



PAVOL JOZEF ŠAFÁRIK UNIVERSITY IN KOŠICE

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Statistical error for cosmic rays modulation evaluation by 1-D model

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Parker's equation (SDE set)

1 – D case:

$$\frac{\partial f}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left(r^2 K_{diff} \frac{\partial}{\partial r} f \right) - \frac{1}{r^2} \frac{\partial r^2 V_{sw} f}{\partial r} + \frac{1}{3} \left(\frac{1}{r^2} \frac{\partial r^2 V_{sw}}{\partial r} \right) \frac{1}{p^2} \frac{\partial}{\partial p} (p^3 f)$$

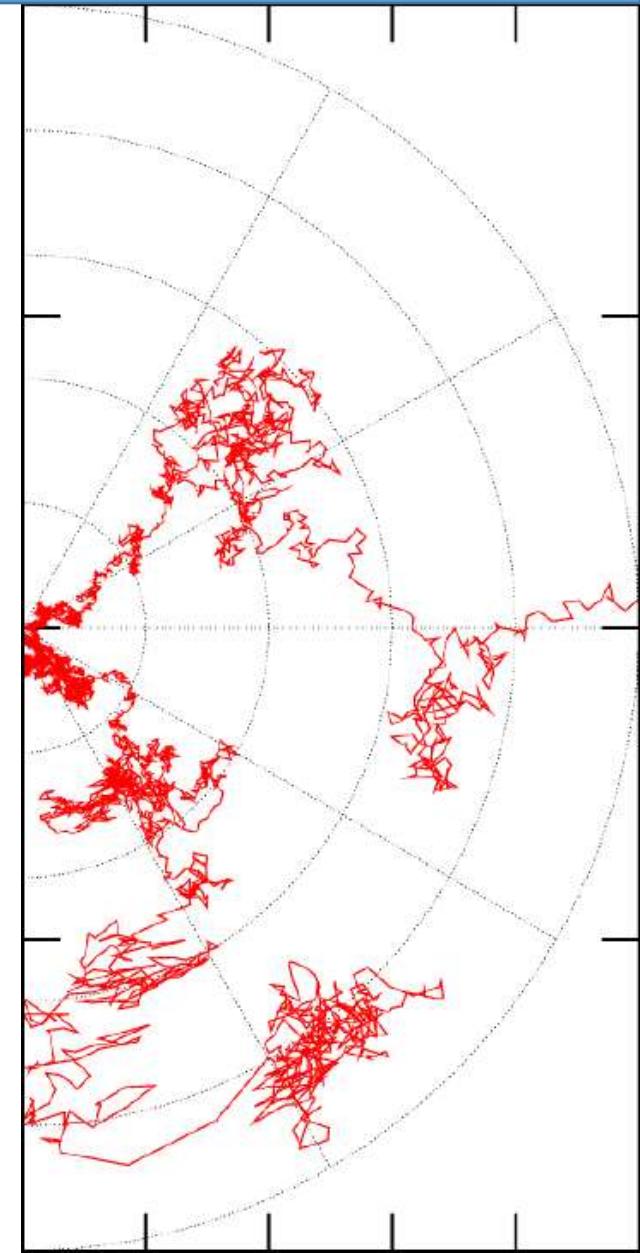
$$K_{diff} = K_0 \beta P.$$

Set of forward - in - time SDE F-p:

$$dr = \left(\frac{2K_{diff}}{r} + V_{sw} \right) dt + \sqrt{2K_{diff}} dW$$

$$dp = -\frac{2V_{sw}p}{3r} dt$$

$$L = -\frac{4V_{sw}}{3r}$$



Statistical error evaluation

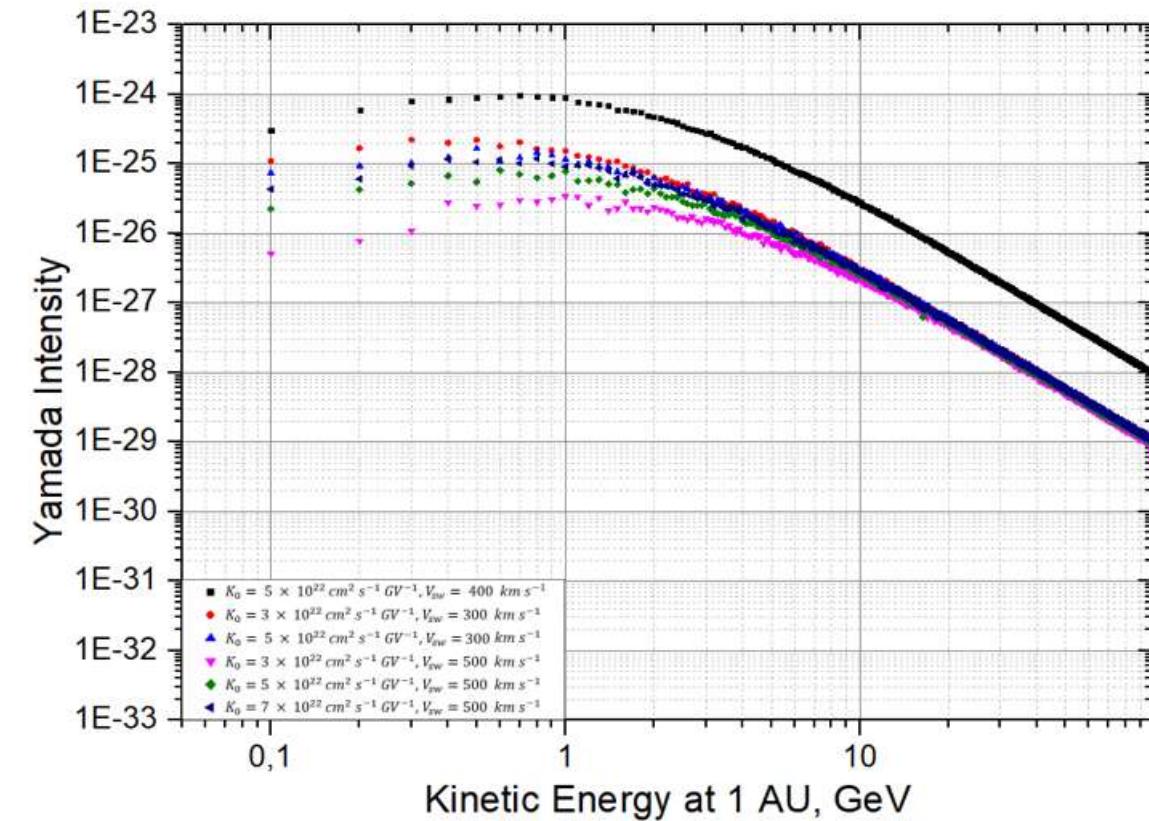


Fig. 1. Spectra at 1 AU evaluated for different sets of input parameters.

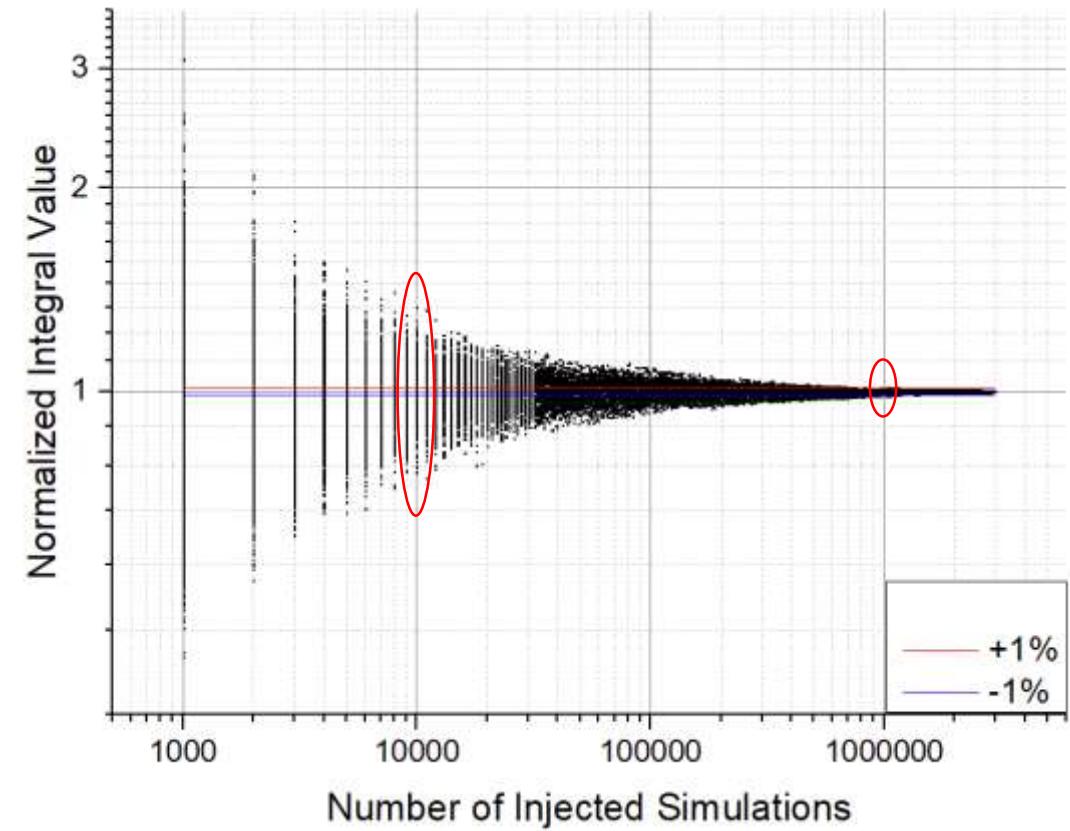


Fig. 2. Normalized integral of whole spectrum[0 – 100GeV] value distribution with respect to number of injected simulations. For the chosen set of input parameters ($K_0 = 5 \times 10^{22} \text{ cm}^2 \text{ s}^{-1} \text{ GV}^{-1}, V_{sw} = 400 \text{ km s}^{-1}$).

Statistical error evaluation

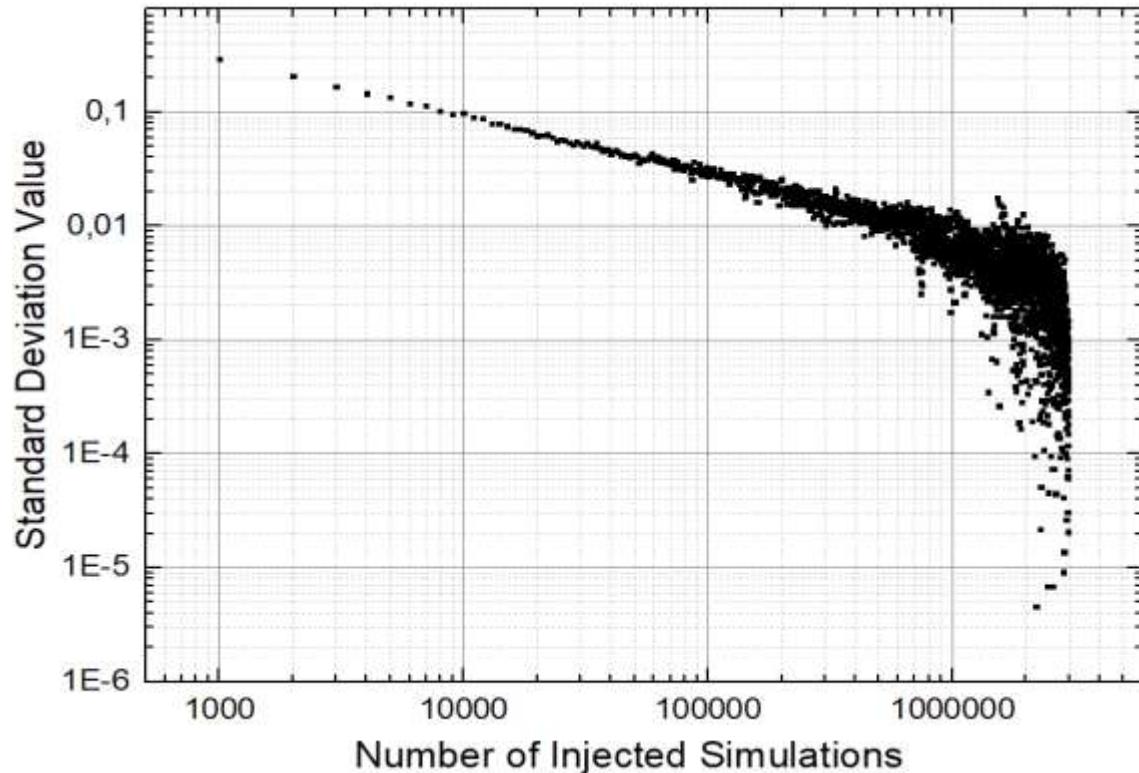


Fig. 3. Standard deviation evaluated from normalized integrals ($K_0 = 5 \times 10^{22} \text{ cm}^2 \text{ s}^{-1} \text{ GV}^{-1}$, $V_{sw} = 400 \text{ km s}^{-1}$).

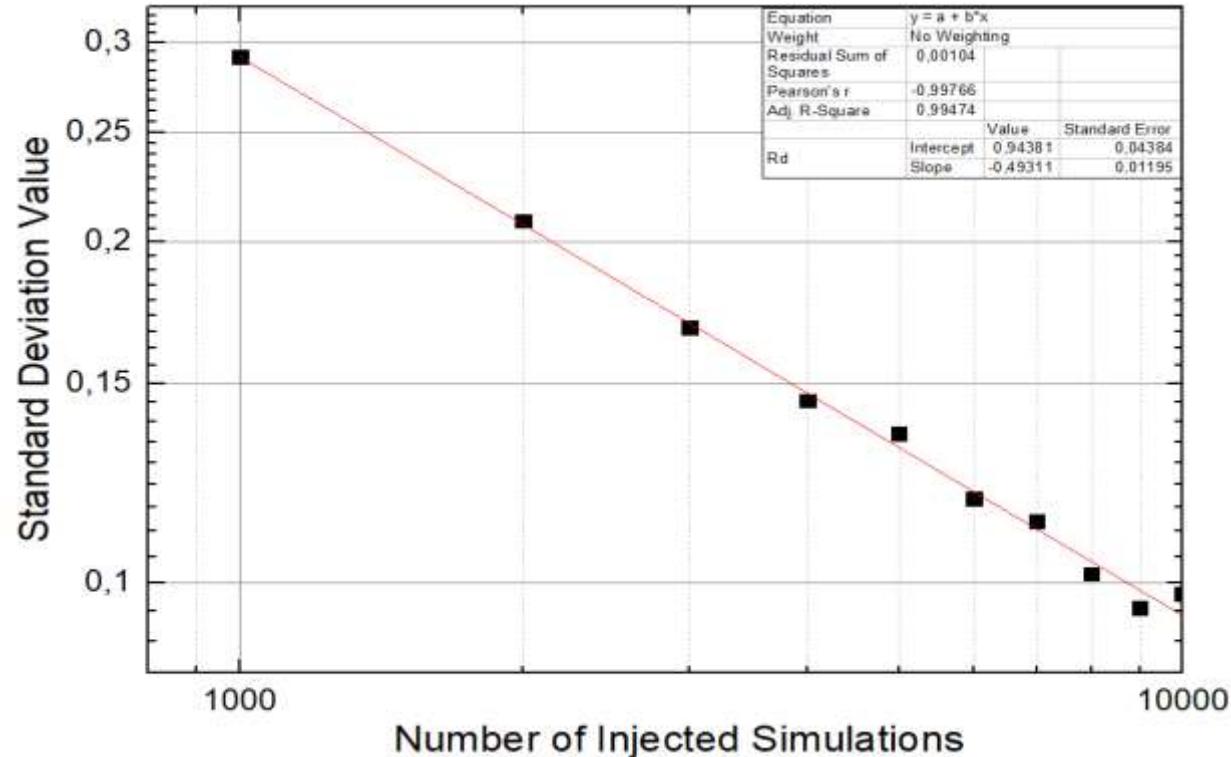


Fig. 4. Linear fit evaluated from standard deviation distribution in range from 1000 to 10000 simulations ($K_0 = 5 \times 10^{22} \text{ cm}^2 \text{ s}^{-1} \text{ GV}^{-1}$, $V_{sw} = 400 \text{ km s}^{-1}$).