

Hadronic uncertainties of inclusive atmospheric lepton fluxes from fixed-target experiments

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ICRC 2021, 2021/07/16, general forum?



Target audience

1. Atmospheric neutrino community:

- Neutrino astronomy
- Fundamental neutrino properties
- New physics

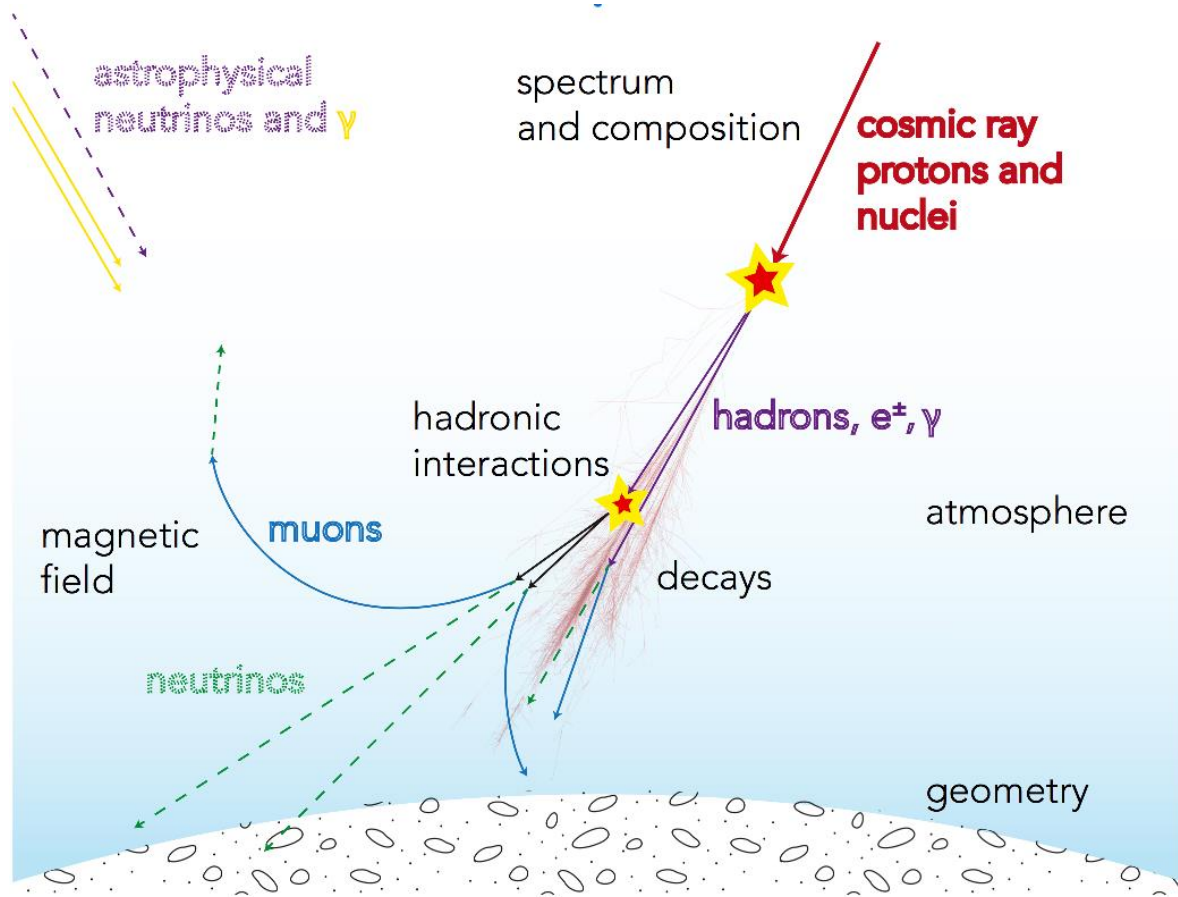
2. Cosmic ray community:

- Direct and indirect cosmic ray flux measurements and modeling
- Cosmic ray composition

3. Hadronic interaction community:

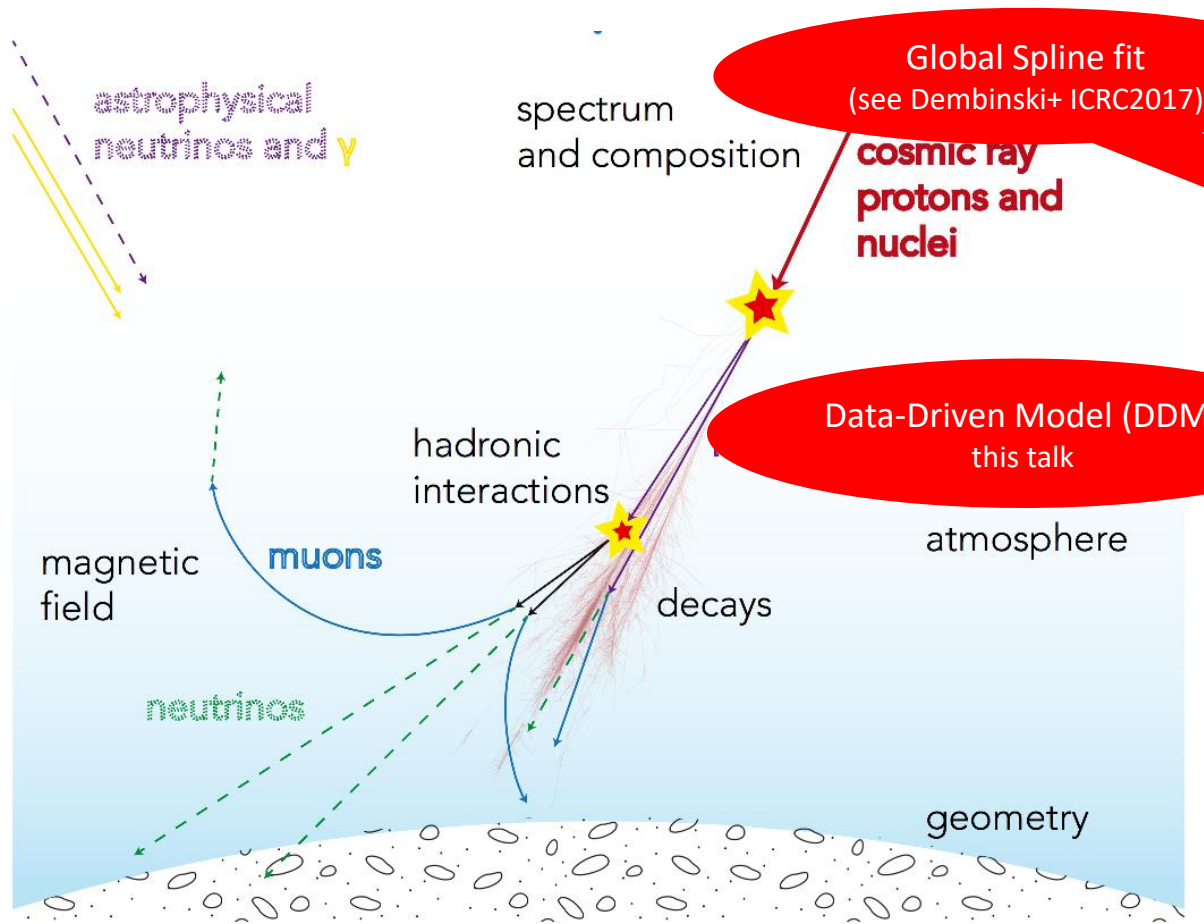
- Fixed target and colliders
- Air showers

High-precision atmospheric lepton calculations



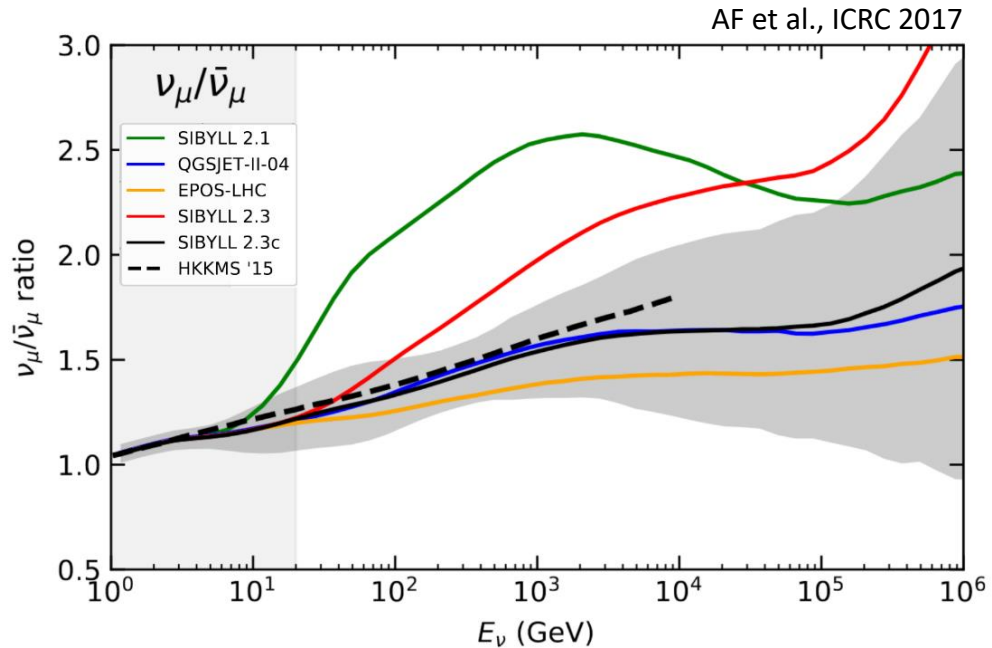
- For high precision calculations all phenomena need accurate modeling
- Uncertain “ingredients”:
 - Cosmic ray spectrum and composition
 - Hadronic interactions
 - Atmosphere (dynamic, depends on use case)
 - (Rare) decays
 - Geometry, magnetic fields, solar modulation
- No clear prescription how to handle uncertainties.
- Methods: Monte Carlo, analytical, numerical
- Energy range MeV – EeV!

High-precision atmospheric lepton calculations



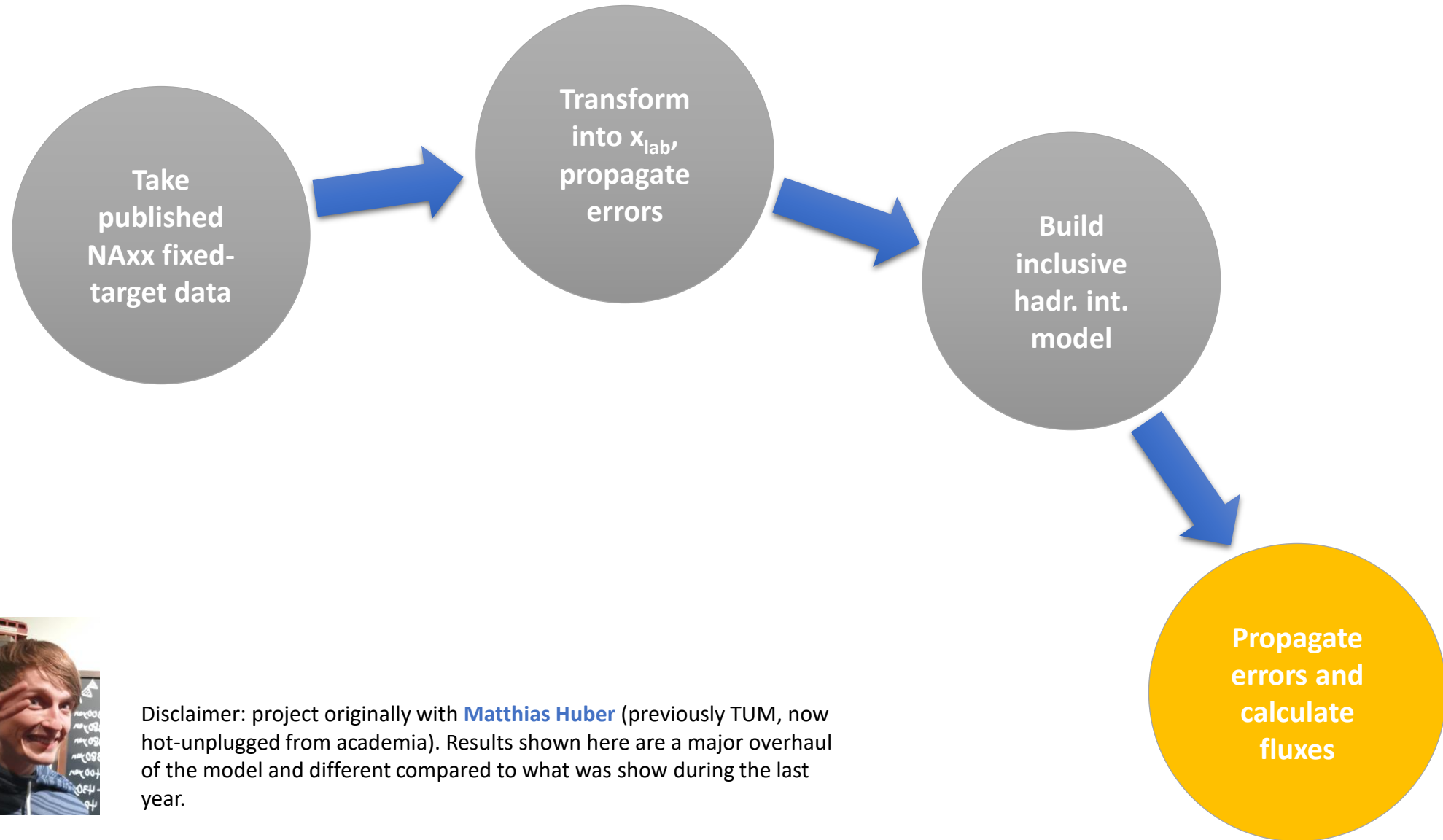
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Current state-of-the-art



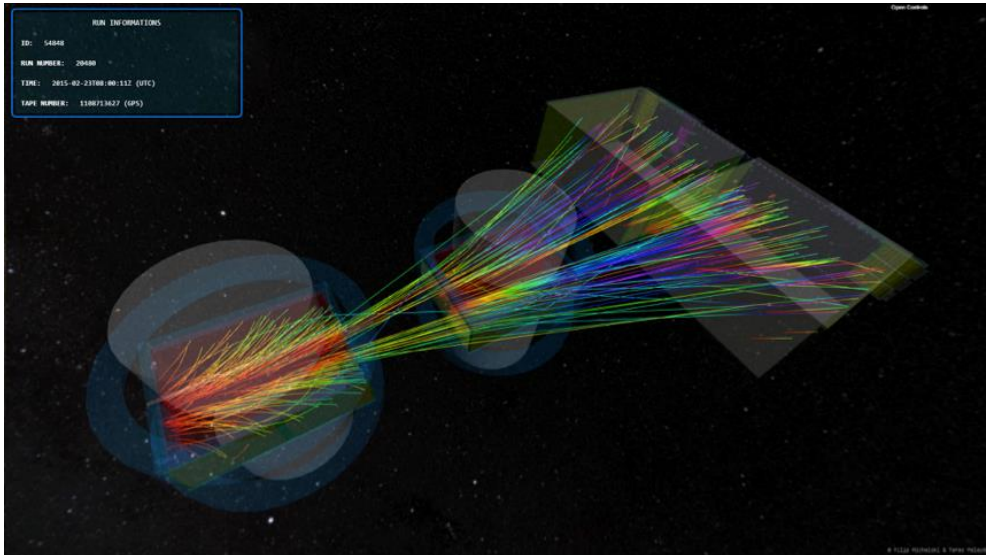
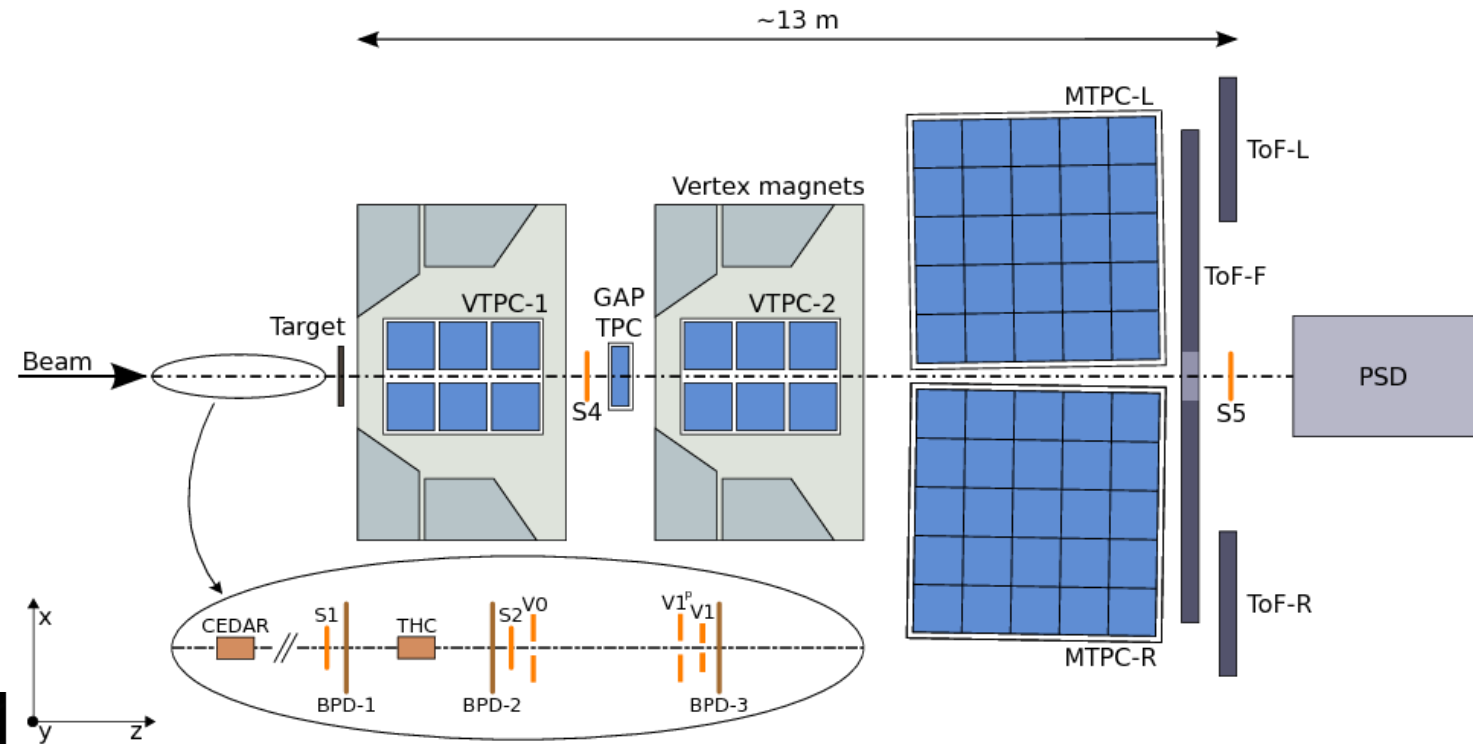
- Hadronic interaction models used in cosmic ray physics SIBYLL, EPOS, QGSJET, DPMJET predictions very different
- **Data-inspired** uncertainties (gray band, Barr et al. 2006 PRD74) are not an envelope of model predictions
- Are these uncertainties over-/underestimated? Are the models wrong?
- How can we make use of high-precision data taken by the CERN North Area NA 49 and 61 experiments beyond inspiration?

DDM: Data-Driven hadronic interaction Model



Disclaimer: project originally with [Matthias Huber](#) (previously TUM, now hot-unplugged from academia). Results shown here are a major overhaul of the model and different compared to what was show during the last year.

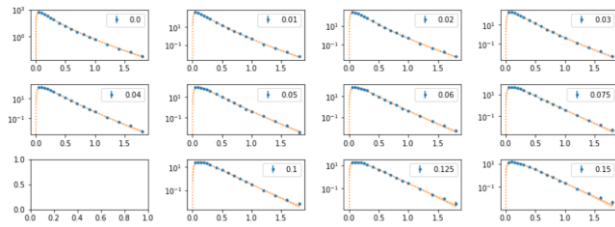
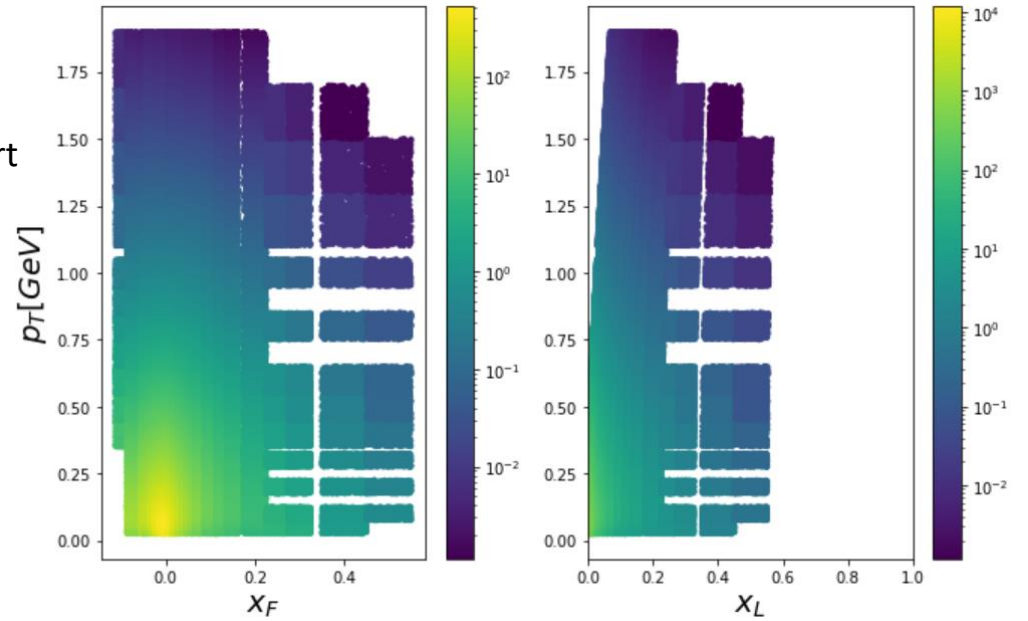
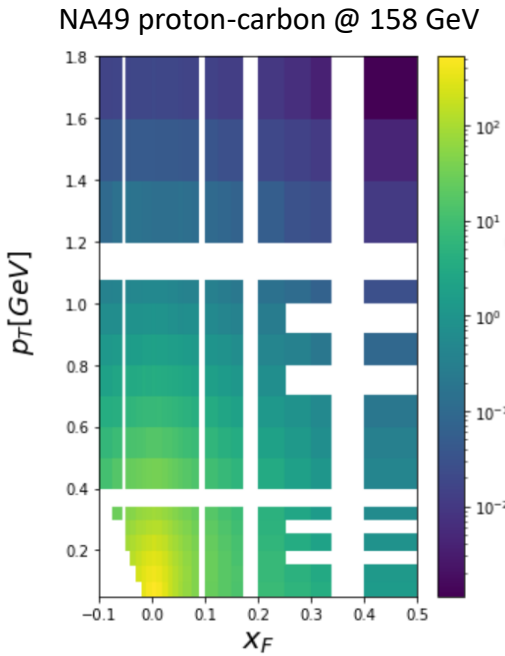
NA61/SHINE



Building the DDM

Sample from $x_F = pz/\sqrt{s}$ and convert into $x_L = E_{\text{secondary}}/E_{\text{proj}}$

$$x_{Lab} = \frac{E_c}{E_a} = \frac{\gamma \sqrt{m_c^2 + \frac{1}{4}x_F^2 E_{c.m.}^2 + p_{c,T}^{*2} + \frac{1}{2}\gamma\beta x_F^2 E_{c.m.}}}{E_a}$$



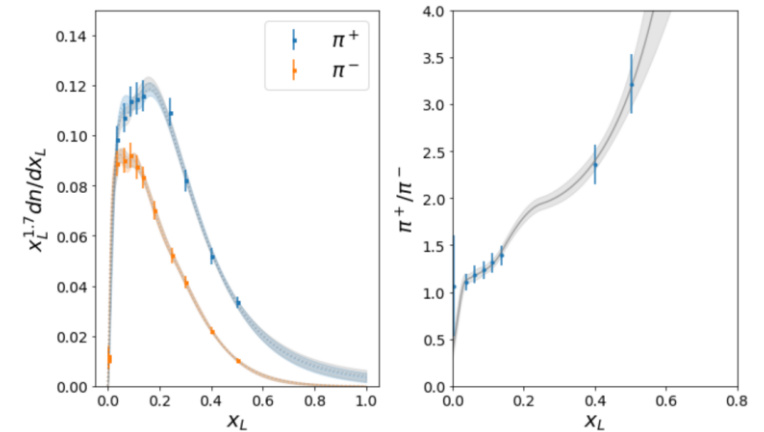
Fit p_T in each x_F bin using $\frac{dn}{dp_{\perp}} = a_0 p_{\perp}^{a_1} e^{a_2 p_{\perp}^{a_3}}$

Fit dn/dx_L with splines, get covariance matrix

Included data

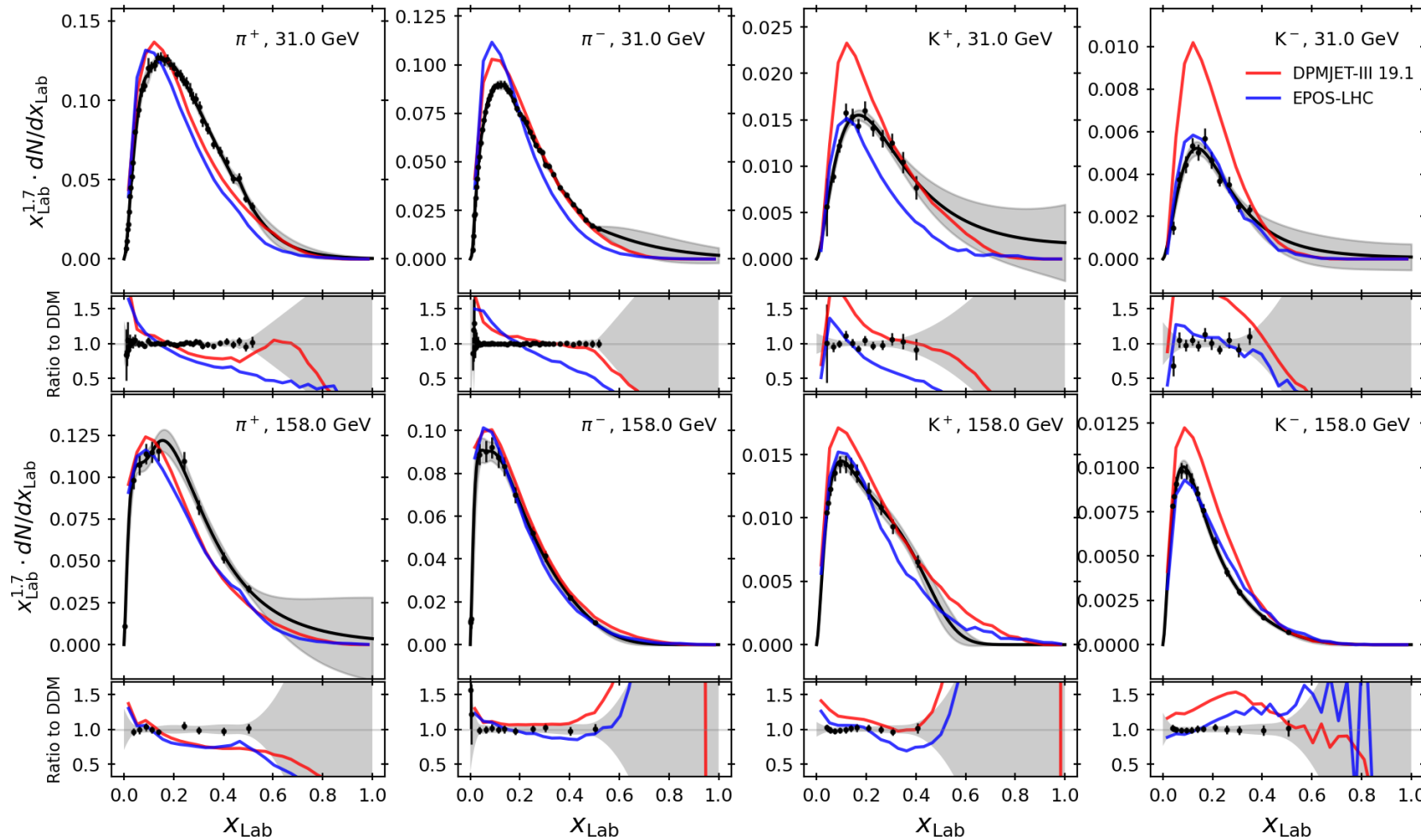
Experiment	beam	$E_{\text{beam}}/\text{GeV}$	Secondaries	Variables
NA49	pC	158	π^{\pm}, \bar{p}, n	x_F, p_{\perp}
NA49	pp	158	K^{\pm}	x_F, p_{\perp}
NA61/SHINE	pC	31	$\pi^{\pm}, K^{\pm}, K_S^0, \Lambda$	p, θ
NA61/SHINE	π^-C	158, 350	$\pi^{\pm}, K^{\pm}, \bar{p}$	p, p_{\perp}

(In the next iteration we would like to include new results from NA61 and old results from NA59 that require Be->C extrapolation.)



Fits of proton-carbon data

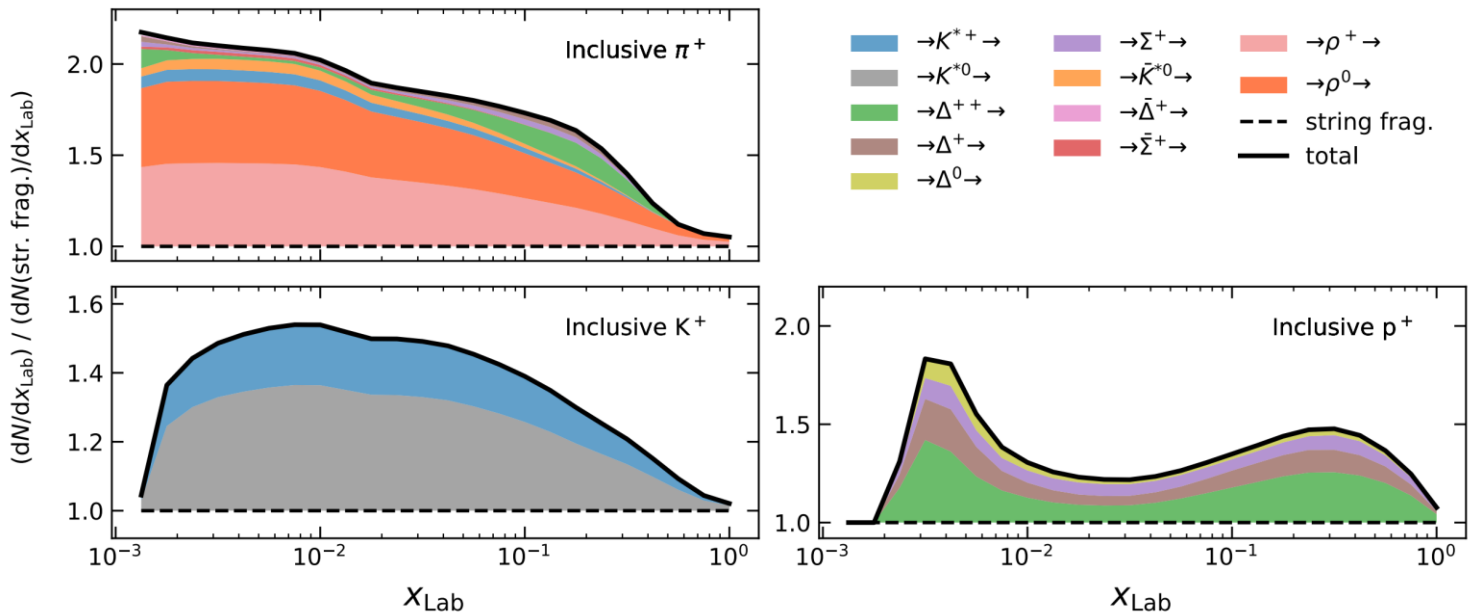
NA49 & NA61 proton-carbon



- Performed in $\log(dN/dx)$ using linear (π^+ & π^- @ 31 GeV) cubic splines (rest) with $s > 0$
- **Uncertainties consistently blow up** in absence of x_L data
- Covariance matrix via hesse, multiplied by 2 to contain most of the data's error bars
- Models weak for π^+ (both energies) and K^- at 158 GeV
- An additional data point at large x would add very significant constraints
- K^+ data fit at 158 GeV corrected from $pp \rightarrow pC$, based on average of 4 hadronic interaction models (work in progress)

Why is it so difficult to just make better models

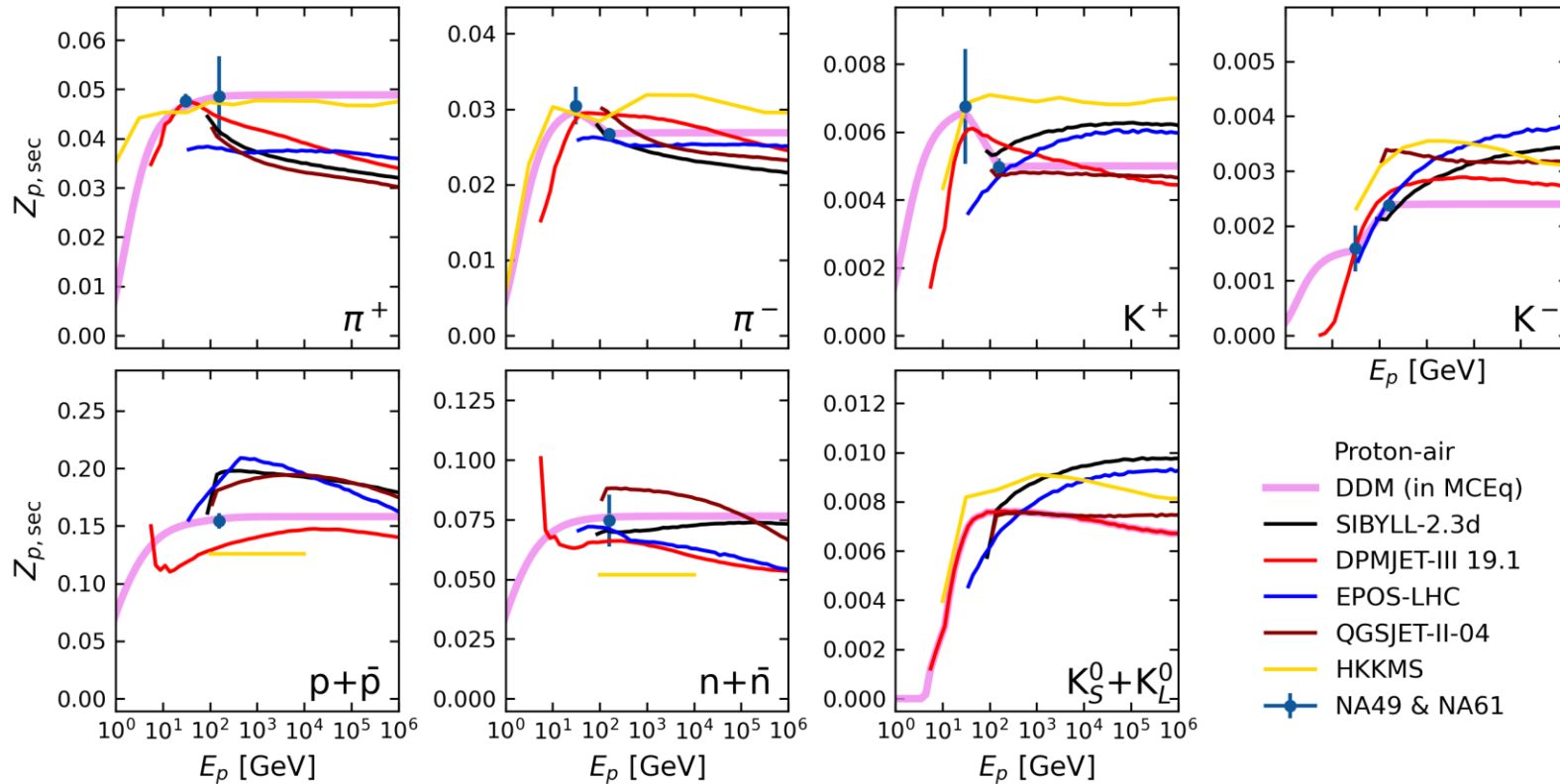
Feed-down from higher-mass states



AF et al. PRD 100 (2019)

- We tried (see [Fedynitch et al. PRD 100 \(2019\)](#) and [Riehn et al. PRD102 \(2020\)](#))
- A major problem is the definition of what “pions” or “kaons” are, since a large fraction originates from feed-down of higher mass states
- For cascades in the atmosphere, the definition coincides with that of NA49/61 that only correct for longer lived strange particles like Λ
- Older data from accelerators may not be useful, since it is not corrected for feed-down (see e.g. epic papers by [S. Wenig](#) and [H.G. Fischer](#) from NA49)
- For most interaction models the inclusive (pion) yields are a superposition of ρ , Δ etc., which are explicitly produced in the model’s fragmentation routines
- There are no “easy to tune” free parameters

Assembling the model + assumptions



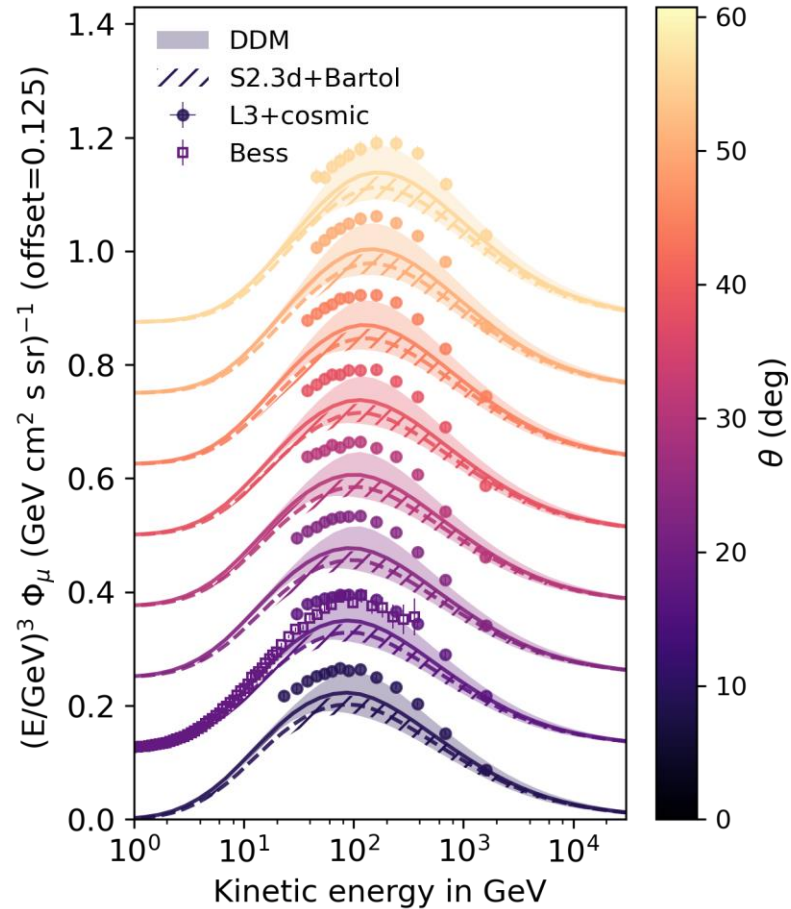
- The spectrum weighted moments (Z-factors) simplify discussion on relevant particle yields
- **Main assumption: Feynman scaling** beyond 158 GeV
- OK assumption for inclusive fluxes due to the x^γ in the integral and suppression of small x values
- DDM interpolates between 31 and 158 GeV data linearly in $\log(E_p)$
- The error on the data (blue dots) originates from the fits (Slide 10)
- This version of DDM **may potentially** underestimate kaons due to threshold effects still present at 158 GeV
- Higher-energy data from NA59 may contain additional hints

$$Z_{N\pi}(E_\pi) = \int_{E_\pi}^{\infty} dE_N \frac{\Phi_{CR}(E_N) \sigma_{N-air}(E_N) dN_{N+air \rightarrow \pi}(E_N, E_\pi)}{\Phi_{CR}(E_\pi) \sigma_{N-air}(E_\pi) dE_\pi}$$

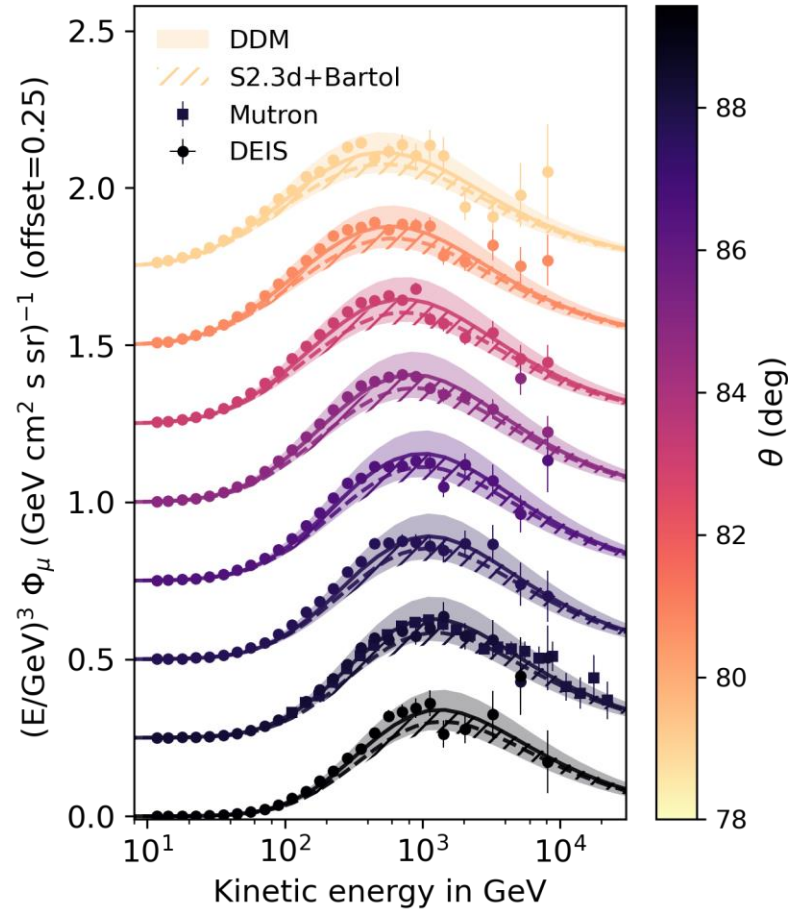
$$Z_{N\pi} = \int_0^1 x_L^{\gamma-1} F_{N\pi}(x_L) dx_L = \int_0^1 x_L^\gamma \frac{dn_\pi}{dx_L} dx_L$$

DDM+ GSF vs data: muon fluxes

Near vertical

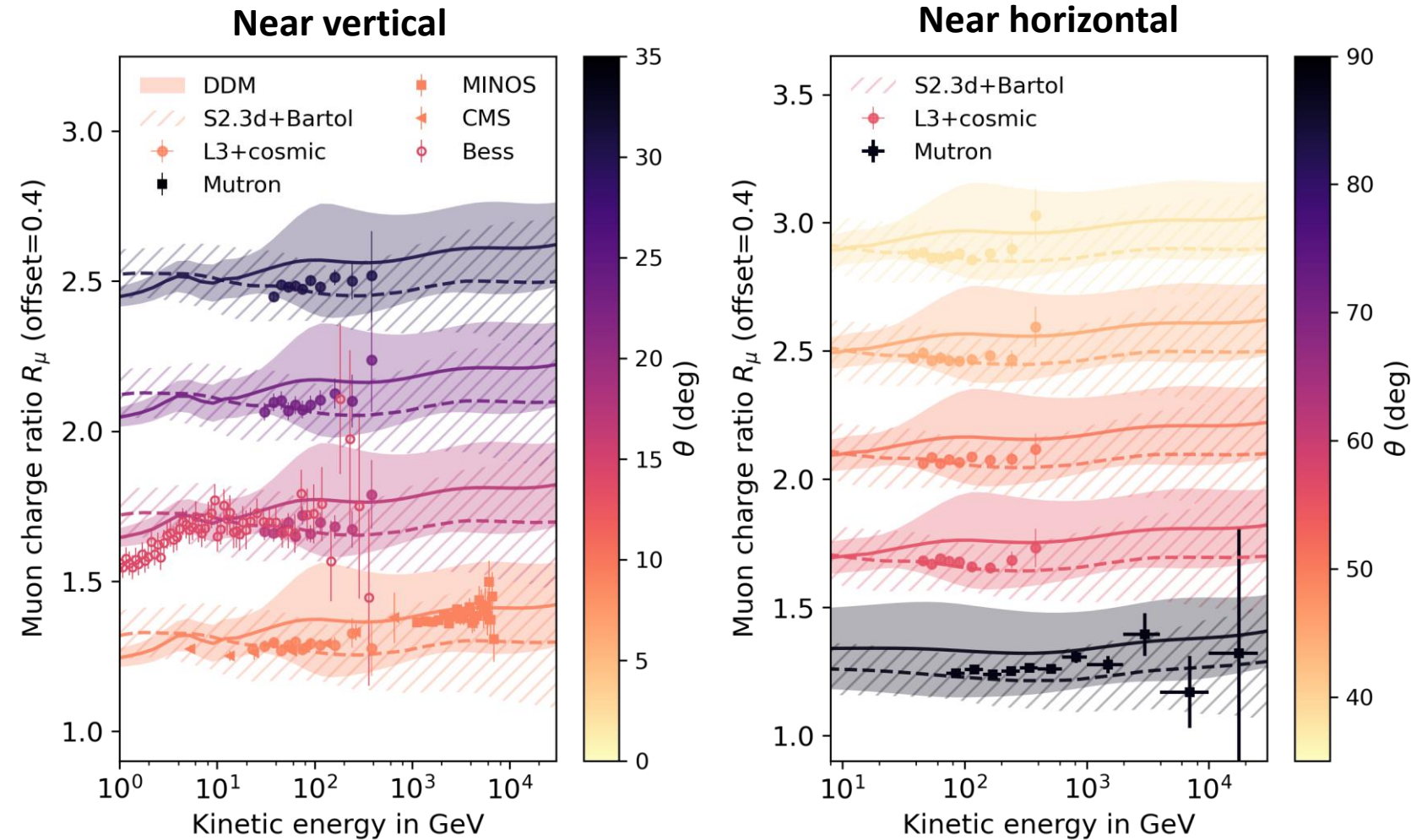


Near horizontal



- Previous estimate from ICRC2017: SIBYLL + Bartol error propagation (hatched)
- Calculation and error propagation with MCEq
- Data without systematics. L3c and Bess allow for some normalization shift. DEIS has large systematics.
- Indication for tension between vertical and near-horizontal data may indicate that
 - Feynman scaling is not a good assumption
 - More likely: The primary flux (GSF) needs to be pulled within its uncertainties (up \sim TeV and softened beyond that). Needs revisiting...
- Data has smaller uncertainties than the model \rightarrow constraints can be obtained from muon data

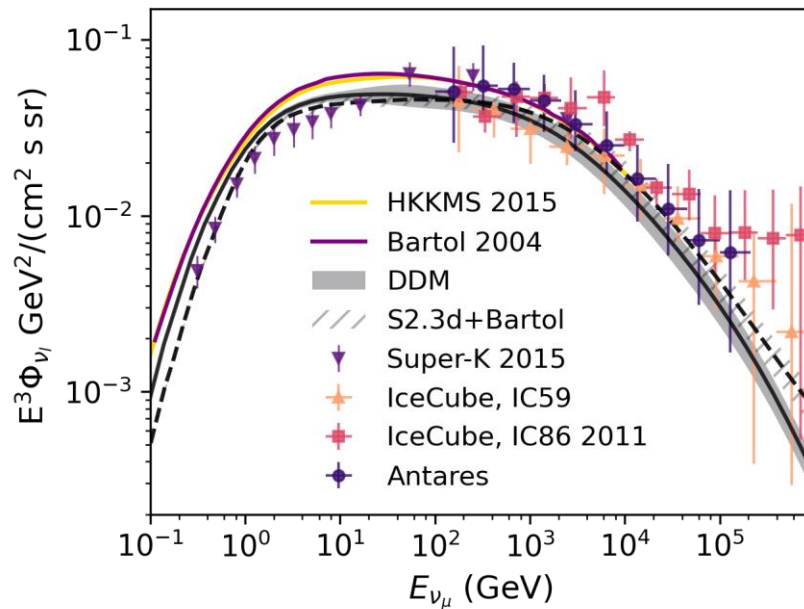
DDM+ GSF vs data: muon charge ratio



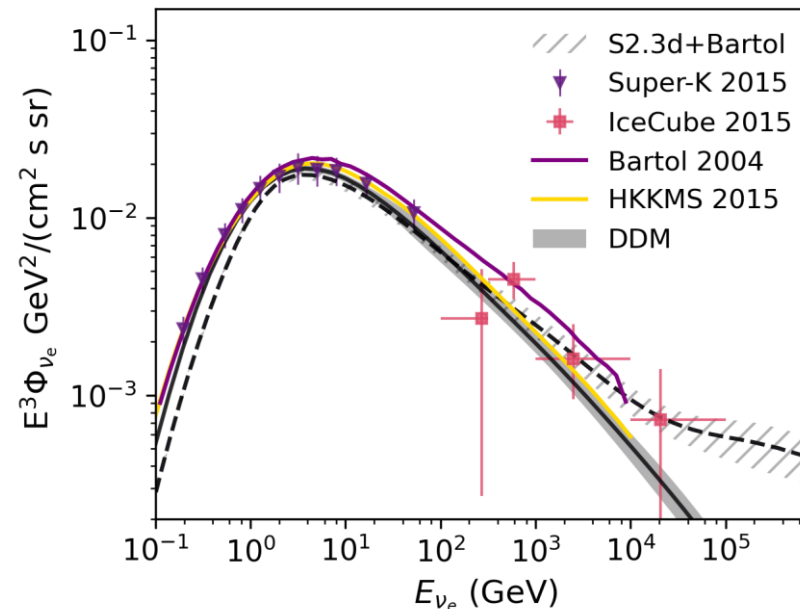
- Data is within uncertainties
- BESS data @ 13 deg ($\text{costh}=0.95$), well described between 5-50 GeV \rightarrow Projectile $E < 300$ GeV
- Same for higher energies @ near-horizontal
- No geomagnetic effects included that may affect lower energy measurements of Bess
- No primary neutron fraction uncertainty included that may affect the charge ratio
- Also, data has smaller uncertainties than the model \rightarrow constraints over a wide energy range on neutrino ratios possible

DDM+ GSF vs data: neutrino fluxes

Muon neutrinos+antineutrinos



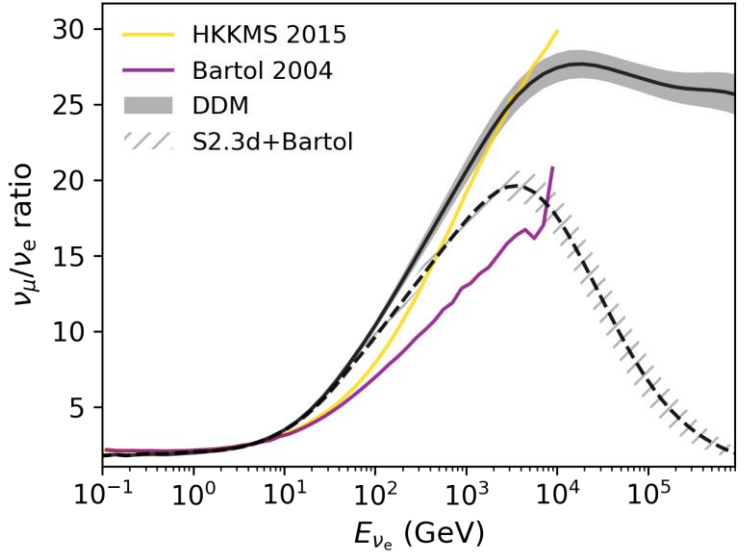
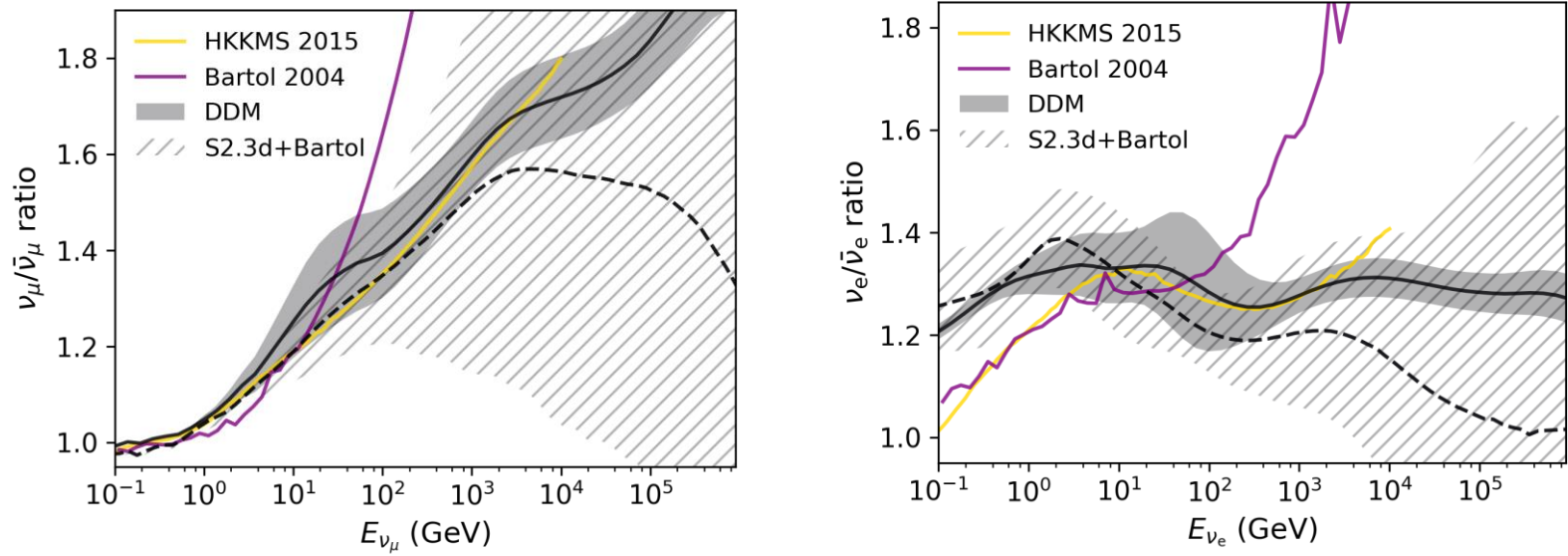
Electron neutrinos+antineutrinos



- Above few GeV DMM is compatible with SIBYLL2.3d+Bartol uncertainties
- At lower energy larger impact from more low-energy muons
- Models not corrected for muon neutrino disappearance (left figure)
- Good compatibility with SK data for electron neutrinos at low energies
- Prompt (hardening at high energy) only SIBYLL, DDM only conventional
- On top is CR flux uncertainty, which will affect $E > 100 \text{ GeV}$

DDM+ GSF vs data: neutrino ratios

Neutrino-antineutrino ratios



Flavor ratio

- Neutrino antineutrino ratio compatible over a wide energy range with HKKMS within error
- At low energy notable improvement compared to Bartol errors due to NA61 31 GeV dataset
- Error on ratios at 100 MeV — GeV may be slightly underestimated due to extrapolation in DDM below 31 GeV
- Flavor ratio above 20 GeV significantly different due to less kaons in DDM wrt HKKMS or Bartol 2004

Summary

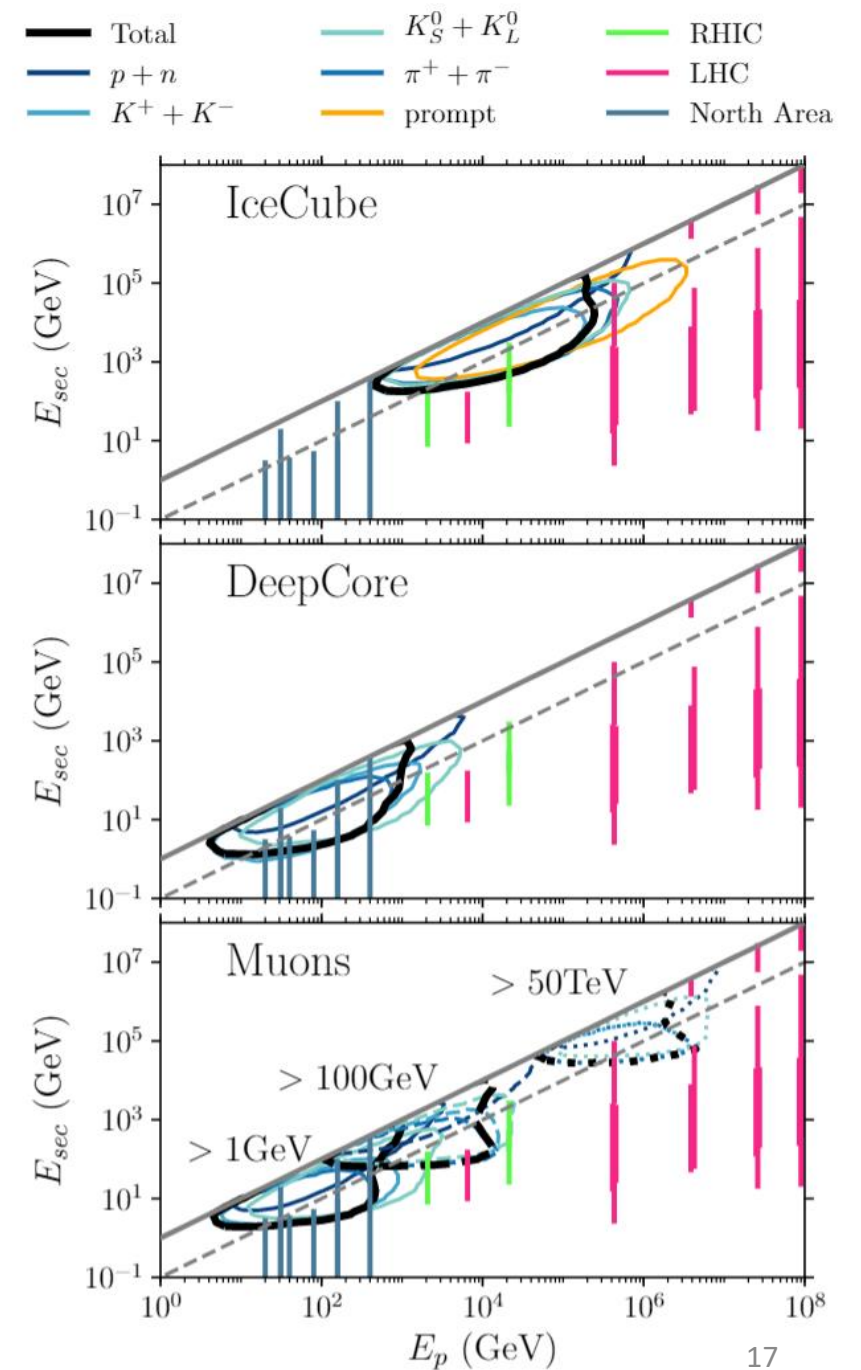
- This new Data-Driven Model (DDM) attacks the largest source of uncertainty in atmospheric neutrino flux calculations. Data from fixed-target accelerators **and** its uncertainties have been successfully parameterized with splines.
- The resulting errors on the lepton fluxes and ratios considerably shrink at low energies and high energies, staying compatible at tens — hundreds GeV with the previous reference (Barr et al.)
- The main sources of the remaining uncertainty are π^+ at somewhat larger x_L and charged kaon measurements on carbon target and at higher energy.
- The impact on atmospheric neutrino oscillation analyses needs requires study, and I offer to help with extracting most from this model.

Outlook

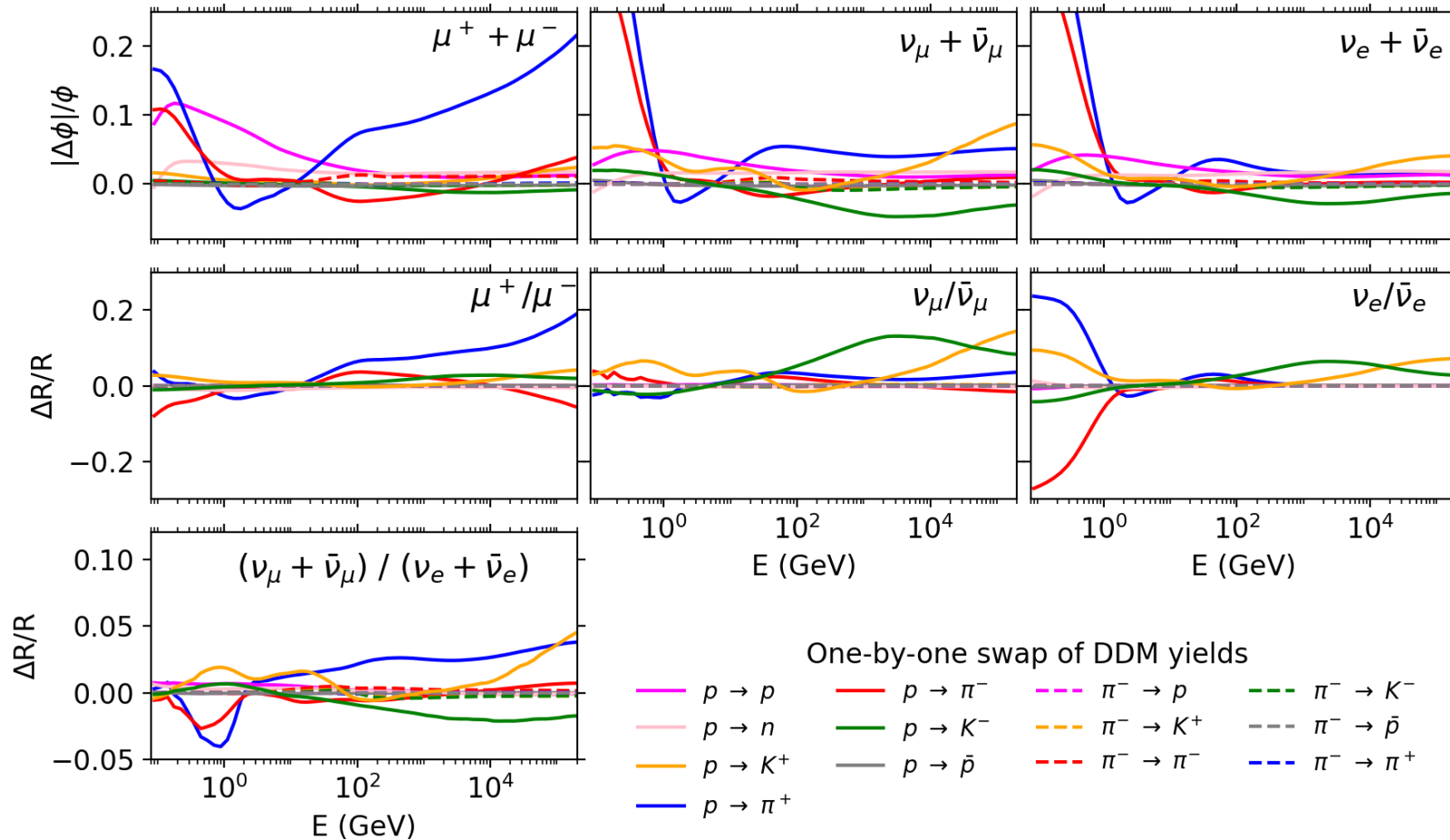
- Upcoming data from NA61 taken at different energies between $\sim 10 - 158$ GeV and (hopefully analyzed in the same way) may constrain the lower energies more significantly \rightarrow expect 3-5% uncertainty. At higher energy, the NA59 data may add crucial constraints after extrapolation from $\text{Be} \rightarrow \text{C}$.
- The model can be calibrated using inclusive muon measurements from surface spectrometers, see this talk by [J.P. Yanez](#)
- At higher energies, deep underground muon intensity data will provide further constraints using the methods presented in [W. Woodley's talk](#)
- The characterization of primary cosmic ray flux uncertainties will be crucial to obtain the best model.

Atm. leptons \leftrightarrow accelerators

- Contours show phase-space probed by atmospheric muon and neutrino experiments
- The lines show **taken** data (not necessarily analyzed) assuming pion secondaries
- Interactions within contours responsible for 90% of the event rate
- Atmv in IceCube probes hadronic interactions at $E < E_{\text{LHC}}$.
- DeepCore probes same phase-space as Super-/Hyper-K
- Muons: vertical, surface, flux integrated above threshold



Impact of individual DDM channels



- Exchanging only one channel of a DPMJET prediction
- Largest impact from π^+ and K^- as expected from sub-panels on Sl. 10
- Only small differences for most other channels: DPMJET (also, SIBYLL and QGSJET) similar to DDM
- Large impact on low energy muons \rightarrow hence also neutrinos from muon decay
- Baryon distributions can shift production depth that matters for unstable particles such as muons