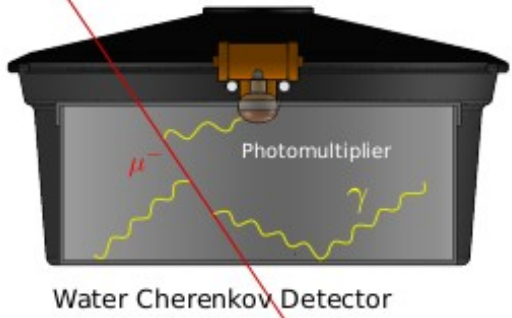
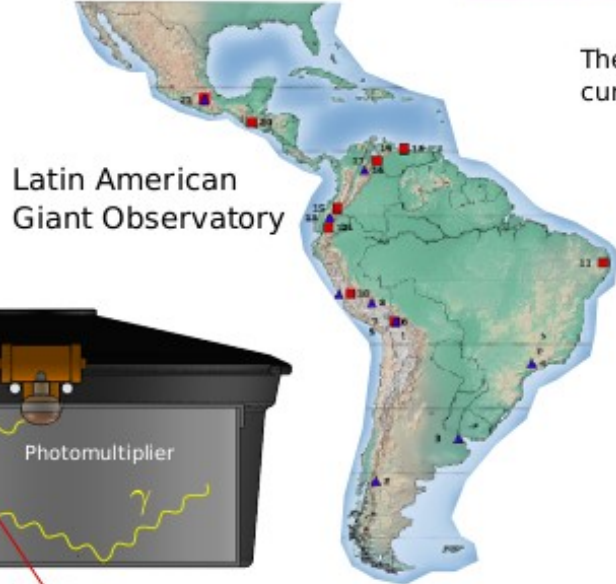
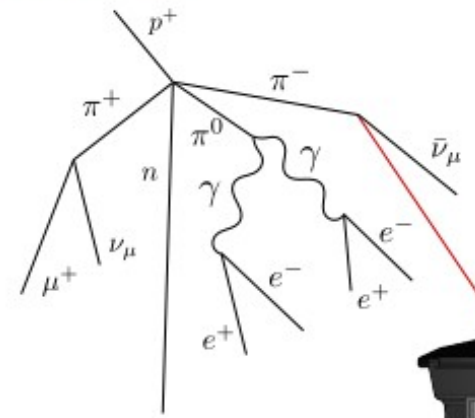


A photomultiplier tube model for the water Cherenkov detectors of LAGO

J. Peña-Rodríguez*, S. Hernández-Barajas, Y. León-Carreño, L. A. Núñez, and L. Otiniano for the LAGO collaboration

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Intro

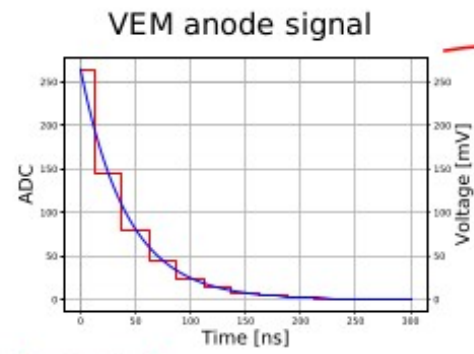


Model

Mathematical Model

PSpice Model

The PMT model takes the number of dynodes (N), the bias voltage (V_B), the photocathode current (I_k), the inter-dynode bias fraction (ϵ_i), and intrinsic parameters (k, α)



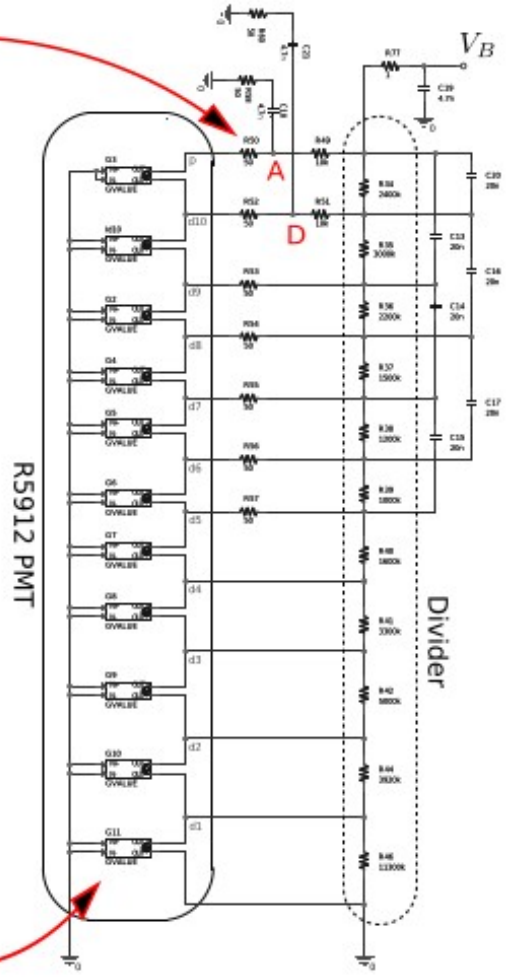
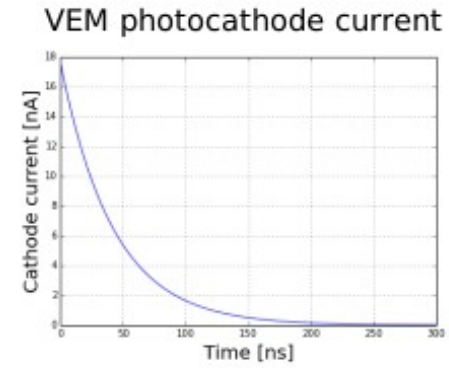
Anode current

$$I_a = I_k k^N (V_B \epsilon)^{N\alpha}$$

i th-Dynode current

$$I_{d,i} = I_k \frac{(kV_B^\alpha)^N \left(\prod_{i=1}^N \epsilon_i\right)^\alpha}{(kV_i^\alpha)^{N+1-i} \left(\prod_{i=1}^{N+1-i} \epsilon_i\right)^\alpha}, \quad i = 1, 2, \dots, N$$

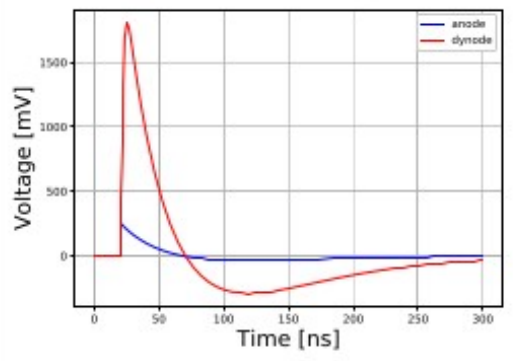
VEM,
Vertical
Muon
Equivalent



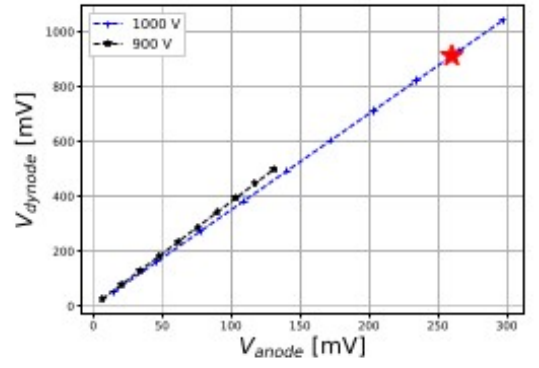
Results

The estimated and measured VEM charge differ by **4%**

Pulse shape

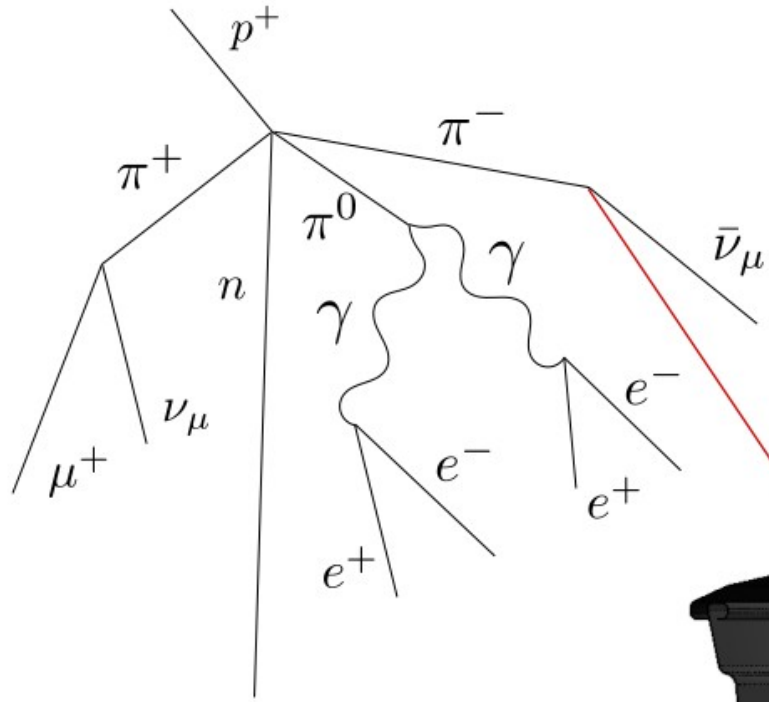


Linearity

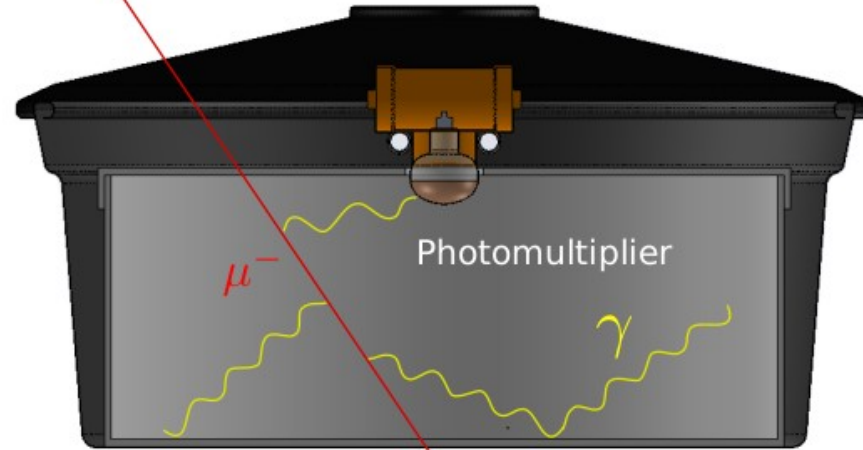


Divider

Intro

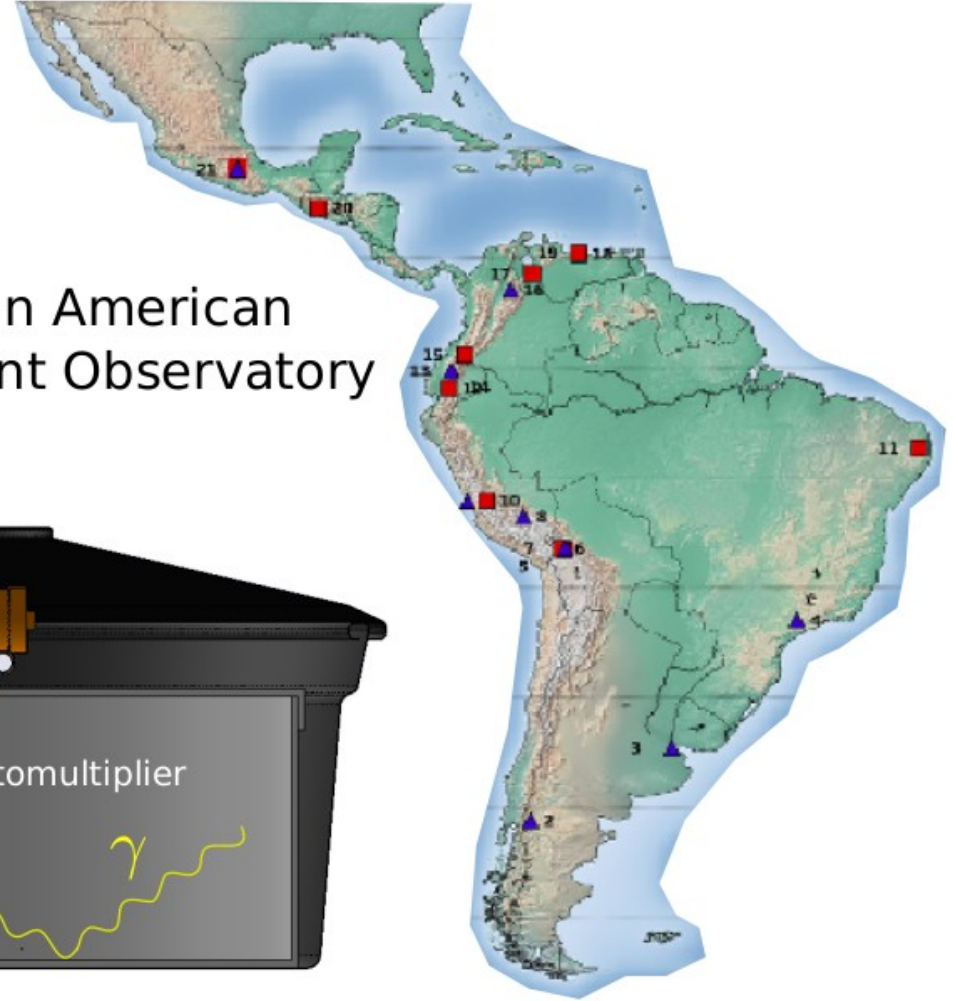


Extensive Air Shower



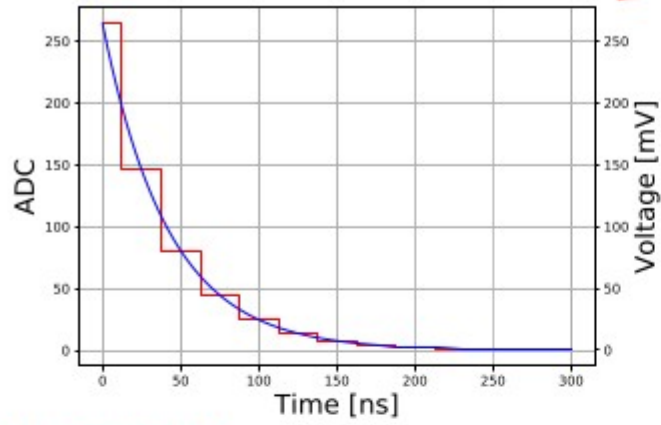
Water Cherenkov Detector

Latin American
Giant Observatory



Model

VEM anode signal



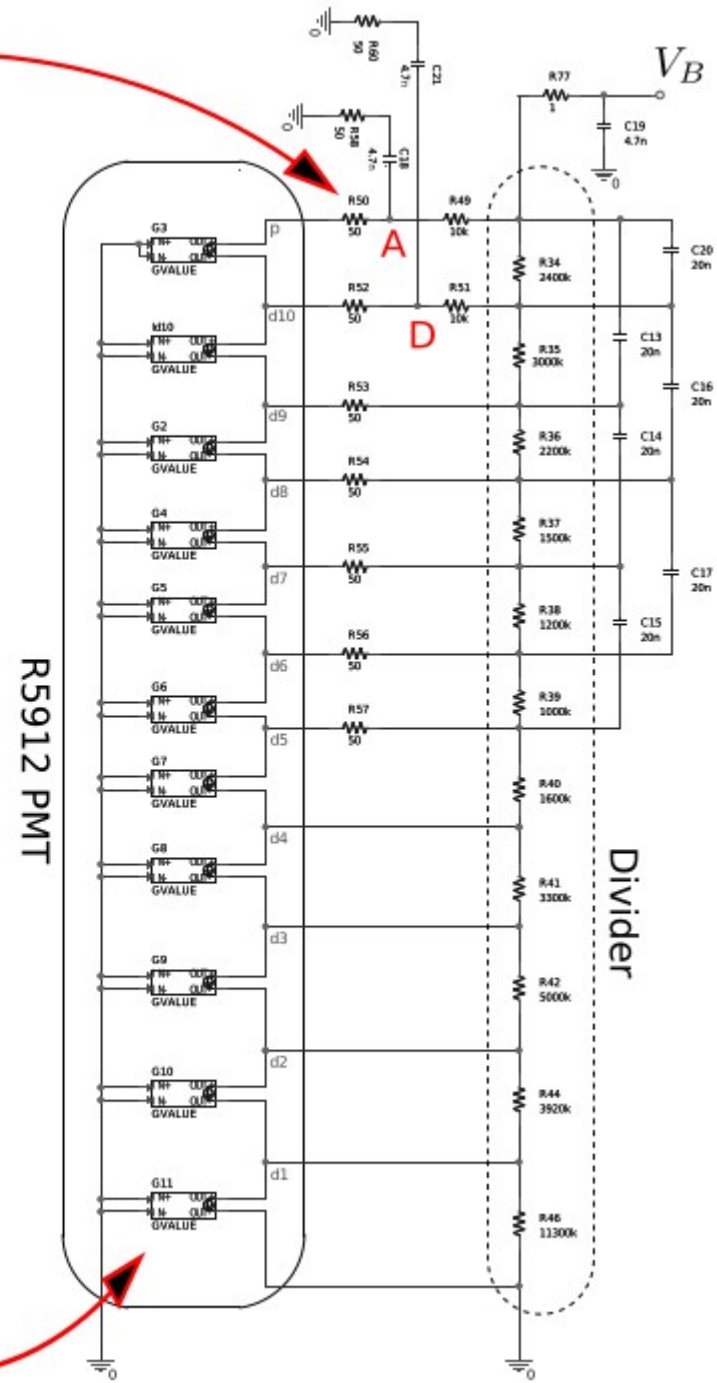
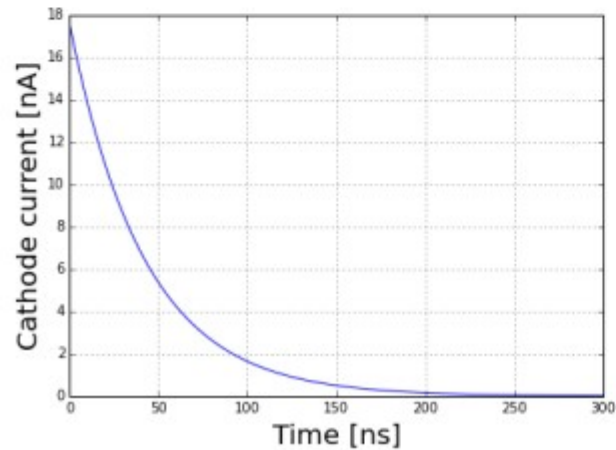
Anode current

$$I_a = I_k k^N (V_B \epsilon)^{N \alpha}$$

*i*th-Dynode current

$$I_{d,i} = I_k \frac{(k V_B^\alpha)^N \left(\prod_{i=1}^N \epsilon_i \right)^\alpha}{(k v_i^\alpha)^{N+1-i} \left(\prod_{i=1}^{N+1-i} \epsilon_i \right)^\alpha}, \quad i = 1, 2, \dots, N$$

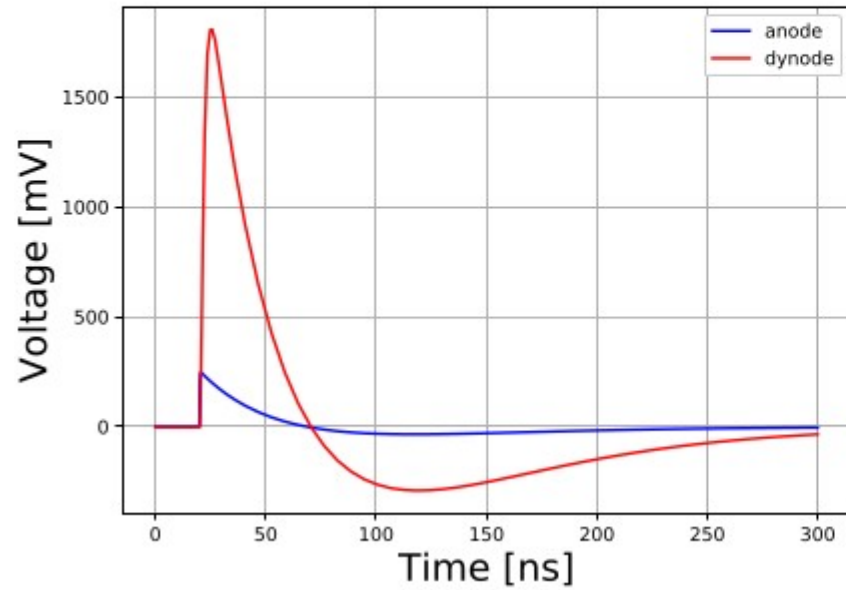
VEM photocathode current



Results

The estimated and measured VEM charge differ by **4%**

Pulse shape



Linearity

