

# *New methods to reconstruct $X_{\max}$ and the energy of gamma-ray air showers with high accuracy in large wide-field observatories*

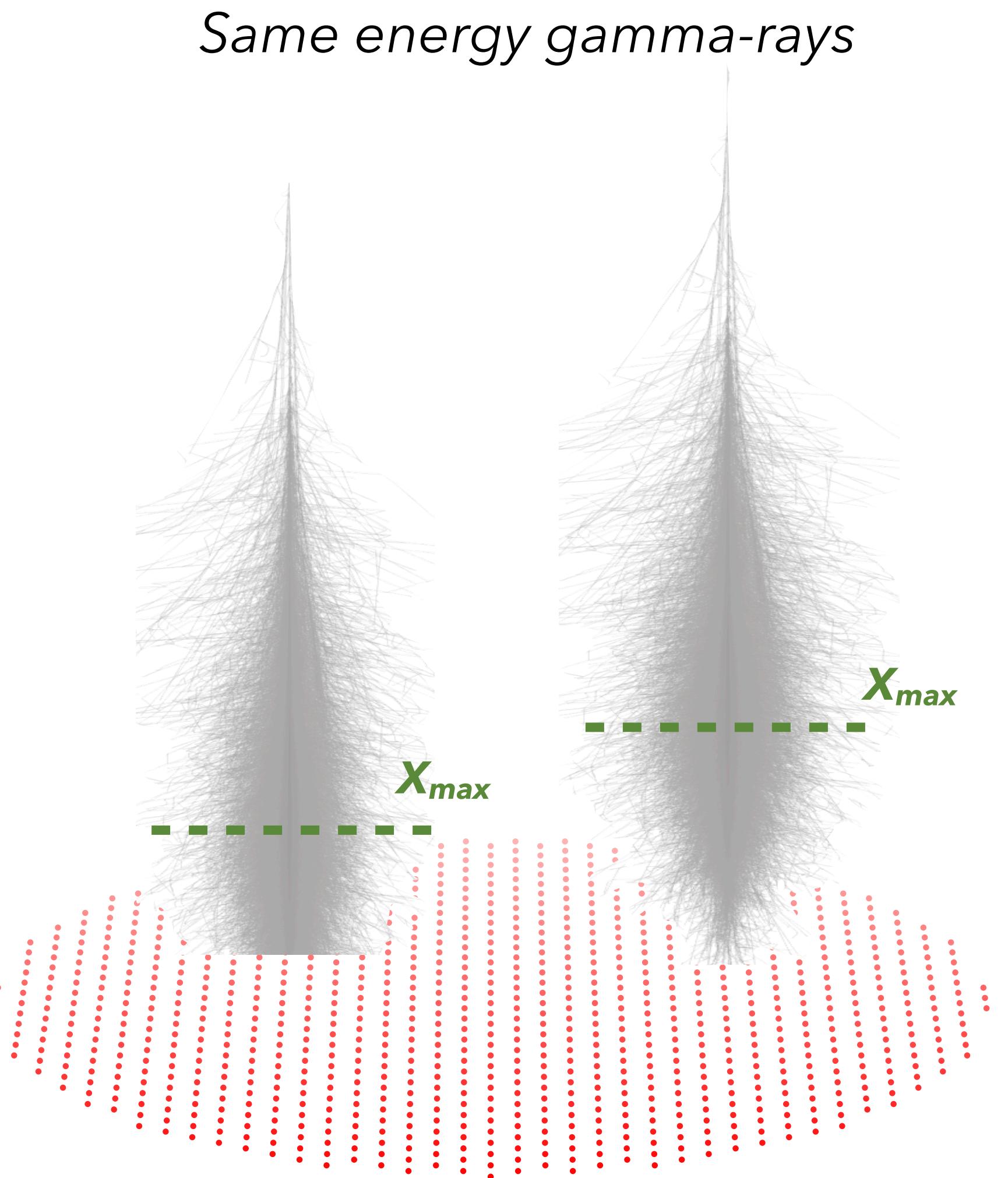
*Eur. Phys. J. C (2021) 81:80 - arXiv: 2010.11390 [hep-ph]*

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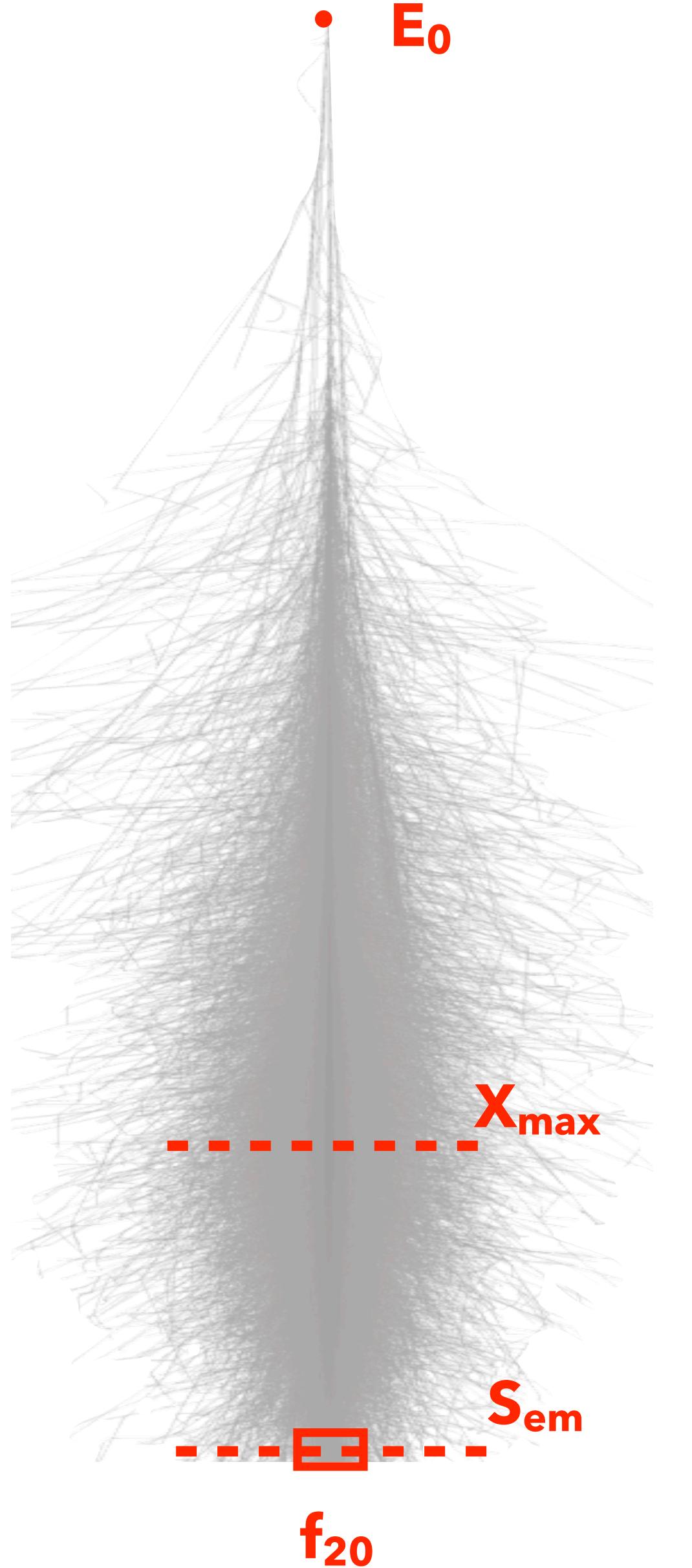
# The problem

- ❖ In ground-arrays the energy of gamma-rays is estimated by sampling the particles at the ground
- ❖ The **primary energy is proportional to the recorded signal at the ground**
- ❖ The **shower fluctuation induces large uncertainties** on the energy determination even using MC template-based likelihood fits
- ❖ At  $E = 10 \text{ TeV}$  results found in the literature quote uncertainties of around 50%



# A new strategy

- ❖ Determine the shower stage and achieve a better determination of the primary energy through:
  1. The **energy at the ground ( $S_{\text{em}}$ )** from the measured signal in the array
  2. The **shower stage ( $X_{\text{max}}$ )** from the  $S_{\text{em}}$  or the shower front curvature
  3. The **primary energy ( $E_0$ )** from the  $S_{\text{em}}$ ,  $X_{\text{max}}$  and the energy fraction in the core region
    - **$f_{20}$**  - energy fraction within 20 m from the shower core  
$$f_{20} = F_{20} / S_{\text{em}}$$

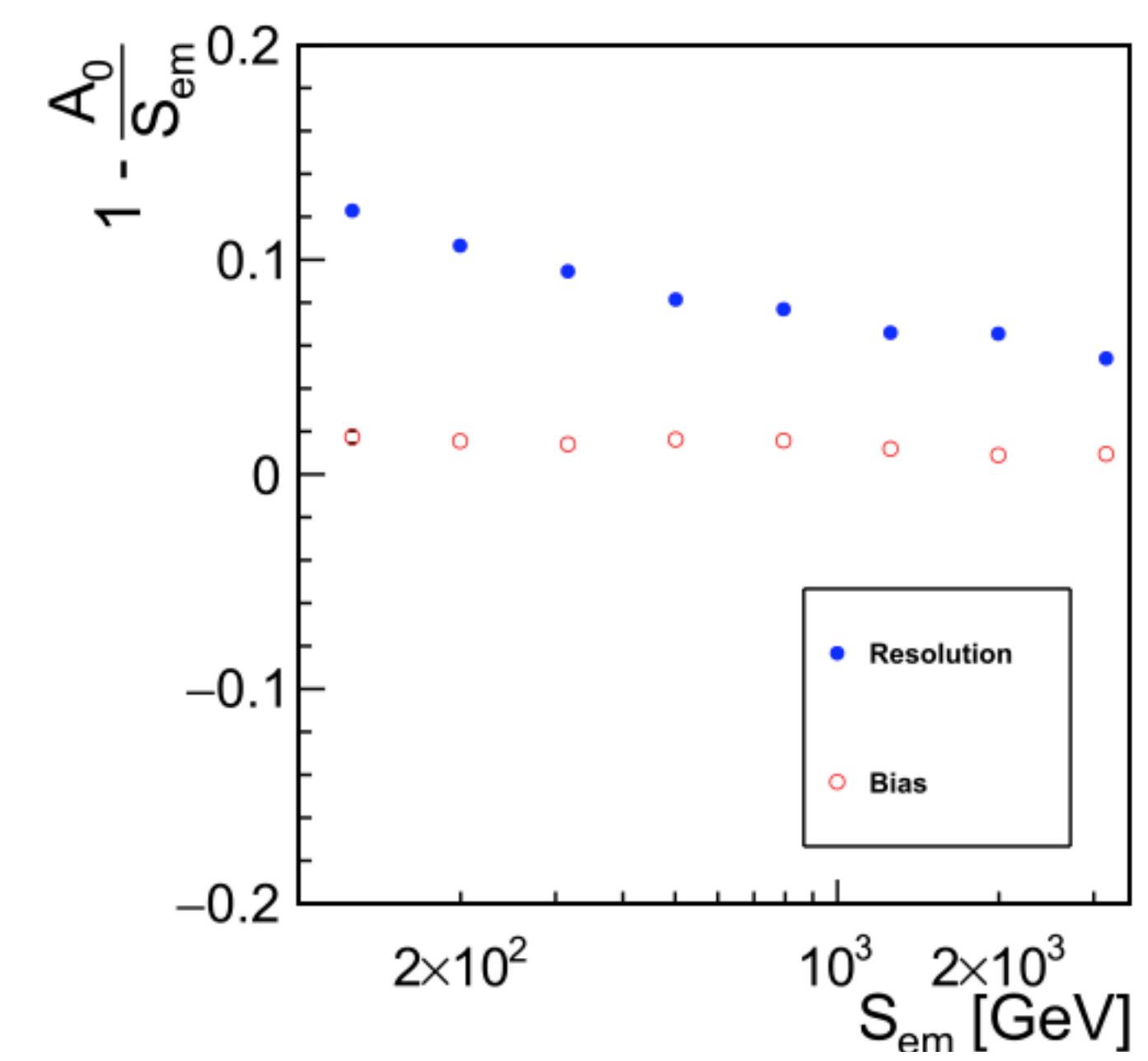
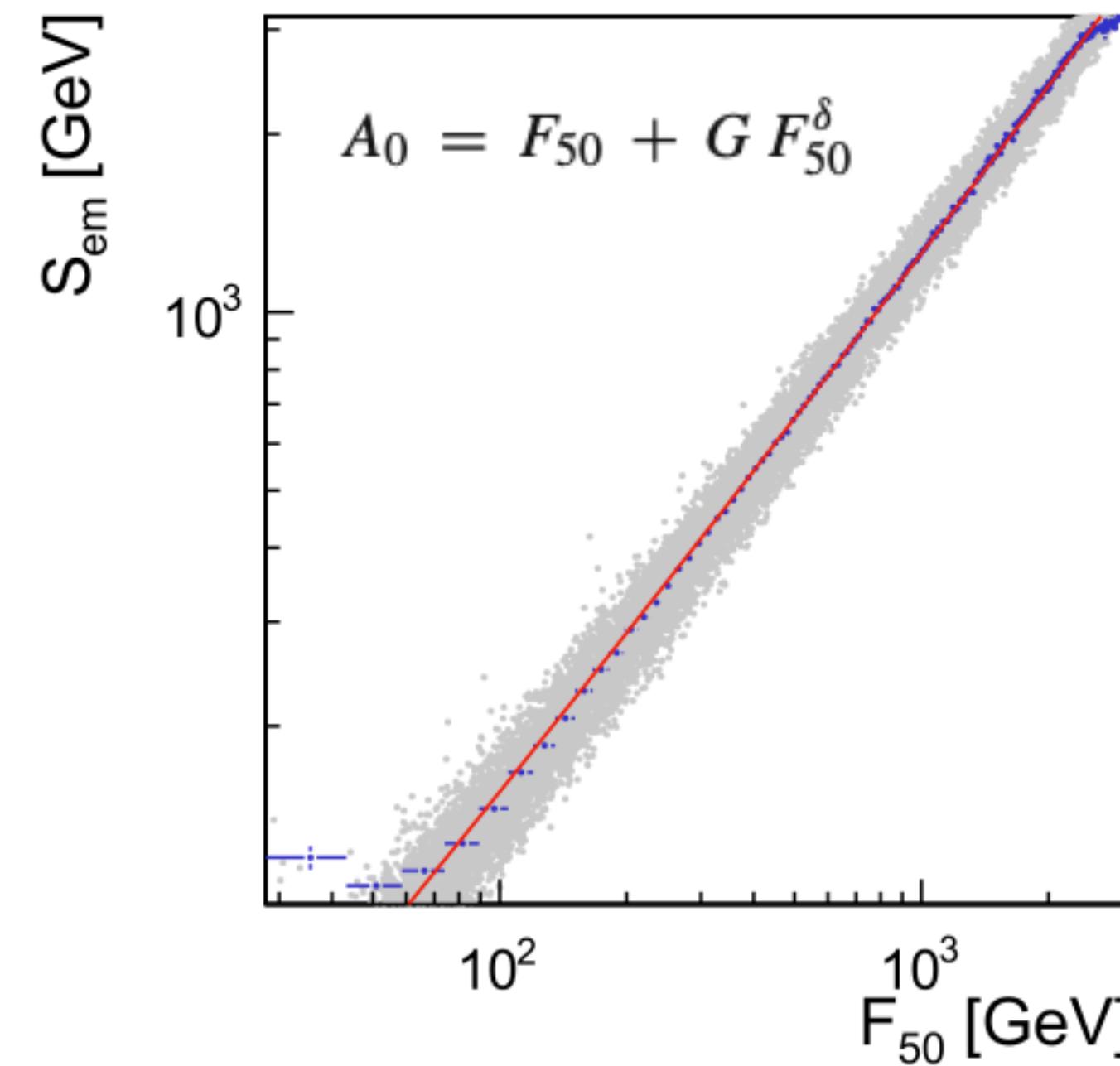
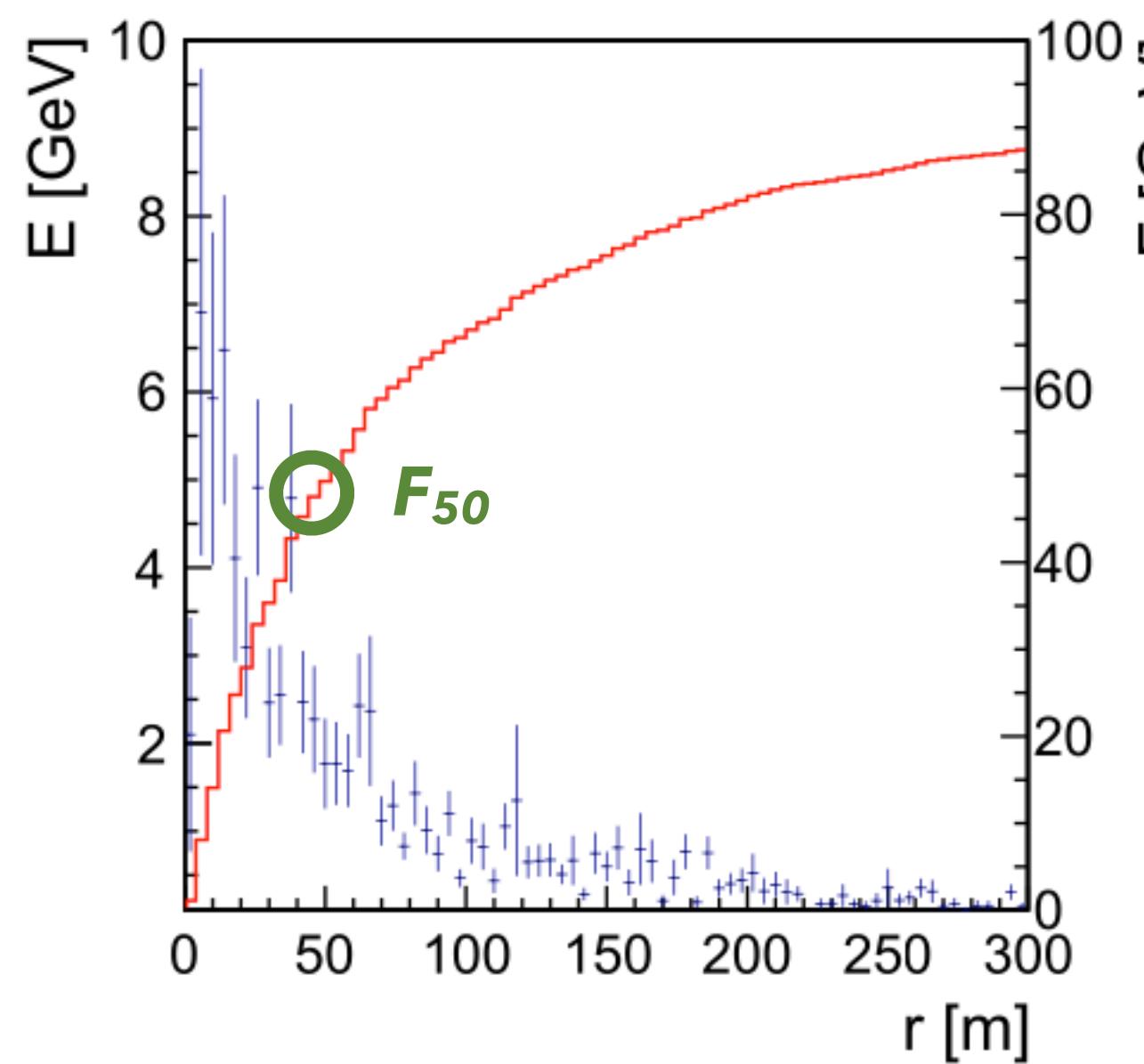


# Simulations

- ❖ Vertical gamma primaries with energies between 250 GeV and 15 TeV simulated with CORSIKA
- ❖ Observation level at 5200 m a.s.l.
- ❖ The **total energy of electromagnetic shower particles** was recorded at the observation level and **histogrammed in radial bins of 4 meters**
- ❖ The signal measured by a water Cherenkov detector is proportional to the energy carried by the electromagnetic shower particles hitting it
- ❖ **Mimic a ground-based gamma-ray observatory** such as LHAASO or the future SWGO

# Energy at the ground ( $S_{\text{em}}$ )

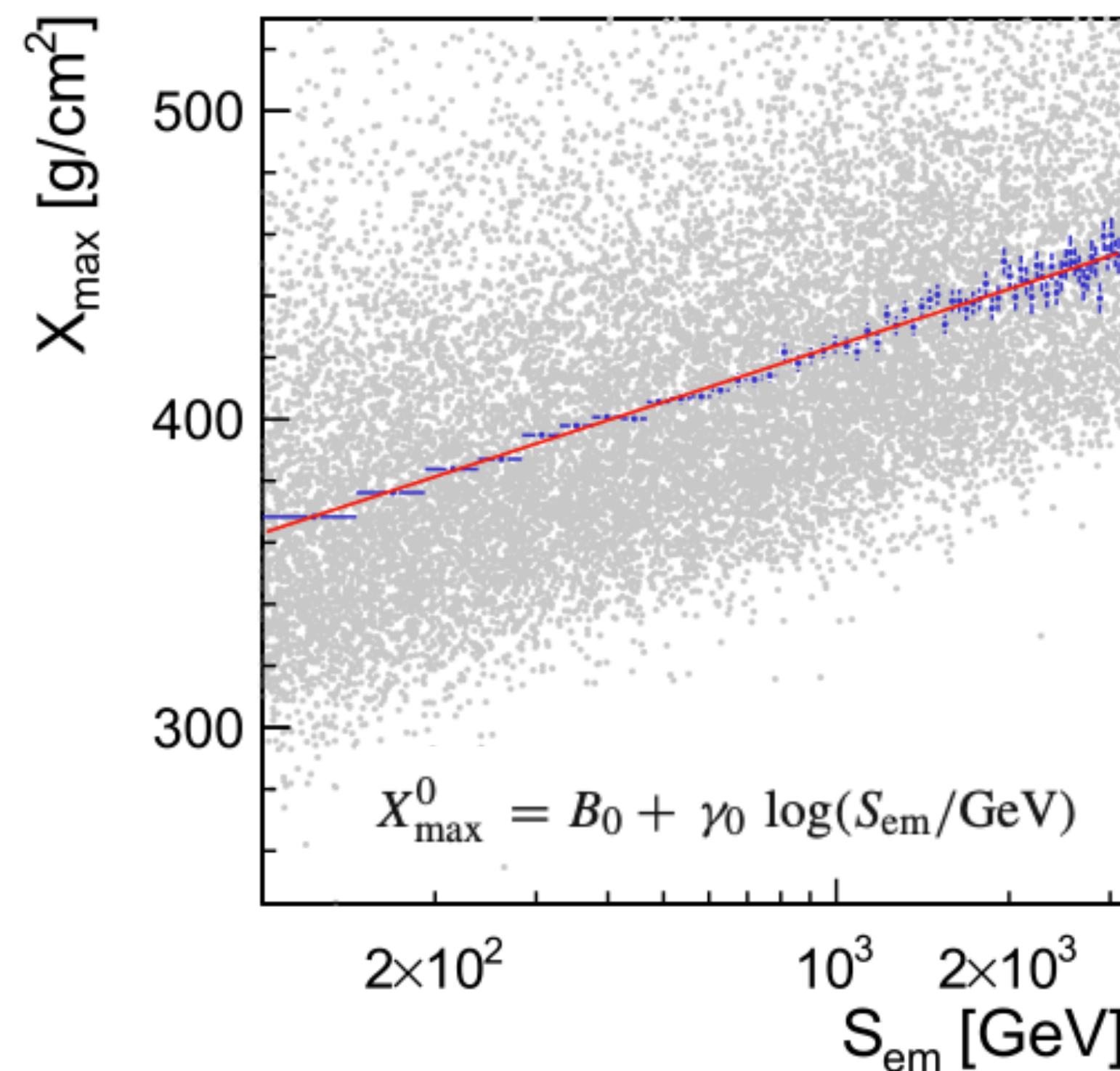
- ✧ Integrate energy (WCD signal) contained within 50 meters from the shower core ( $F_{50}$ )
- ✧  $A_0$  is the estimator for  $S_{\text{em}}$



# Depth of the Shower Maximum ( $X_{\max}$ )

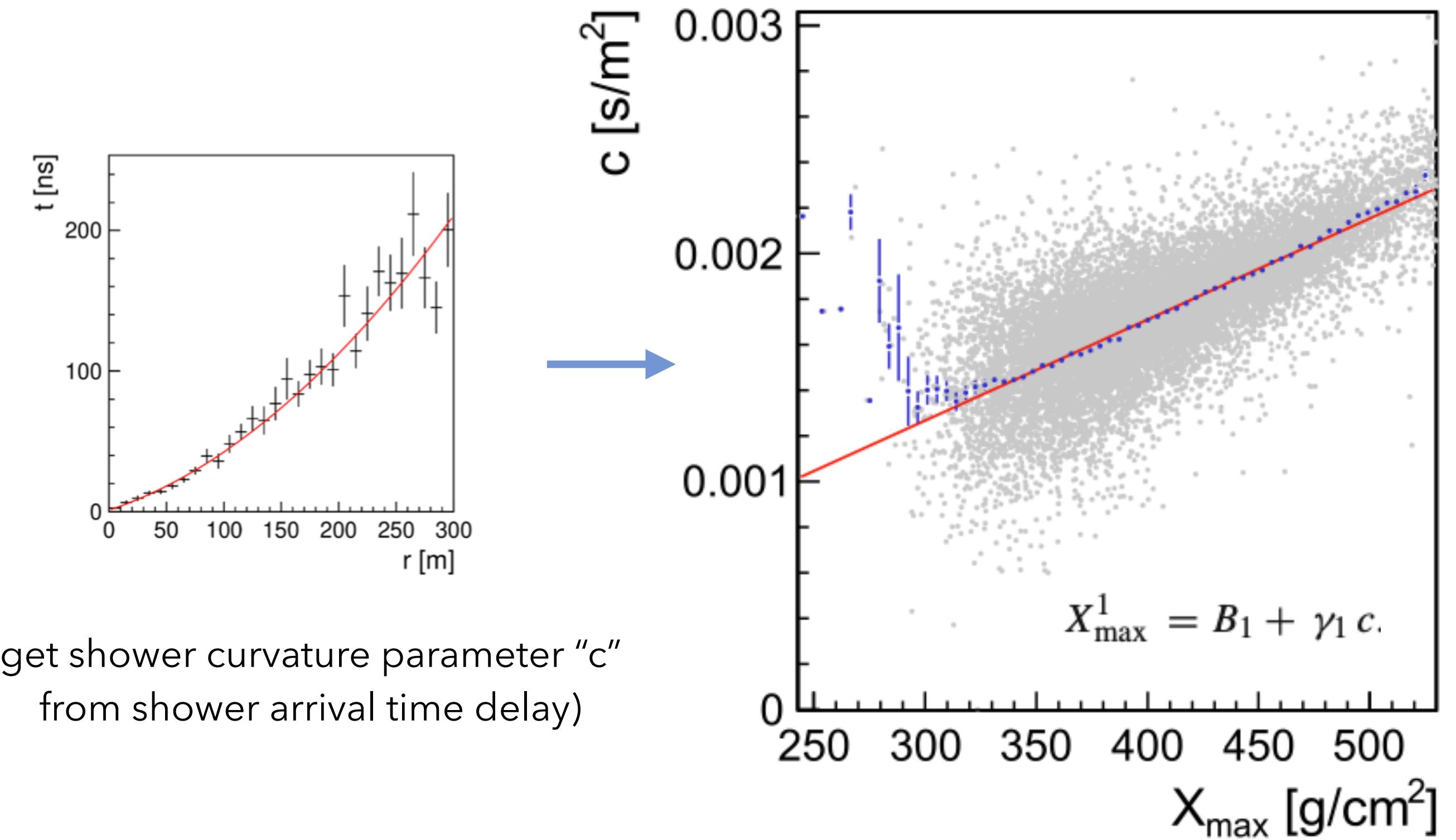
❖ From the  $S_{\text{em}}$

❖  $X_{\max}^0$



❖ From the shower curvature

❖  $X_{\max}^1$

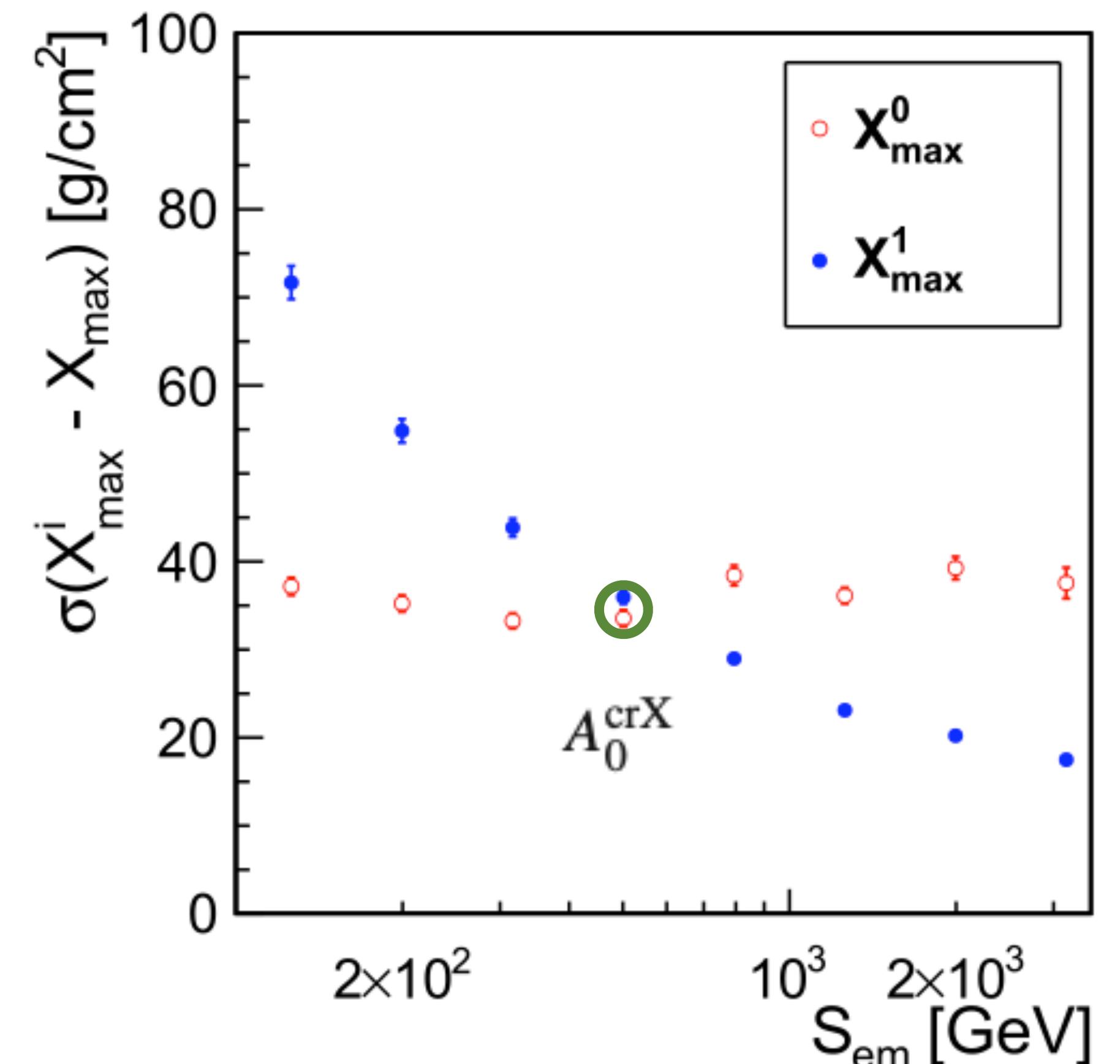


(get shower curvature parameter "c"  
from shower arrival time delay)

# Depth of the Shower Maximum ( $X_{\max}$ )

- ❖ From the  $S_{\text{em}}$ 
  - ❖  $X_{\max}^0$
- ❖ From the shower curvature
  - ❖  $X_{\max}^1$
- ❖ Negligible bias
- Use shower curvature only for high energies

$$X_{\max}^R = \begin{cases} X_{\max}^1 & \text{if } A_0 > A_0^{\text{crX}} \\ & \text{and } X_{\max}^1 > 300 \text{ g cm}^{-2} \\ X_{\max}^0 & \text{otherwise} \end{cases}$$

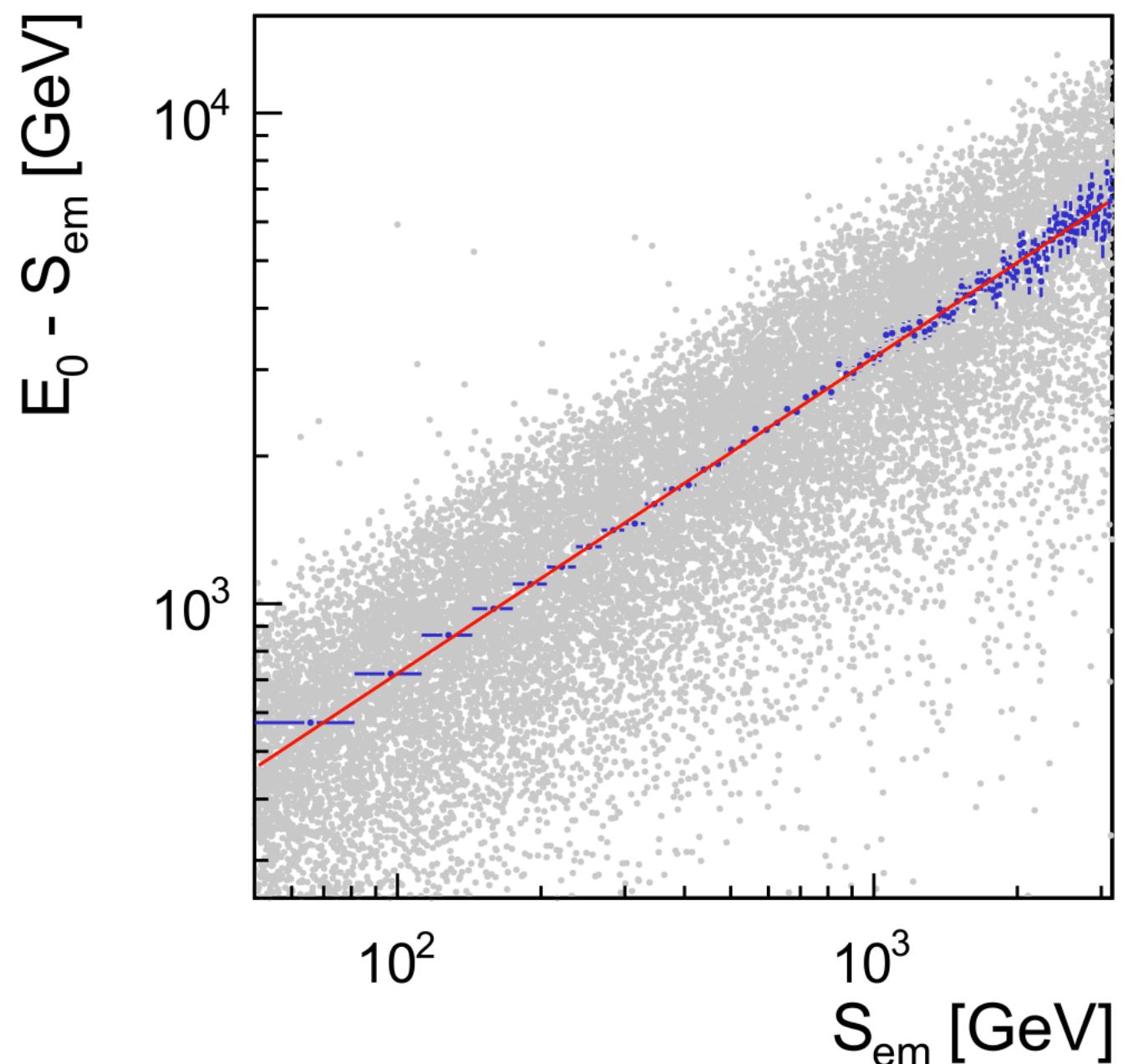


# Measurement of primary energy ( $E_0$ )

Using only  $S_{\text{em}}$

$$E_0^{(1)} = S_{\text{em}} + C (S_{\text{em}})^\beta$$

C - calibration constant

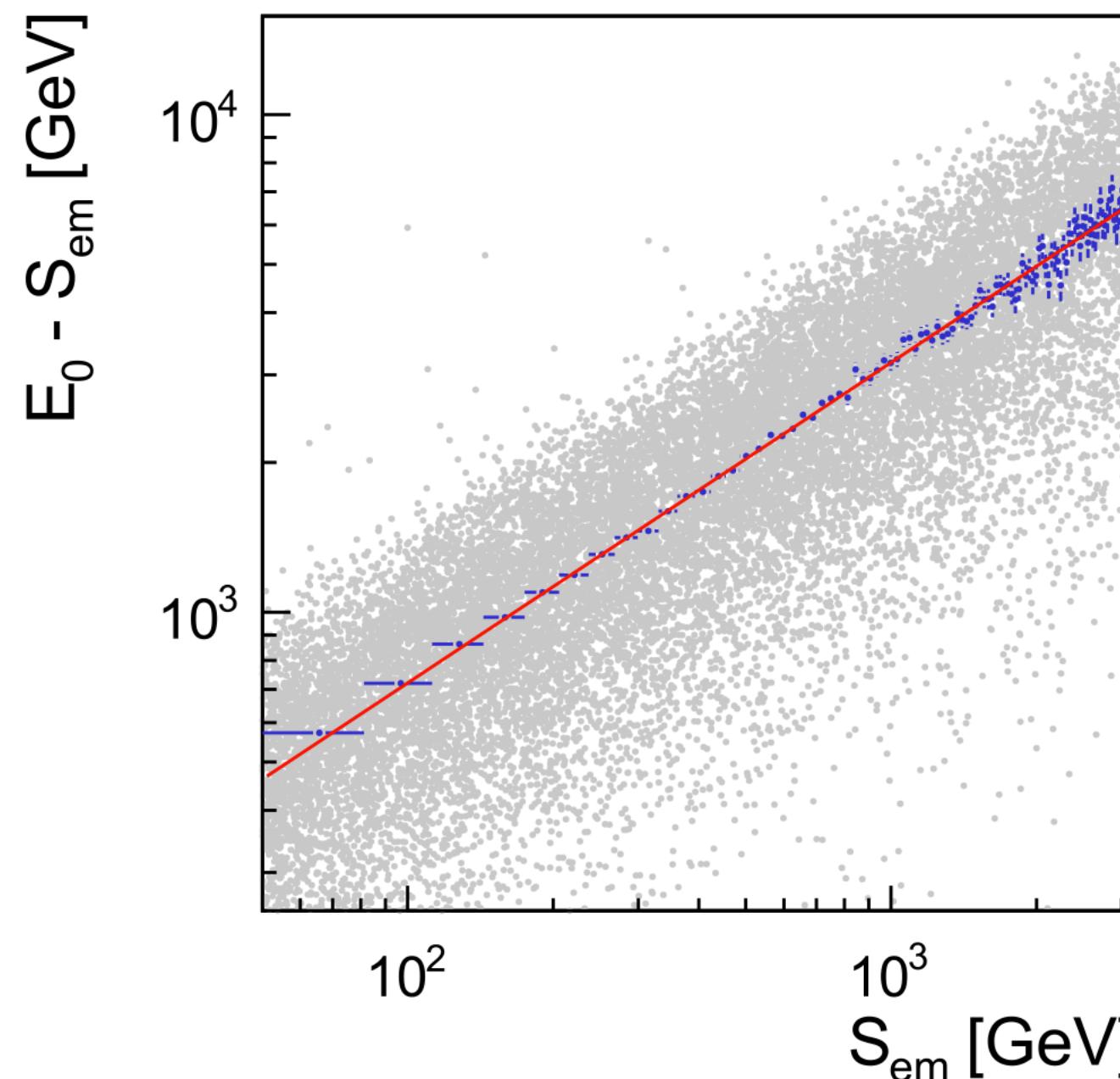


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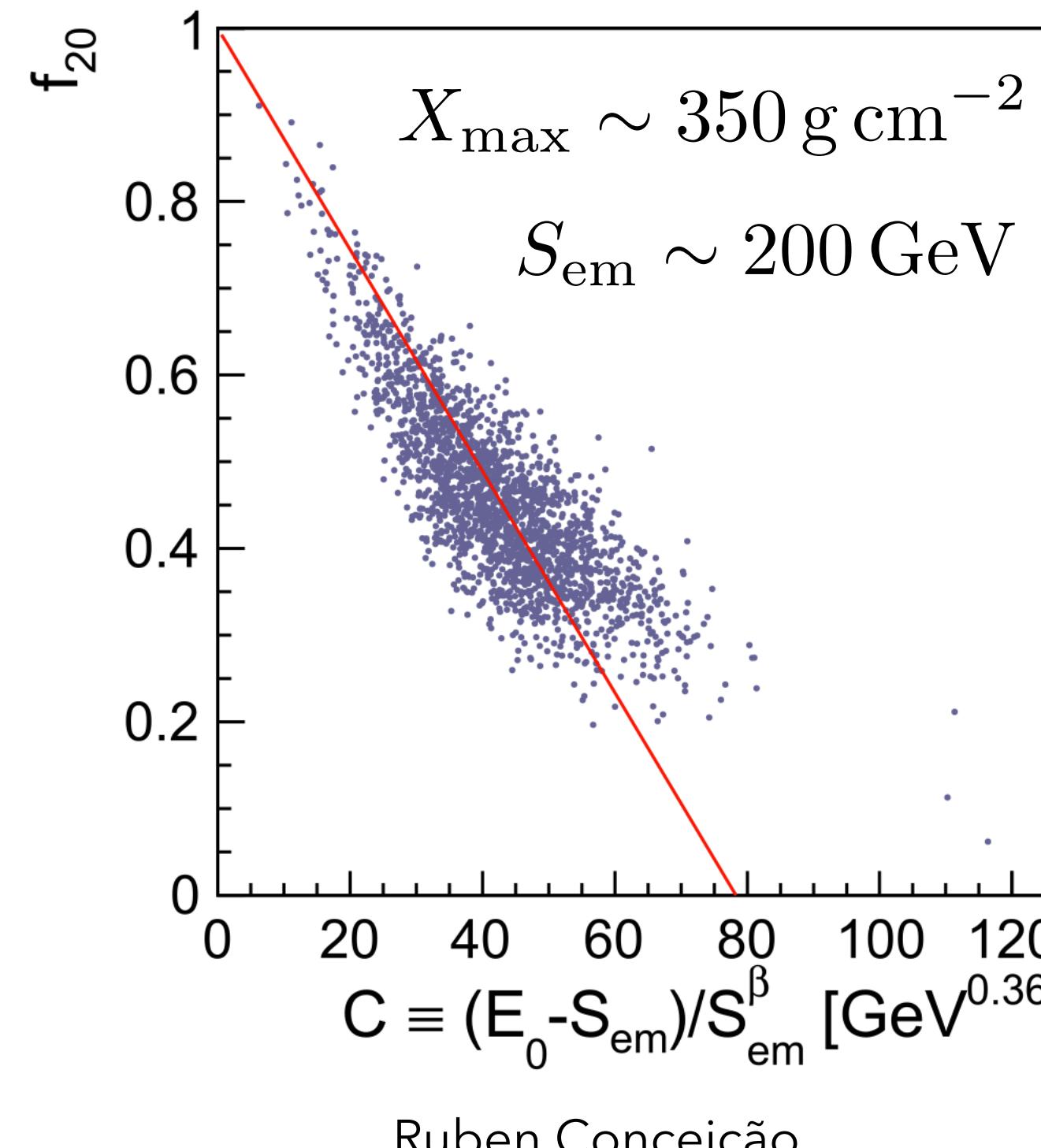
C - calibration constant



Using  $S_{\text{em}}, X_{\text{max}}, f_{20}$

$$E_0^{(2)} = S_{\text{em}} + C(f_{20}, X_{\text{max}}, S_{\text{em}}) (S_{\text{em}})^\beta$$

C - is a function of 3-measured shower observables



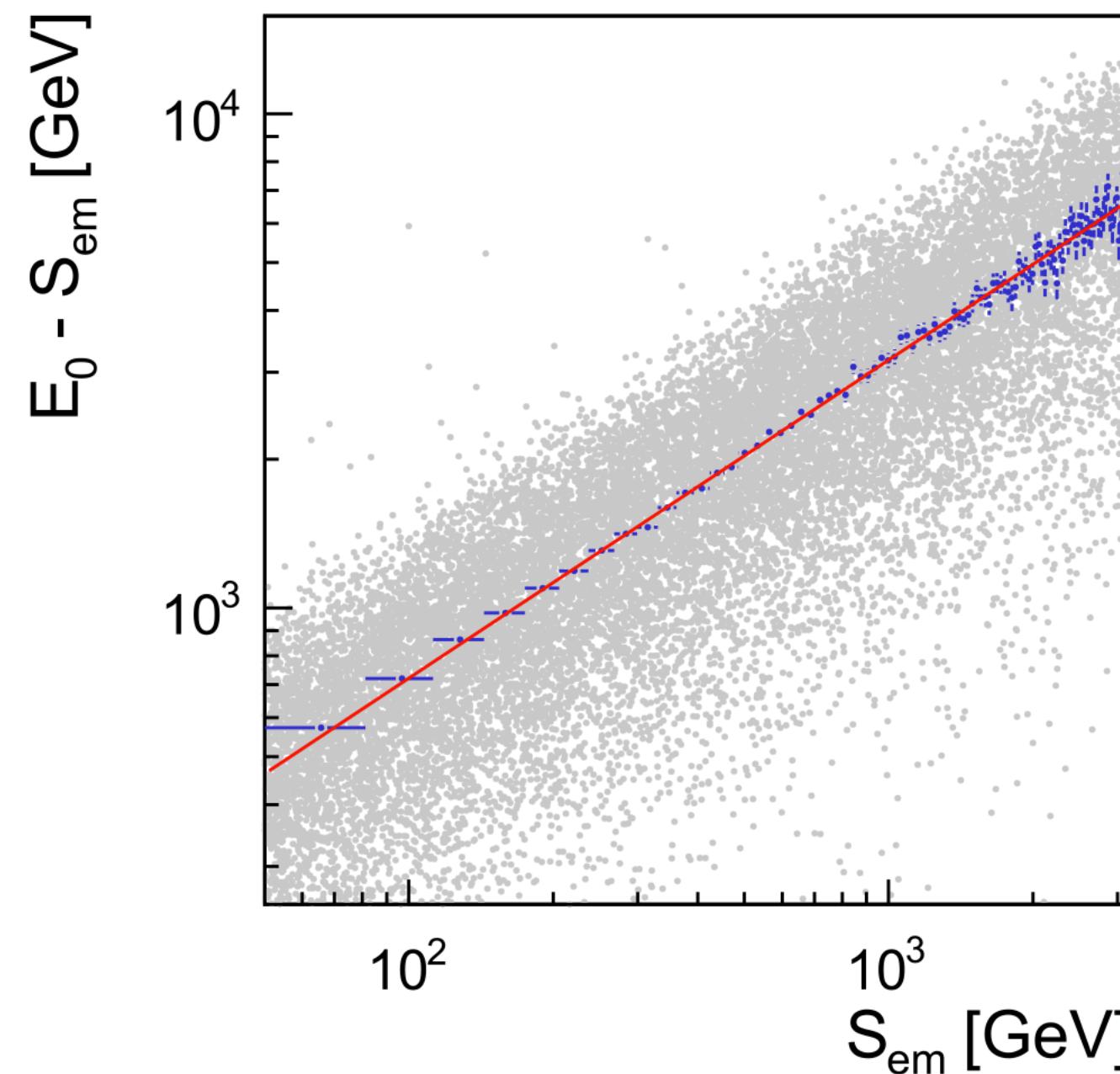
Even with the *same  $X_{\text{max}}$*   
showers can have distinct  
developments leading to a  
*different energy lateral  
distribution function* at the  
ground

# Measurement of primary energy ( $E_0$ )

Using only  $S_{\text{em}}$

$$E_0^{(1)} = S_{\text{em}} + C (S_{\text{em}})^\beta$$

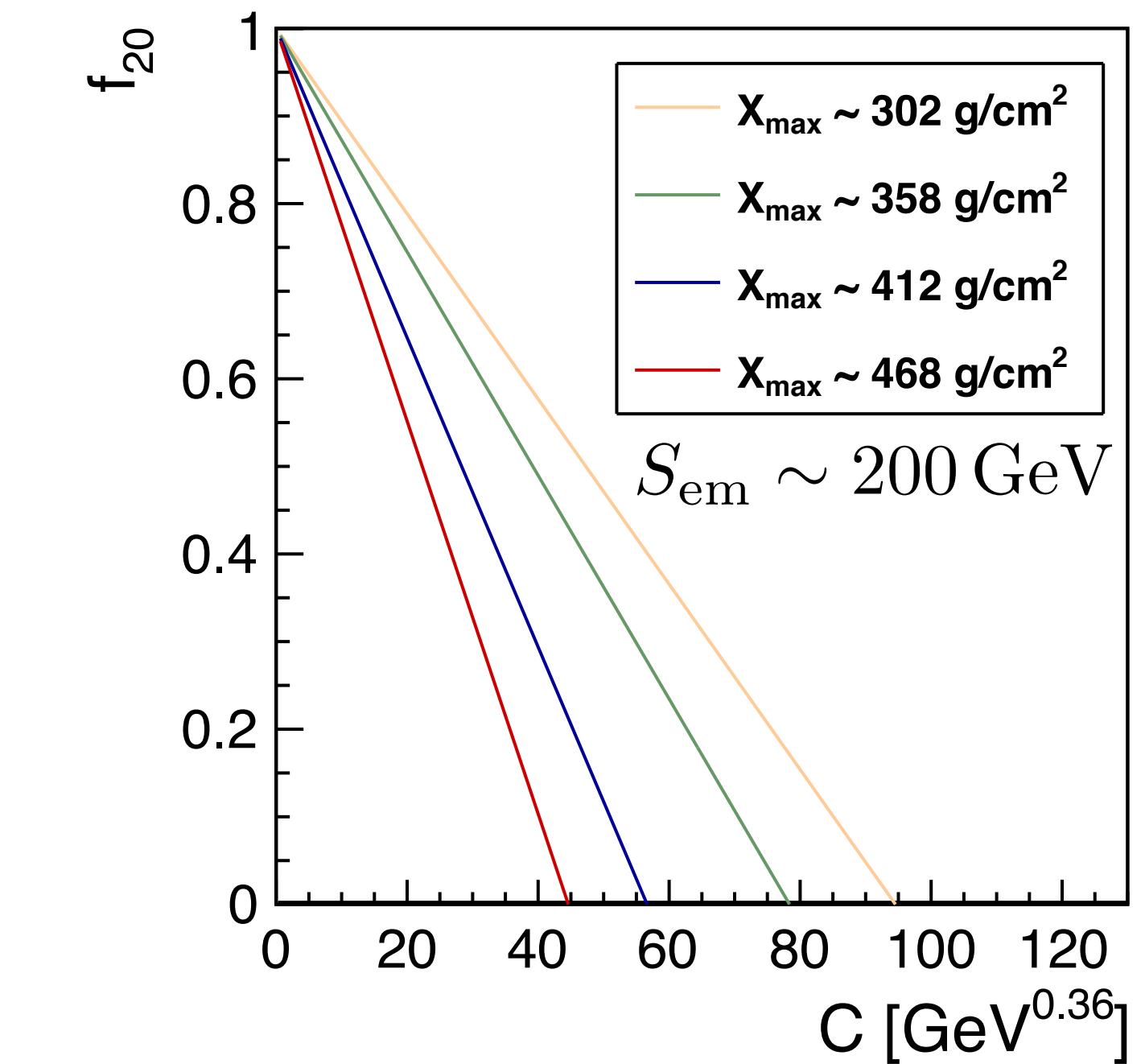
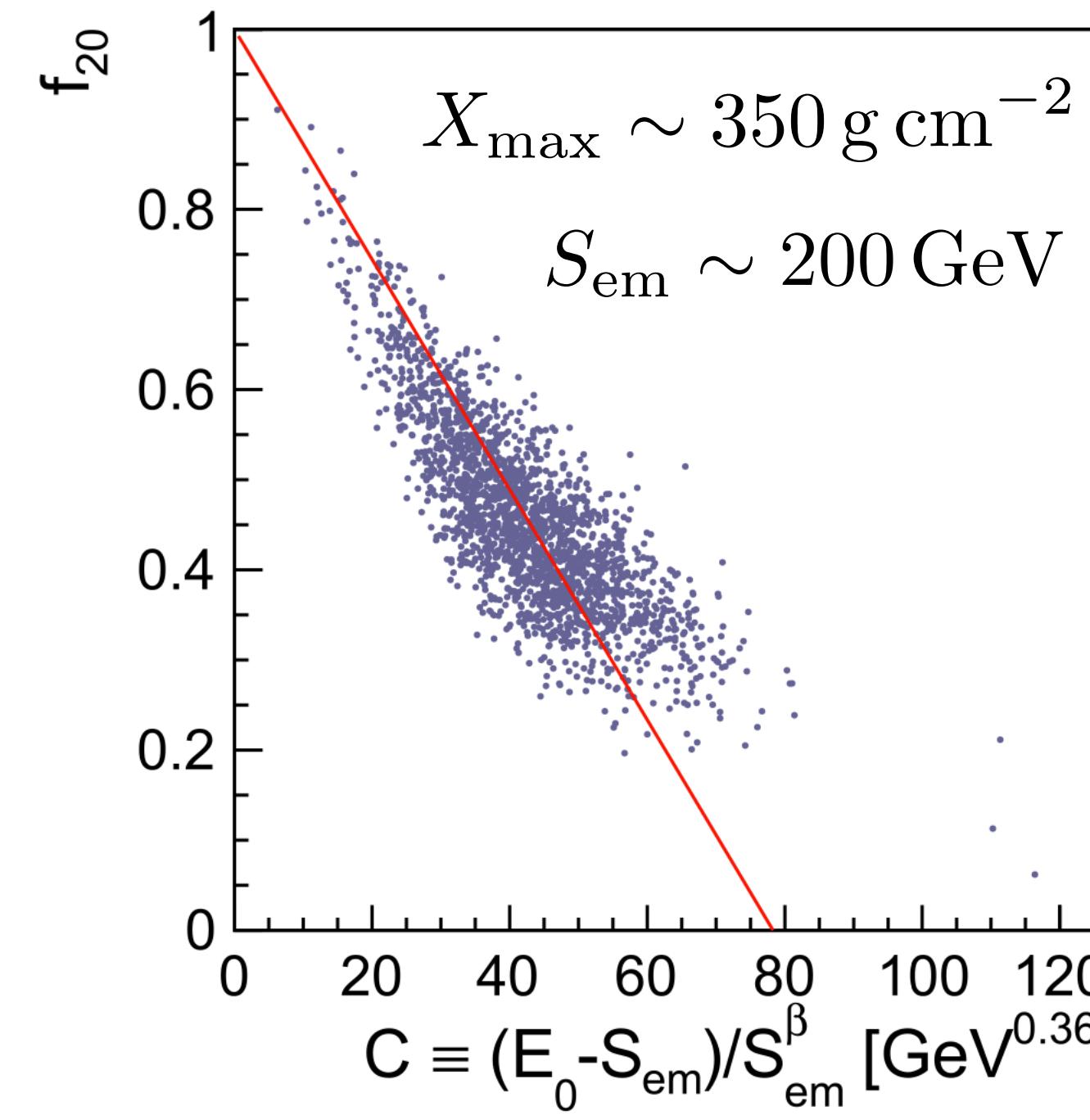
C - calibration constant



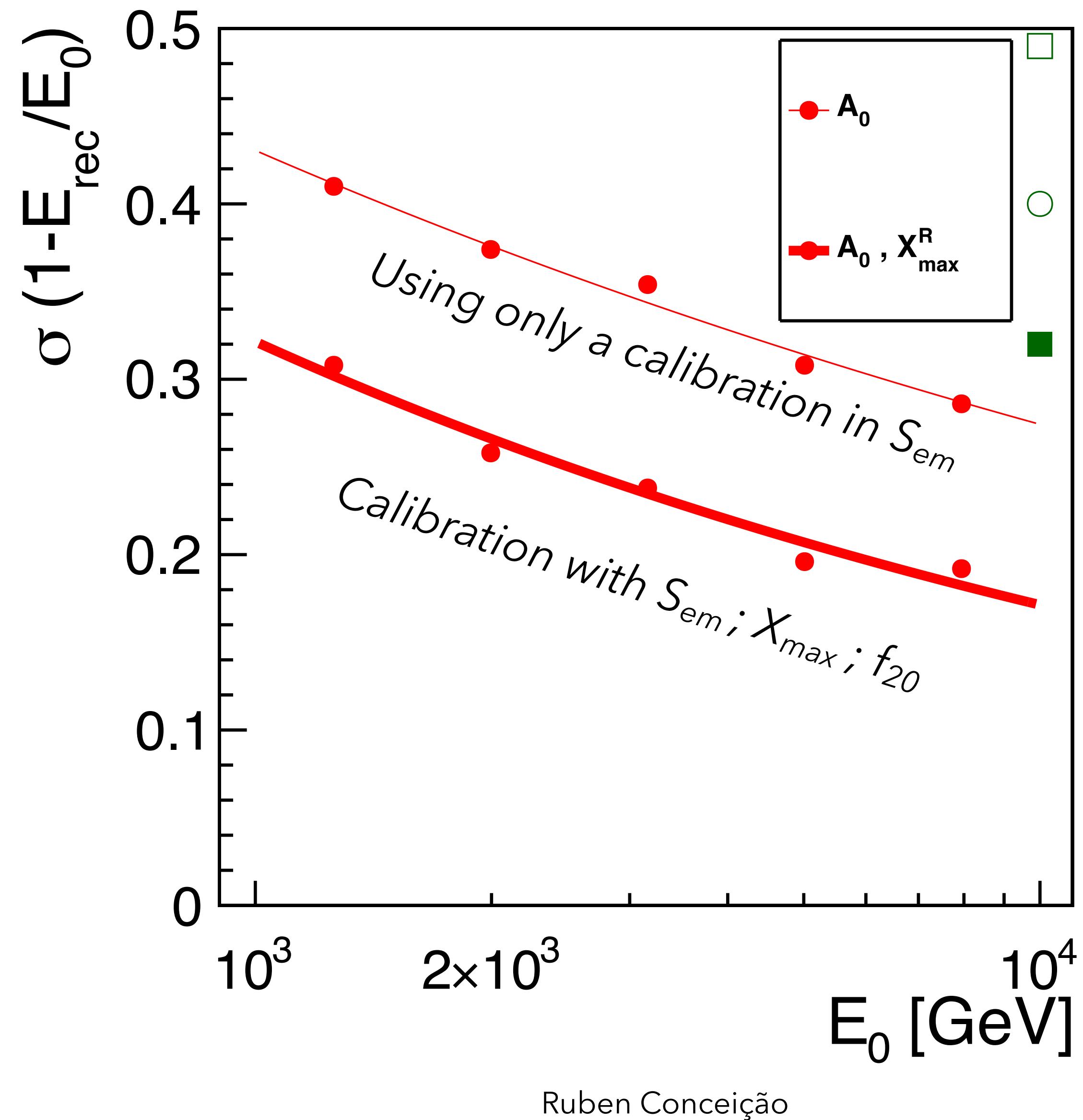
Using  $S_{\text{em}}, X_{\text{max}}, f_{20}$

$$E_0^{(2)} = S_{\text{em}} + C(f_{20}, X_{\text{max}}, S_{\text{em}}) (S_{\text{em}})^\beta$$

C - is a function of 3-measured shower observables



# The final result



MC template -  $\theta < 45^\circ$  (2019)

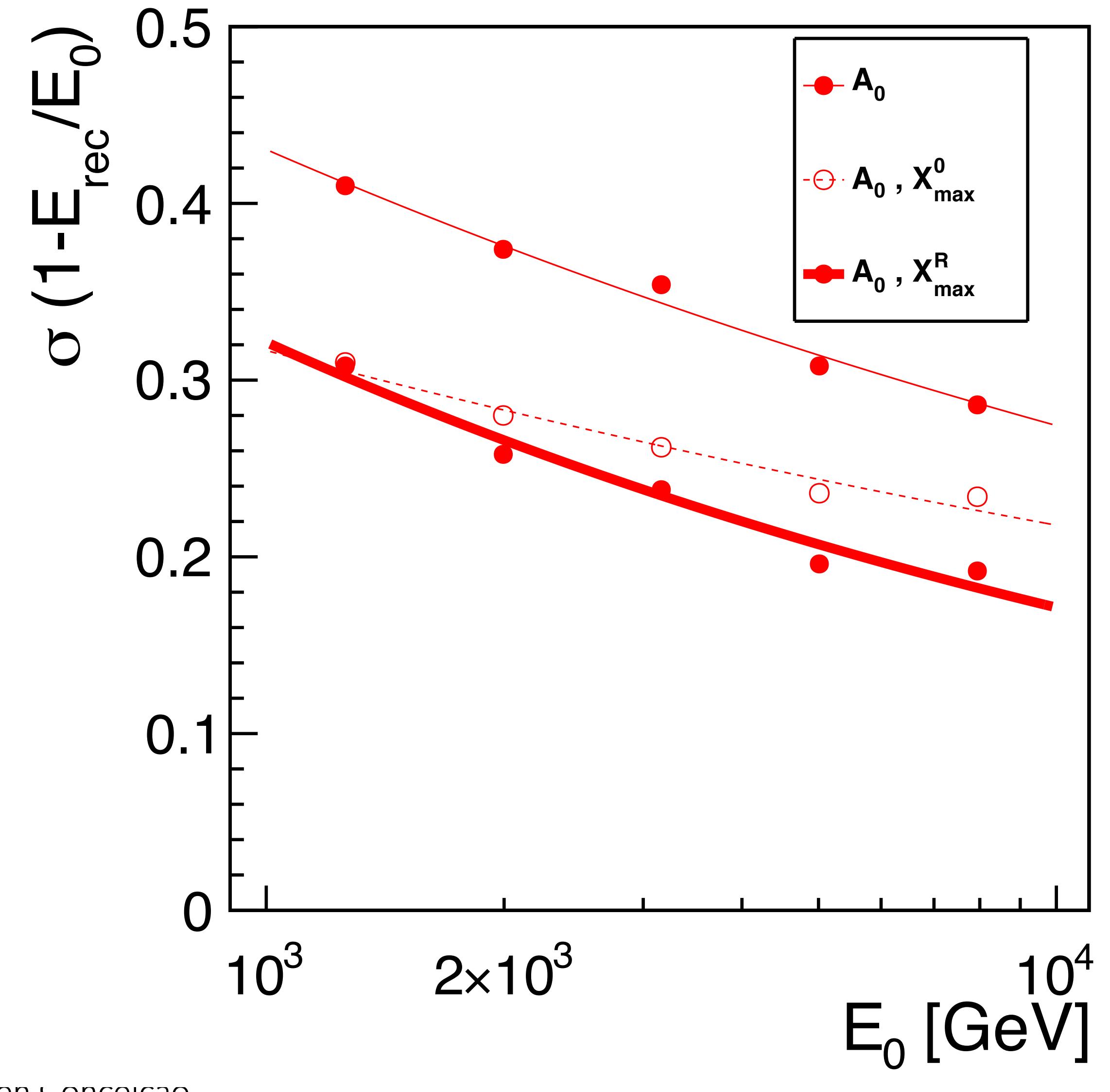
HAWC -  $\theta < 45^\circ$  (2019)

LHASSO -  $\theta = 0^\circ$  (2020)

↓  
*Improvement of  
more than 10%*

# The final result

The measurement of  $X_{\max}$  through the shower curvature has a noticeable effect at the highest energies

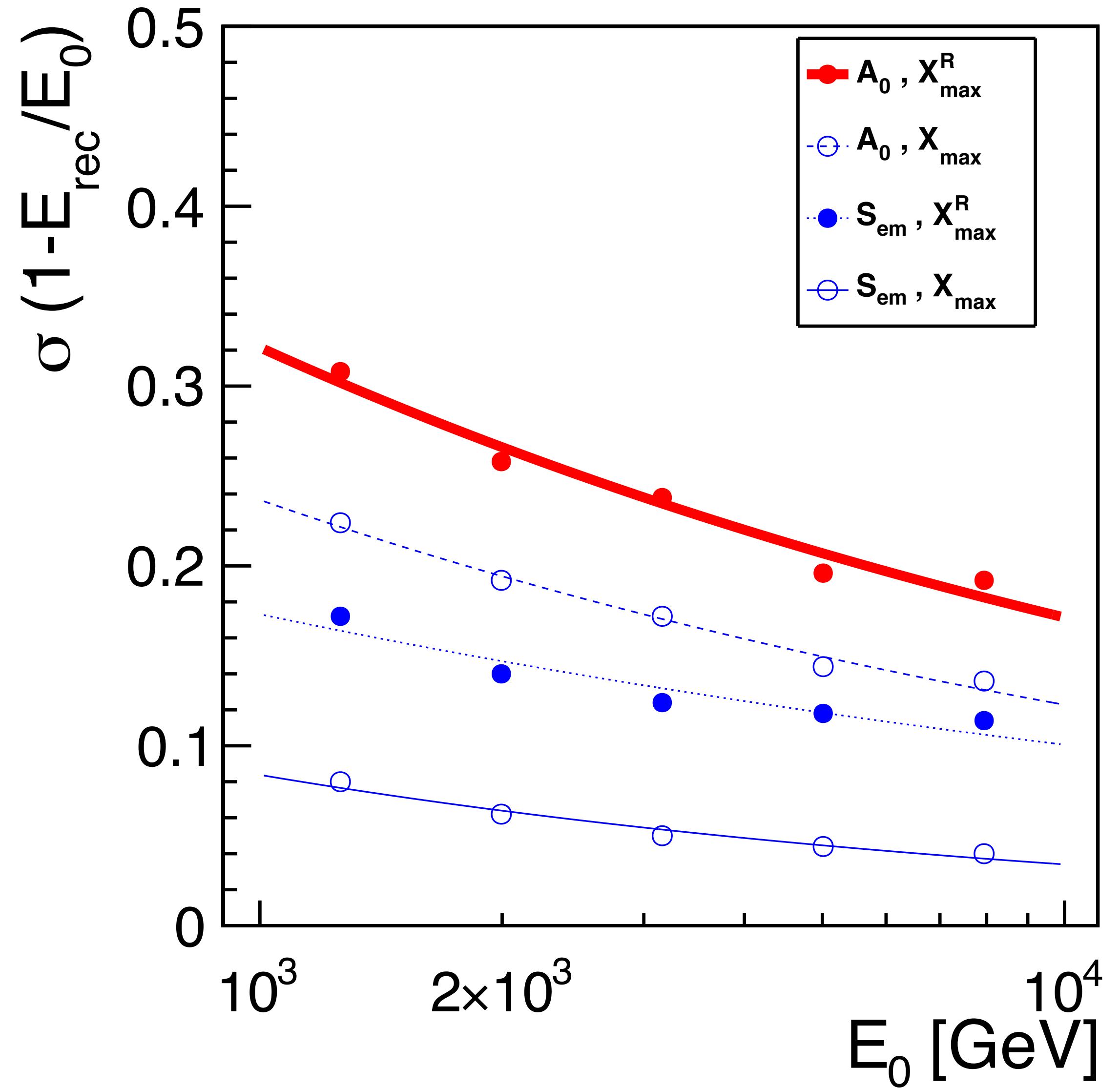


# The final result

As expected the, the determination of the shower stage plays an important role on the energy reconstruction resolution

Knowing  $X_{\max}$  the resolution on the determination of  $S_{\text{em}}$  becomes crucial

There is still space for improvement



# Summary

- ✧ We present a method to improve the energy reconstruction of shower in ground-array gamma-ray observatories
  - ✧ *Eur. Phys. J. C (2021) 81:80 - arXiv:2010.11390 [hep-ph]*
- ✧ The **energy reconstruction is improved through the determination of the shower development stage**, which is achieved combining the following measurable shower quantities:
  - ✧ Energy (signal) collected at the ground,  $S_{\text{em}}$ ;
  - ✧ Estimation of the shower maximum depth,  $X_{\text{max}}$ , through the shower front plane curvature
  - ✧ Fraction of energy collected near the shower core,  $f_{20}$ .

# Acknowledgements



Fundação  
para a Ciência  
e a Tecnologia



PROGRAMA OPERACIONAL COMPETITIVIDADE E INTERNACIONALIZAÇÃO



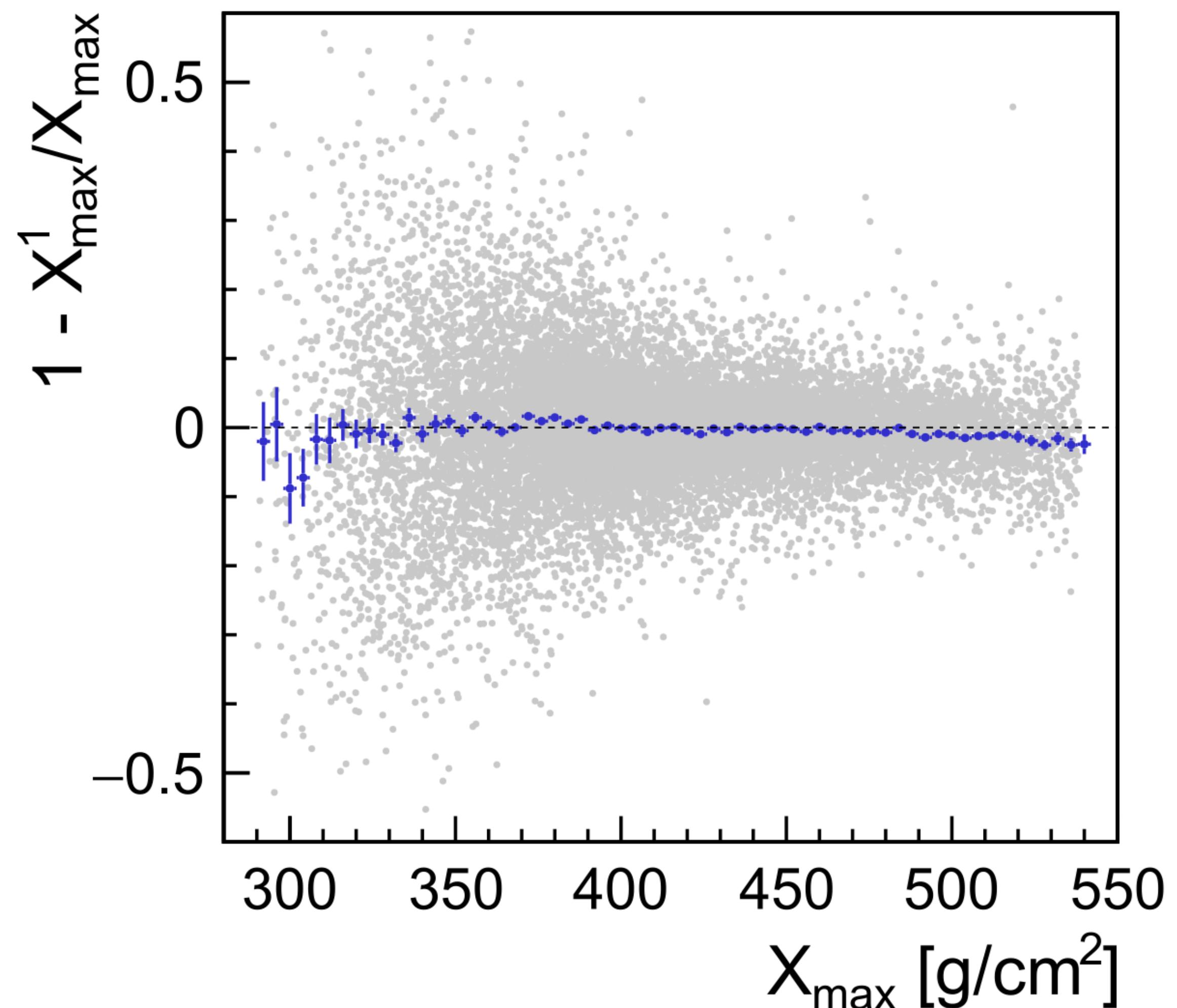
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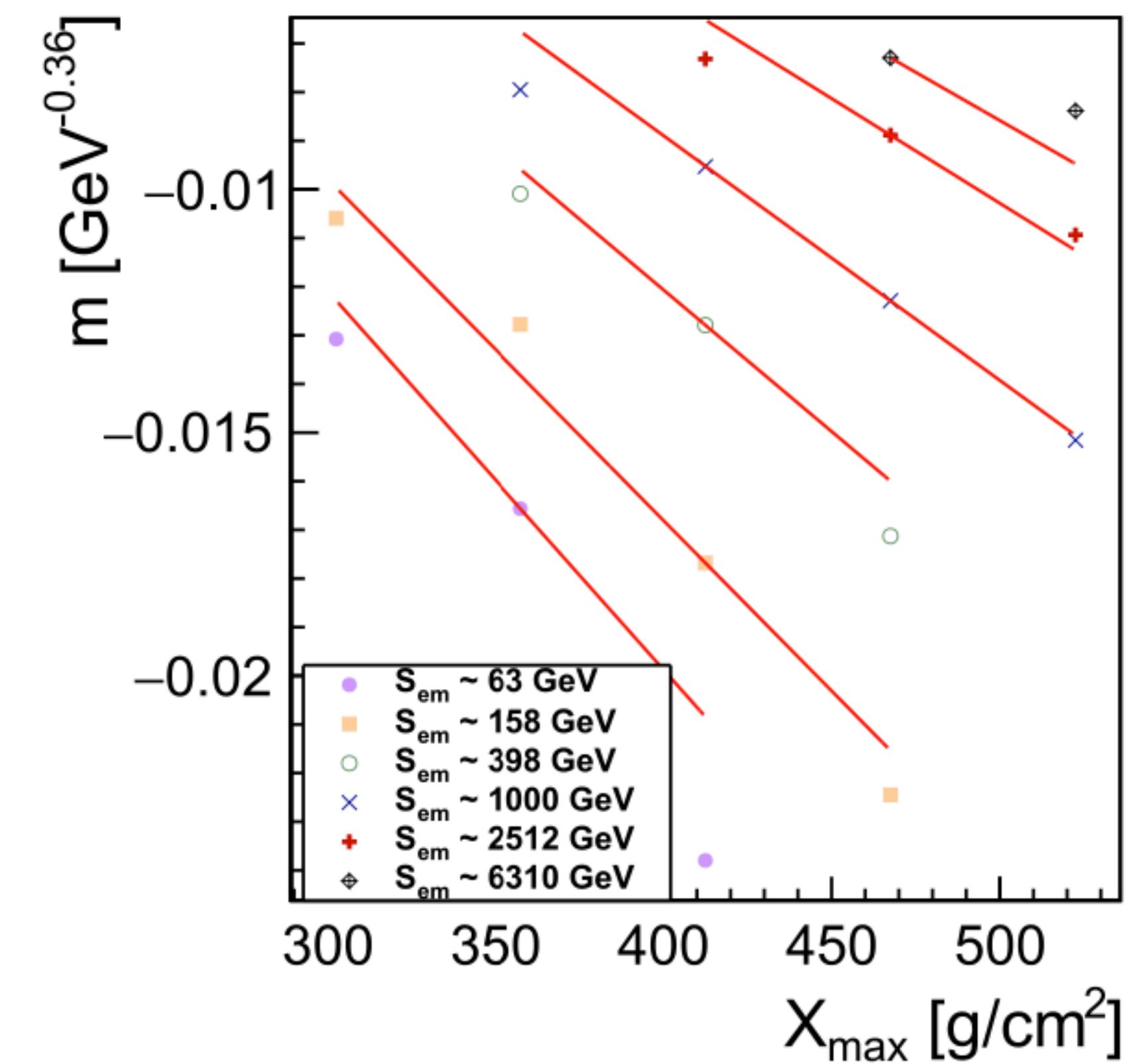
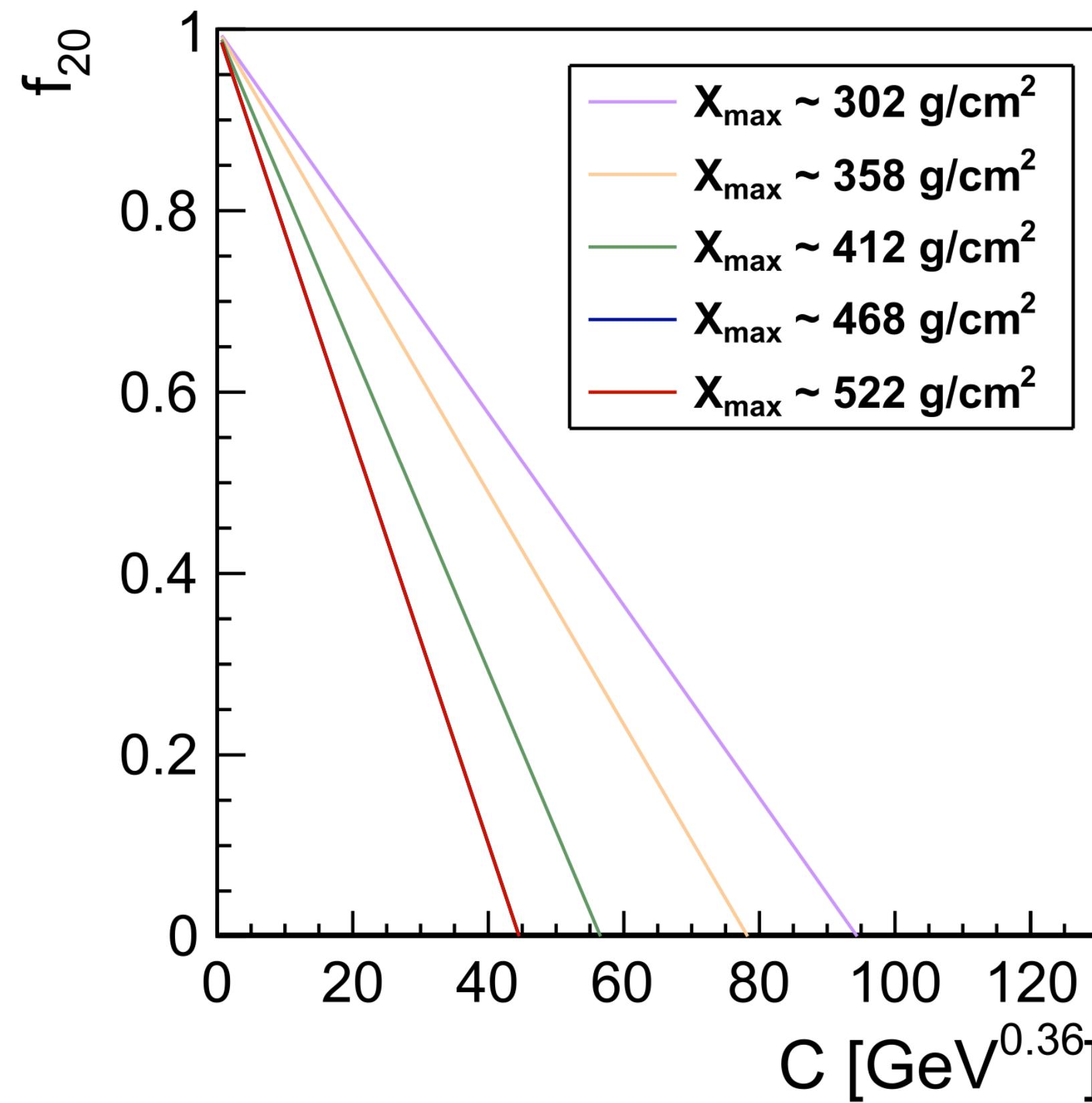


# Backup Slides

# Bias on the determination of $X_{\max}$ using the shower curvature



# $f_{20}$ parametrization



$$f_{20} = 1 + m(X_{\max}, S_{\text{em}}) C(f_{20}, X_{\max}, S_{\text{em}})$$

$$m(X_{\max}, S_{\text{em}}) = b_m + [s_{m0} + s_{m1} \log(S_{\text{em}}/\text{GeV})] X_{\max}$$