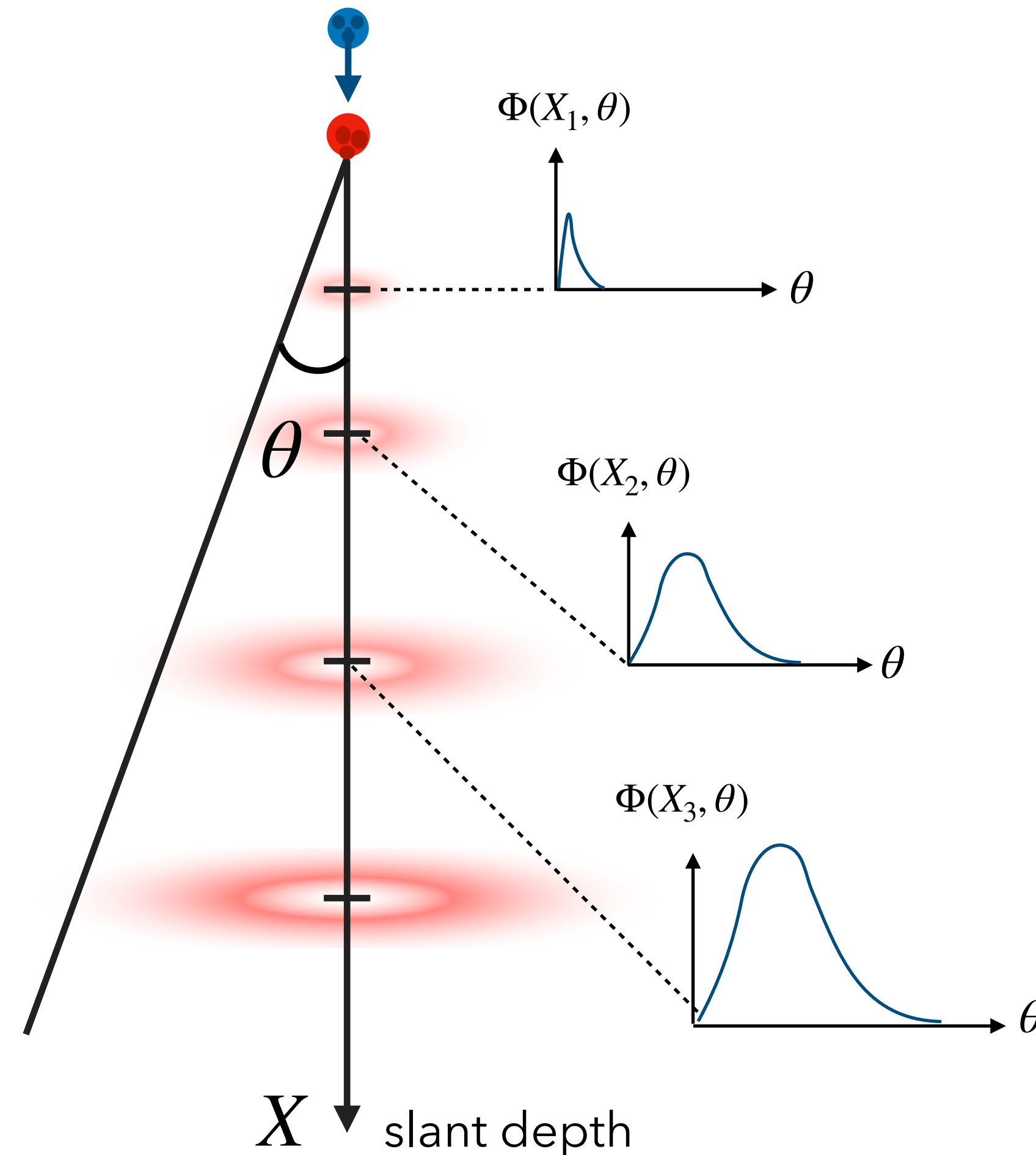


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- > Applications – fast and flexible modelling of **LE atmospheric ν fluxes**.



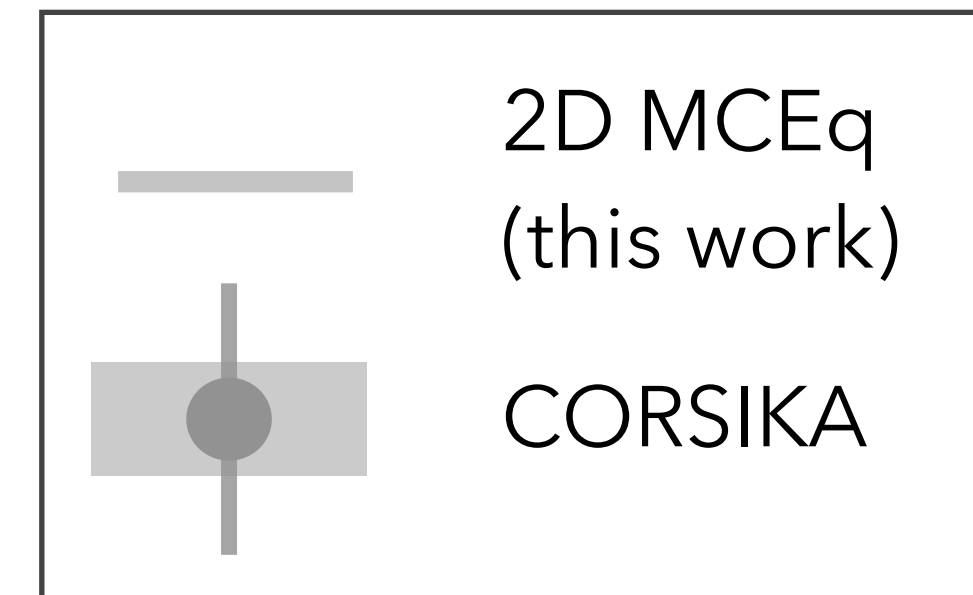
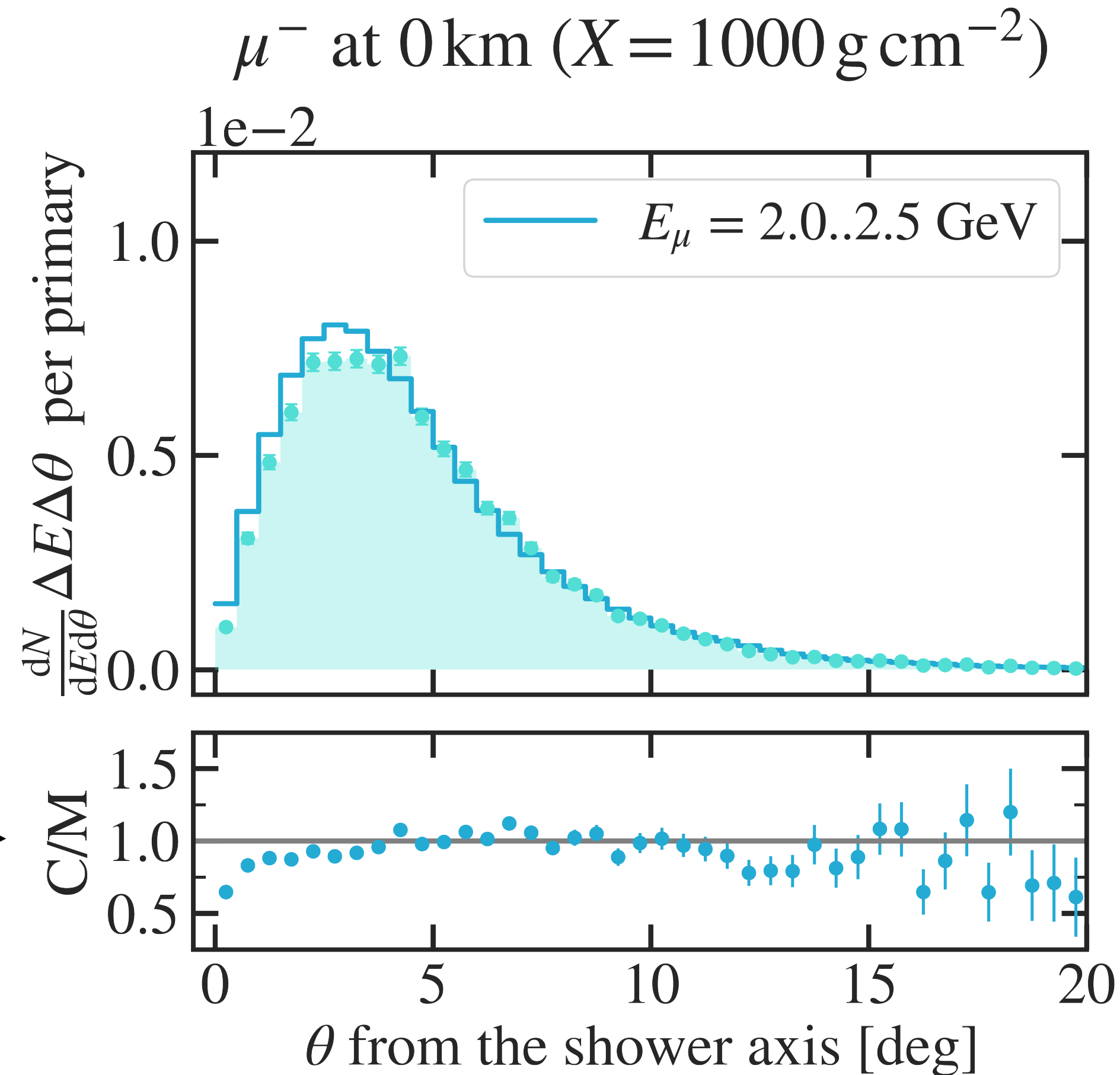
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Selected results

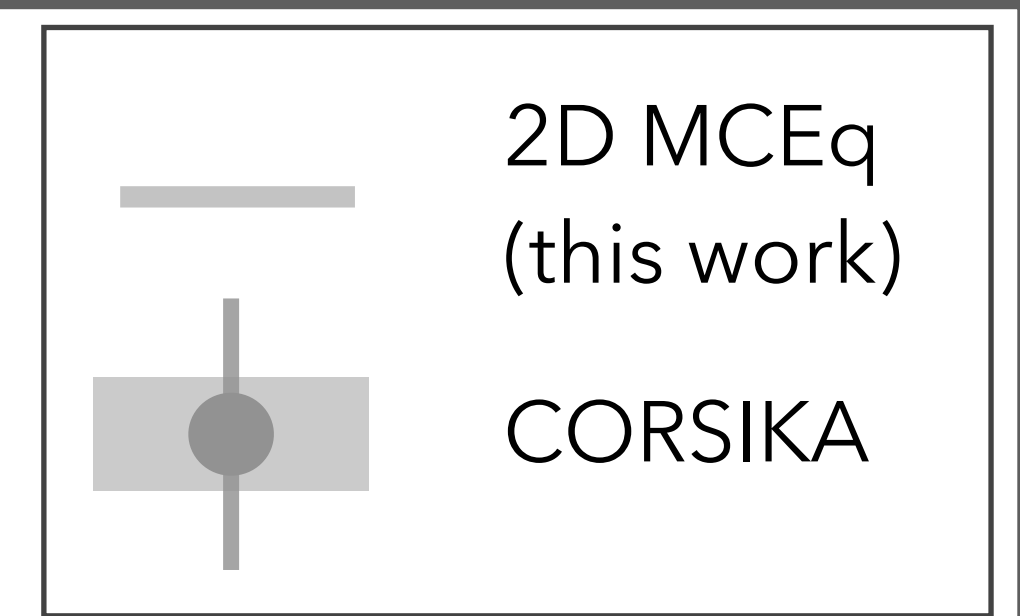
- > Develop a **100 GeV proton cascade in the Earth's atmosphere** using 2D MCEq;
- > Use CORSIKA as the benchmark Monte Carlo;

> Compare the angular distributions of the **secondary muons**:

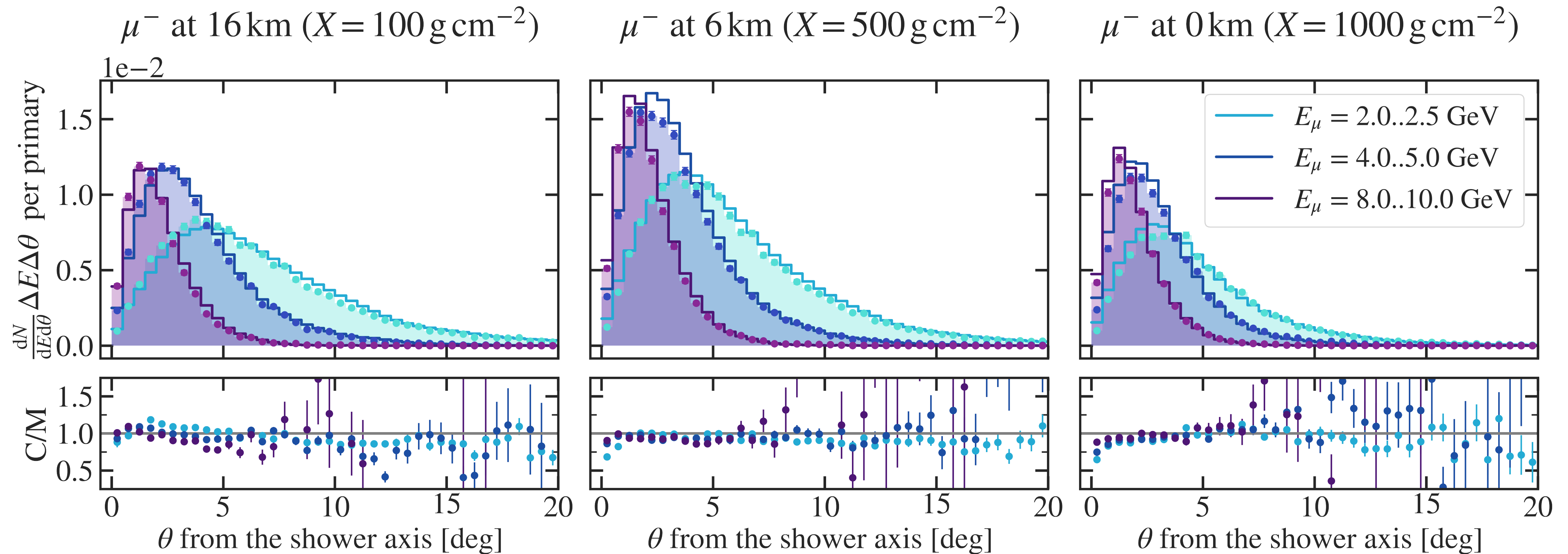
CORSIKA:MCEq



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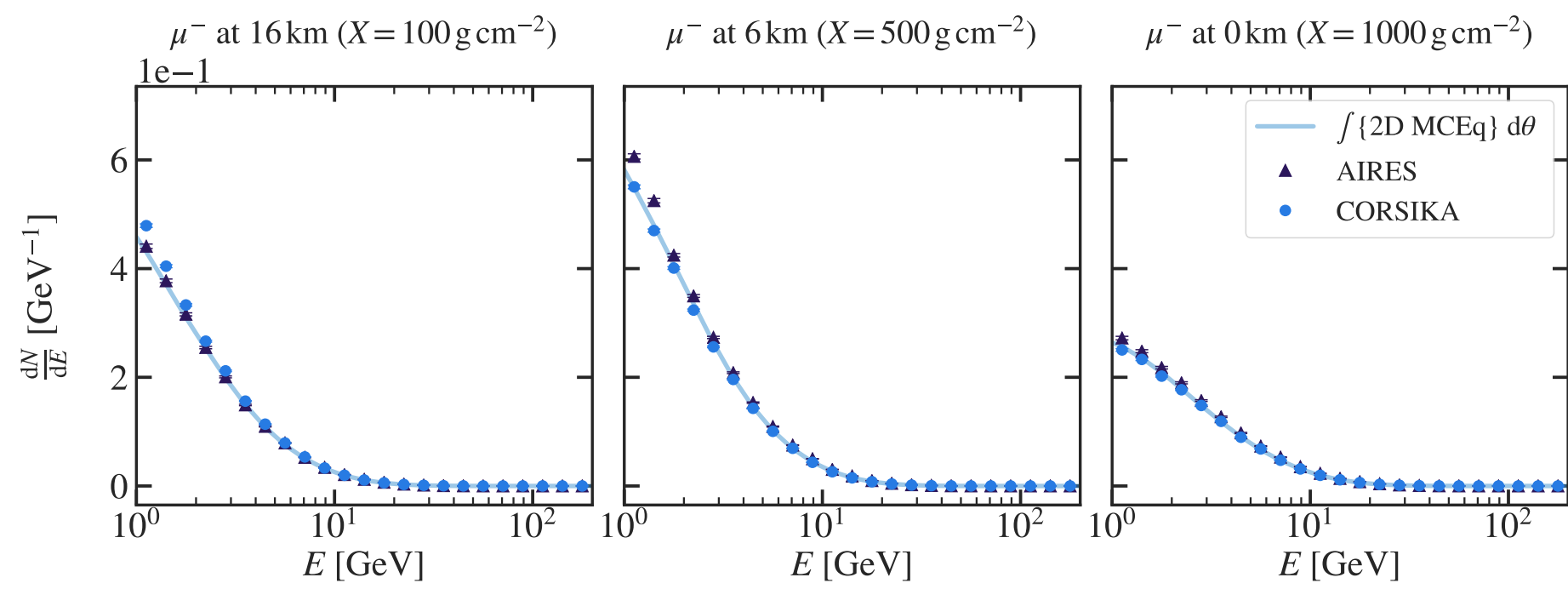
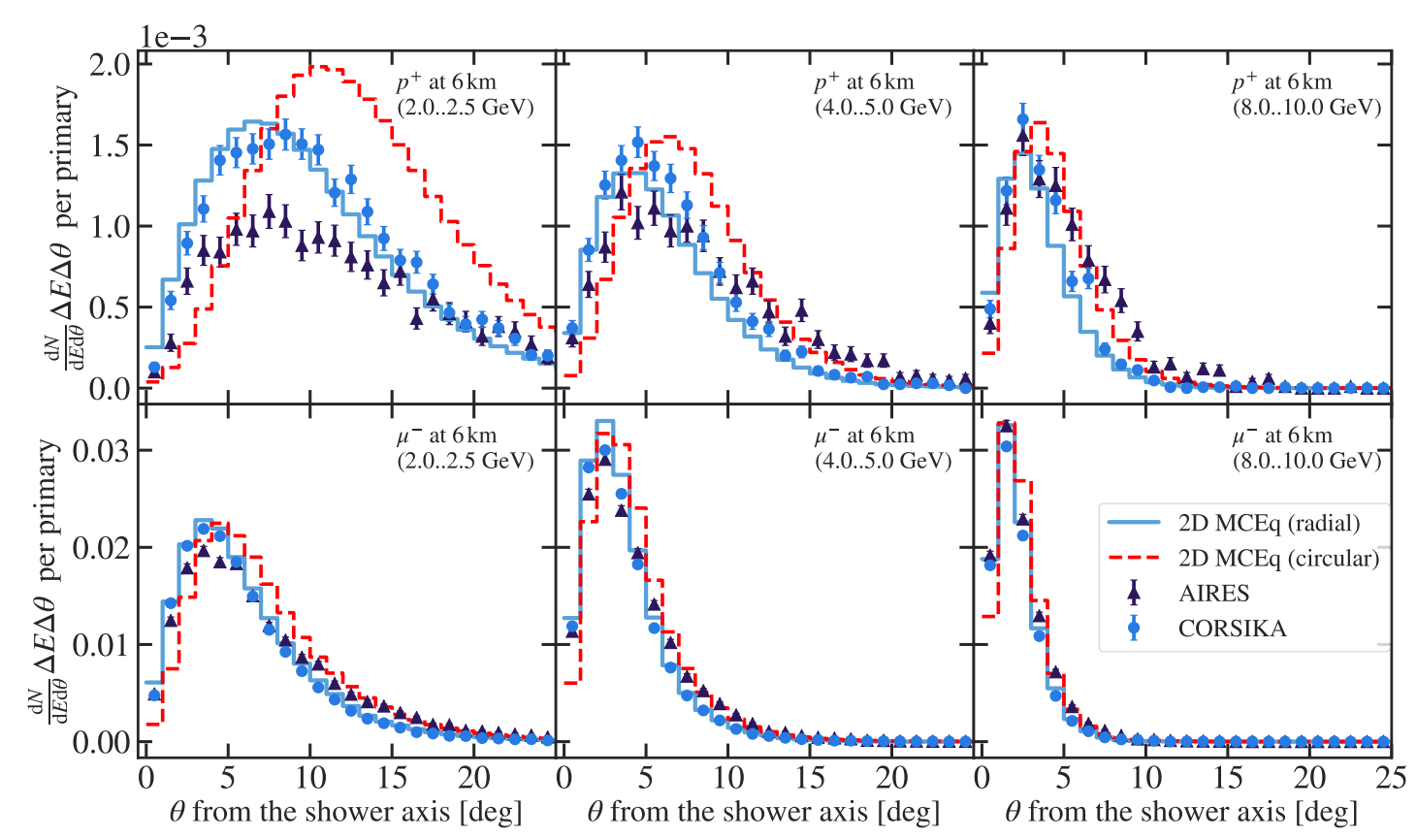
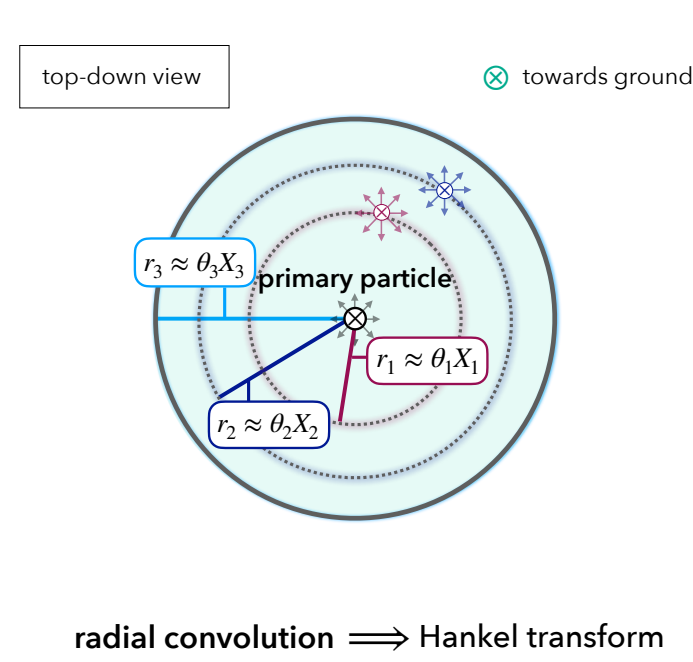
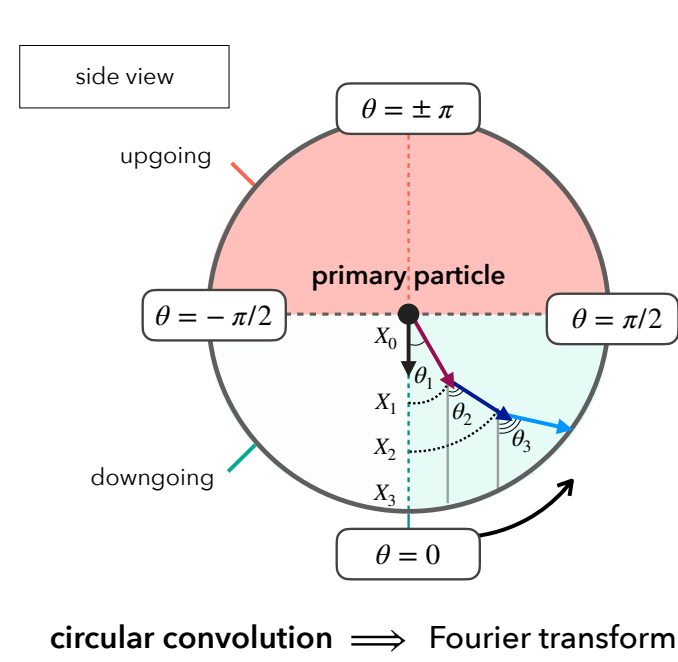


> Find a very good agreement at a range of altitudes and muon energies:



This suggests that our tool can be a fast and accurate alternative to the Monte Carlo cascade development approaches.

Want to know more?

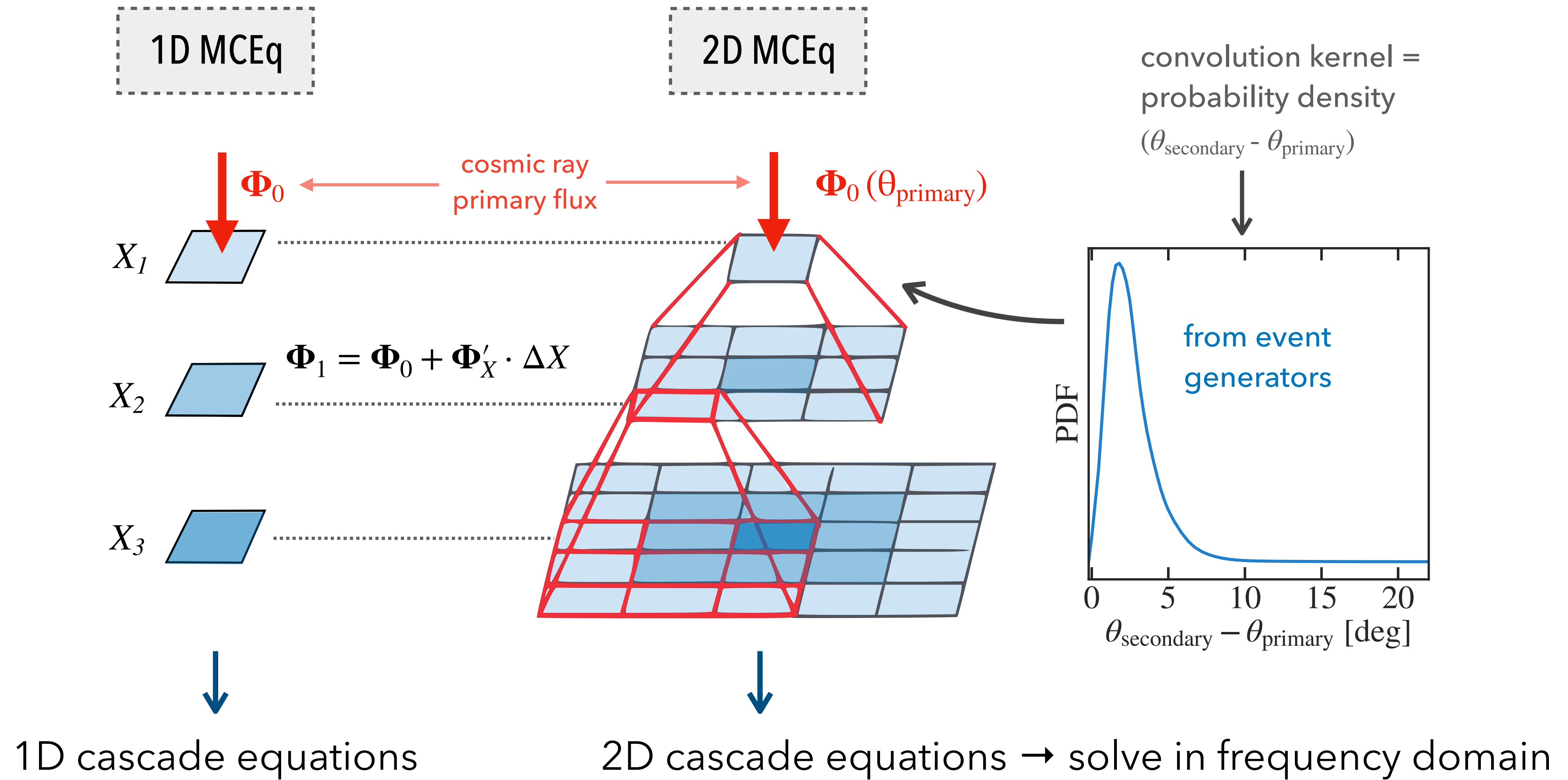


Talk to us at the [presenter's forum](#), email tetiana.kozynets@nbi.ku.dk, or have a look at the [proceedings](#).

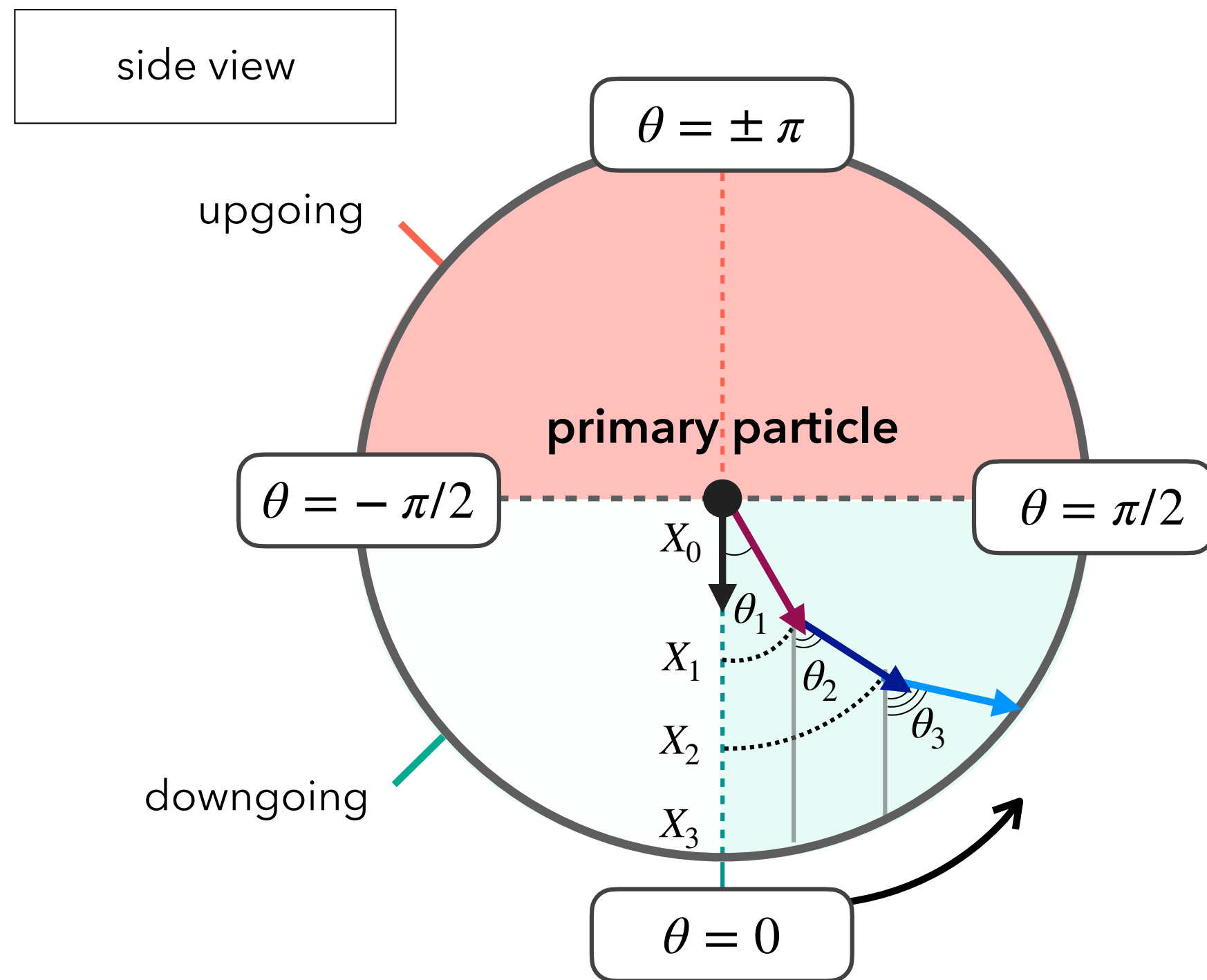
*

Backup

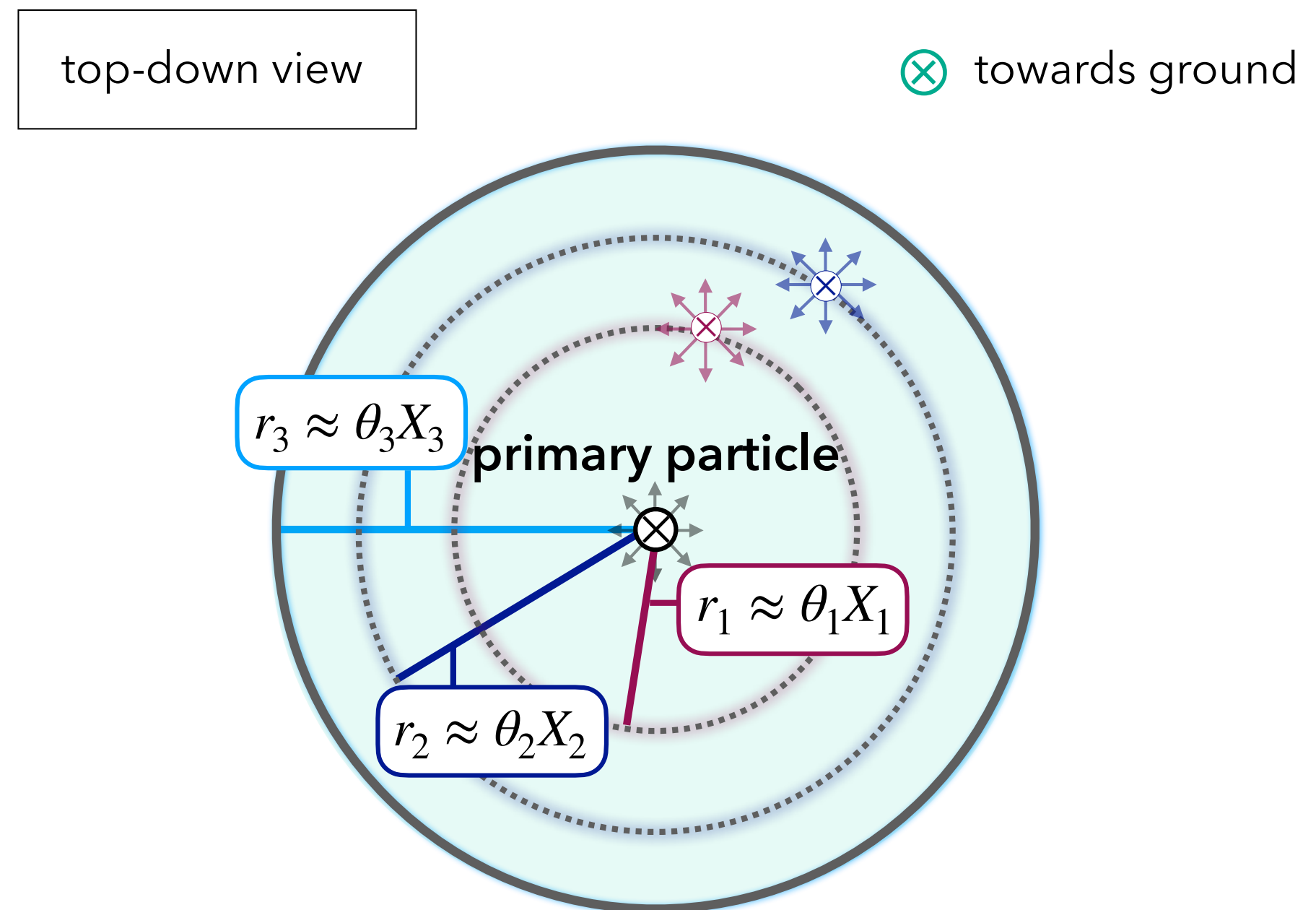
Our approach



Attempted convolution methods

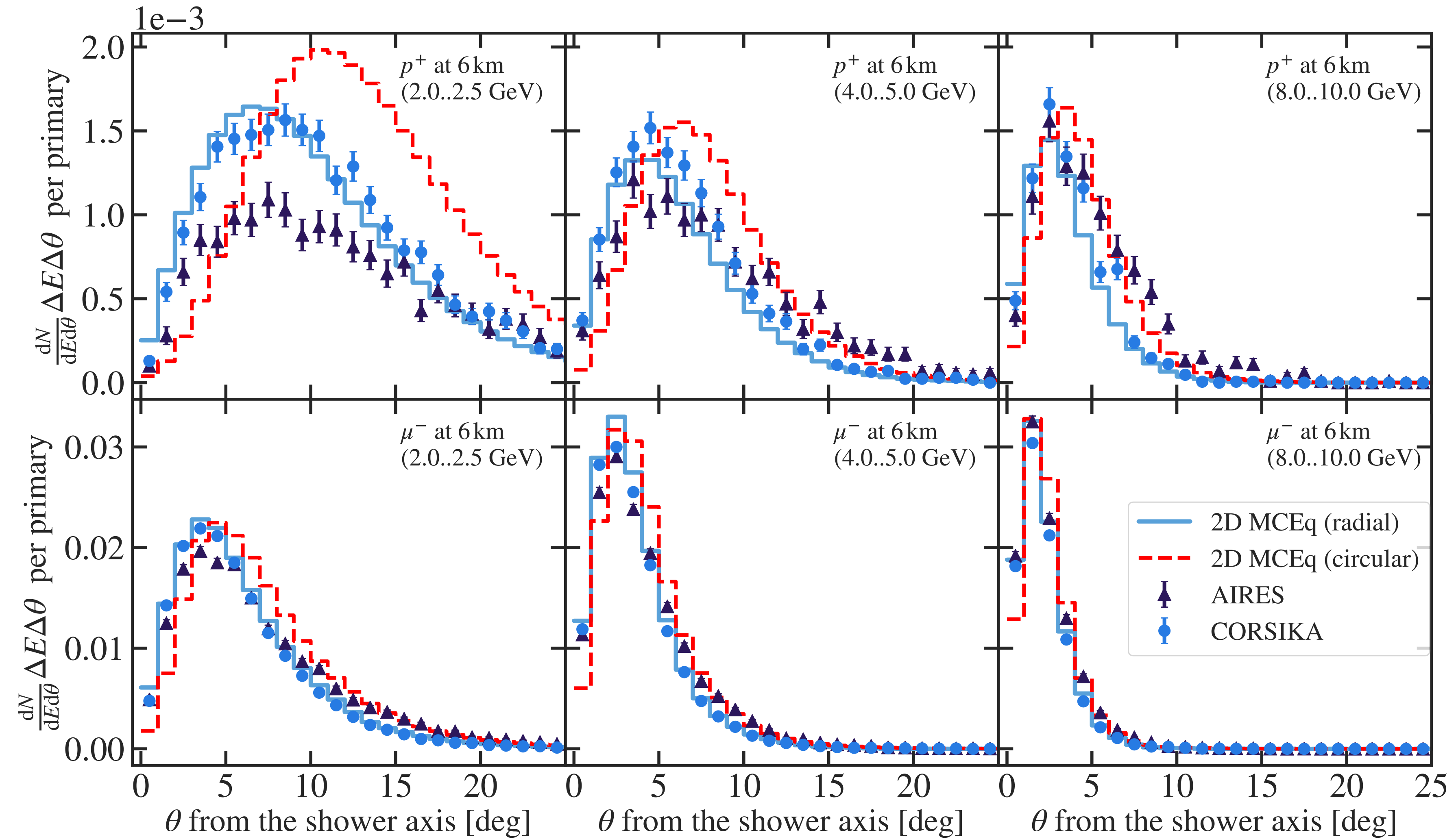


circular convolution \implies Fourier transform



radial convolution \implies Hankel transform

Benchmarking, part II



Angle-integrated spectra

